



**SCOTT**  
Primary School

*Inspire, Believe, Achieve*

# *Maths Calculation Policy*

*January 2026*

This policy has been largely adapted from the White Rose and Power Maths Resources with further material added. It is a working document and will be revised and amended as necessary.

Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children through the use of concrete, pictorial and abstract representations.

**Maths Mastery:** At the centre of the mastery approach to the teaching of maths is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used across the school, which is in line with the requirements of the 2014 Primary National Curriculum.

**Mathematical Language:** The 2014 National Curriculum is explicit in articulating the importance of children using the correct mathematical language as a central part of their learning (reasoning). In certain year groups, the non-statutory guidance highlights the requirement for children to extend their language around certain concepts. It is therefore essential that teaching using the strategies outlined in this policy is accompanied by the use of appropriate and precise mathematical vocabulary. New vocabulary should be introduced in a suitable context (for example, with relevant, real objects, apparatus, and pictures of diagrams) and explained carefully. High expectations of the mathematical language used are essential, with teachers only accepting what is correct 'The quality and variety of language that pupils hear and speak are key factors in developing their mathematical vocabulary and presenting a mathematically justification, argument or proof.' - 2014 Mathematics Programme of Study

This policy has been designed to teach children through the use of concrete, pictorial and abstract methods. This calculation policy should be used to support children to develop a deep understanding of number and calculation.

**Using the Concrete-Pictorial-Abstract Approach:** Children develop an understanding of a mathematical concept through the three steps of: concrete, pictorial and abstract approach. Reinforcement is achieved by going back and forth between these representations.

**Concrete Representation:** This is the first step in a child's learning. The child is introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and it is the foundation for conceptual understanding.

**Pictorial Representation:** Once the child has sufficiently understood the 'hands on' experience, they can be progressed onto relating them to pictorial representations, such as a diagram or a picture of the problem.

**Abstract Representation:** This is the third step in a child's learning. The child should now be capable of representing problems by using mathematical notation, for example:  $12 \div 2 = 6$

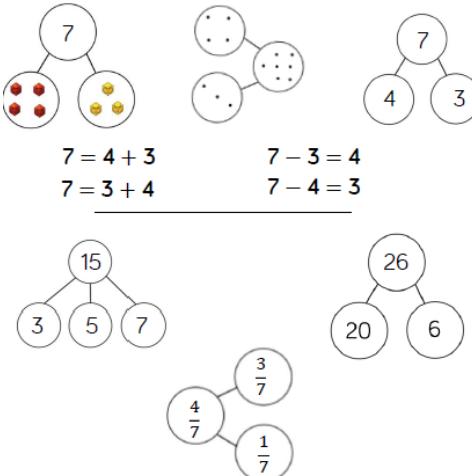
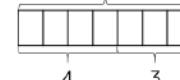
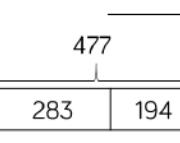
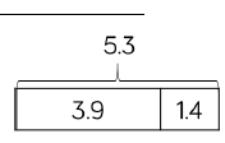
## Maths in the Early Years

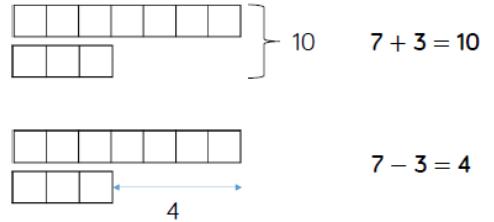
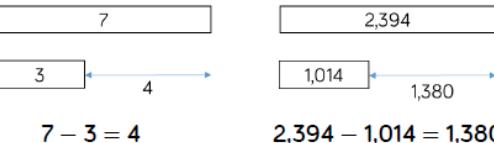
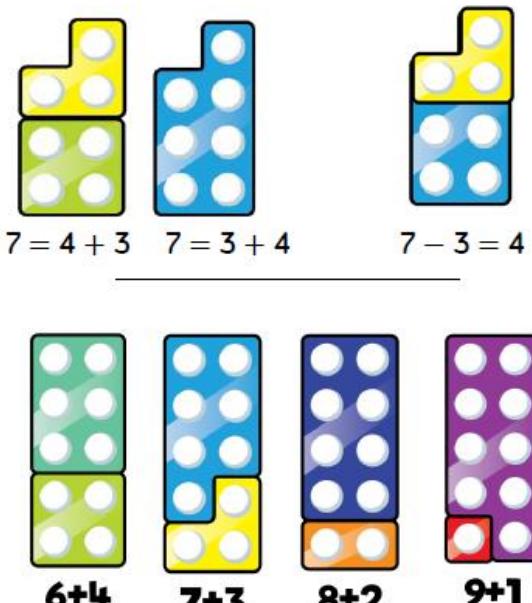
Maths is separated into two areas: 'Number' and 'Numerical Patterns'. Children are taught to count confidently, develop a deep understanding of the numbers to 10, the relationships between them and the patterns within those numbers. By providing frequent and varied opportunities to build and apply this understanding - such as using manipulatives, including small pebbles and tens frames for organising counting - children will develop a secure base of knowledge and vocabulary from which mastery of mathematics is built. In addition, our maths curriculum includes rich opportunities for children to develop their spatial reasoning skills across all areas of mathematics including shape, space and measures. We aim to enable the children to develop positive attitudes and interests in mathematics, look for patterns and relationships, spot connections, 'have a go', talk to adults and peers about what they notice and not be afraid to make mistakes!

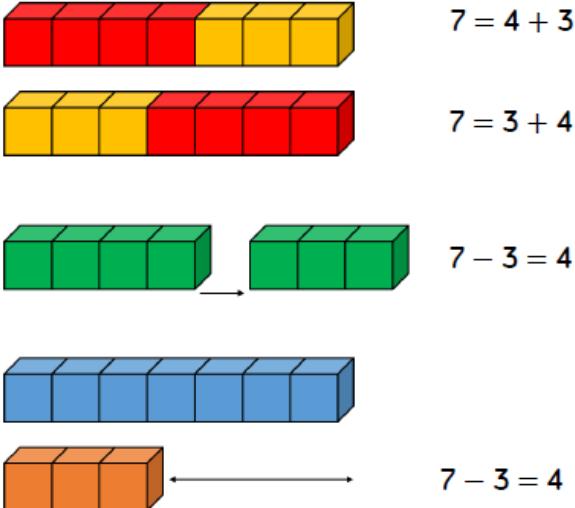
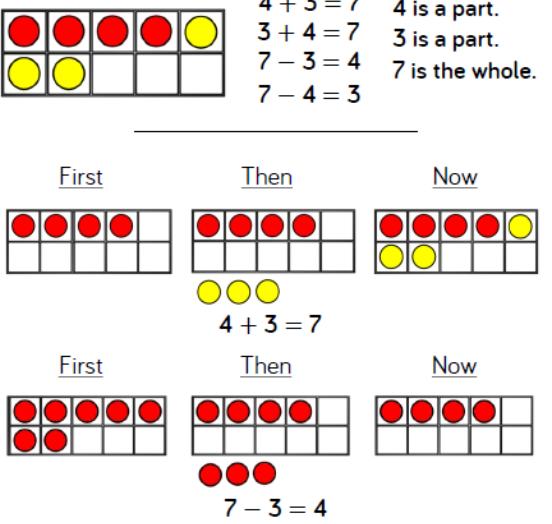
We follow WhiteRose which ensures the five counting principles are taught and embedded:

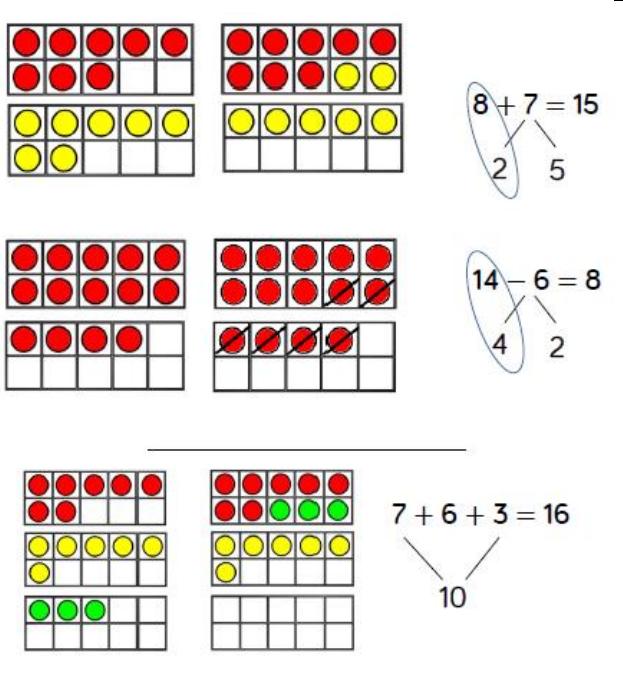
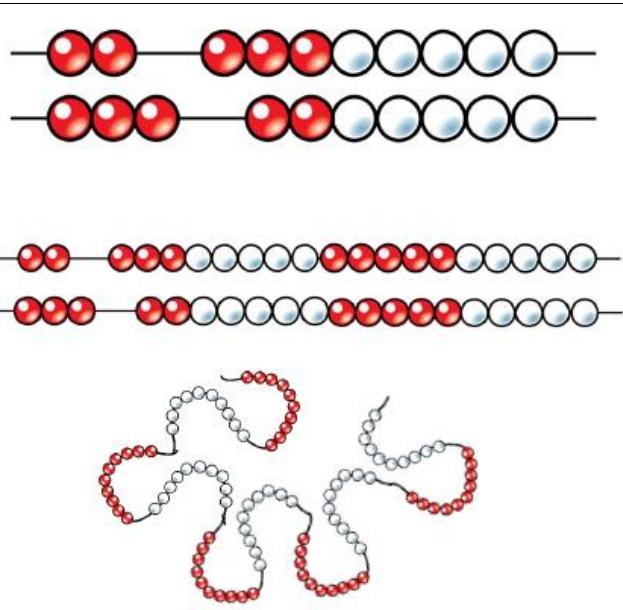
1. **The one-one principle** – This involves the children assigning one number name to each object that is being counted.
2. **The stable-order principle** – Children understand when counting, the numbers have to be said in a certain order.
3. **The cardinal principle** – Children understand that the number name assigned to the final object in a group is the total number of objects in that group.
4. **The abstraction principle** – This involved children understanding that anything can be counted including things that cannot be touched including sounds and movements e.g. jumps.
5. **The order-irrelevance principle** – This involved children understanding that the order we count a group of objects is irrelevant. There will still be the same number.

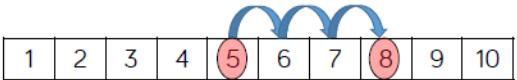
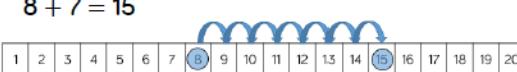
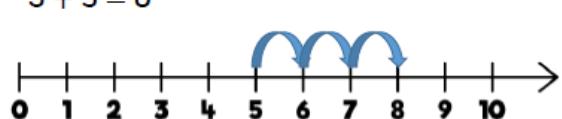
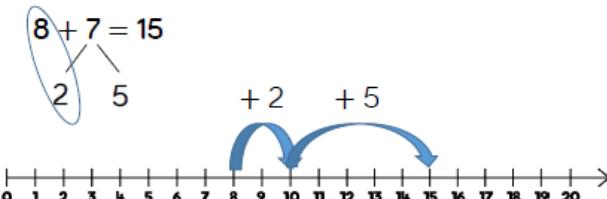
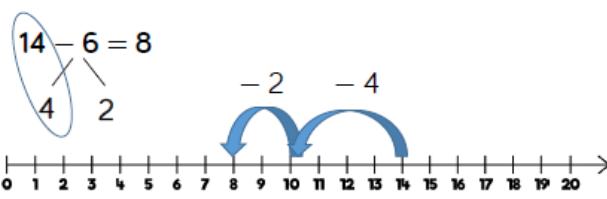
## Overview of Addition and Subtraction Methods Y1-6

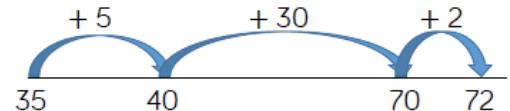
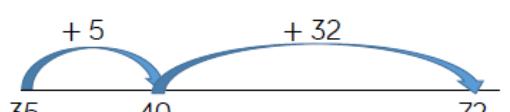
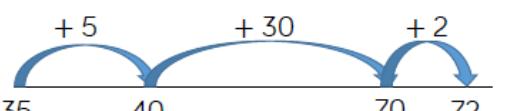
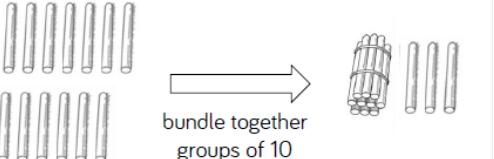
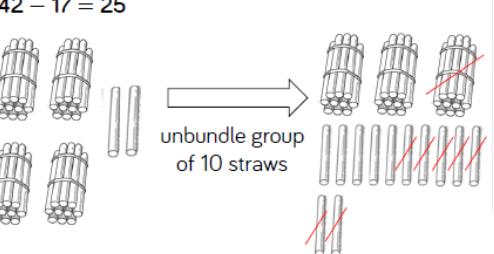
Method	Year Group	Examples	Benefits
Part Whole Models	All	 <p style="text-align: center;"> <math>7 = 4 + 3</math>  <math>7 = 3 + 4</math> </p> <p style="text-align: center;"> <math>7 - 3 = 4</math>  <math>7 - 4 = 3</math> </p>	<p>This part-whole model supports children in their understanding of aggregation and partitioning. Due to its shape, it can be referred to as a cherry part-whole model.</p> <p>When the parts are complete and the whole is empty, children use aggregation to add the parts together to find the total.</p> <p>When the whole is complete and at least one of the parts is empty, children use partitioning (a form of subtraction) to find the missing part. Part-whole models can be used to partition a number into two or more parts, or to help children to partition a number into tens and ones or other place value columns.</p> <p>In KS2, children can apply their understanding of the part-whole model to add and subtract fractions, decimals and percentages.</p>
Bar Model Single	All	<p>Concrete</p>   <p>Discrete</p>   <p>Combination</p>  <p>Continuous</p>  	<p>The single bar model is another type of a part-whole model that can support children in representing calculations to help them unpick the structure.</p> <p>Cubes and counters can be used in a line as a concrete representation of the bar model.</p> <p>Discrete bar models are a good starting point with smaller numbers. Each box represents one whole.</p> <p>The combination bar model can support children to calculate by counting on from the larger number. It is a good stepping stone towards the continuous bar model.</p> <p>Continuous bar models are useful for a range of values. Each rectangle represents a number. The question mark indicates the value to be found. In KS2, children can use bar models to represent larger numbers, decimals and fractions.</p>

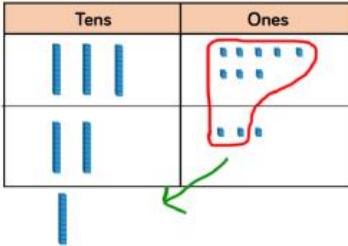
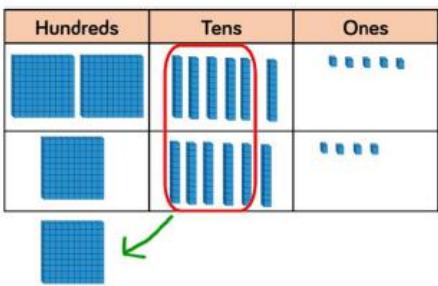
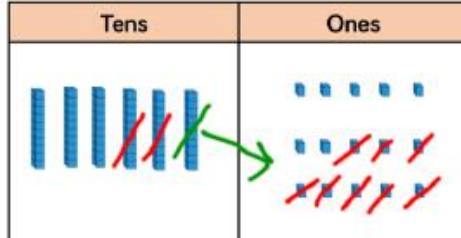
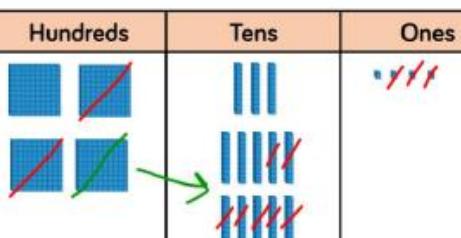
<p>Bar Model Multiple</p>	<p>All</p> <p><u>Discrete</u></p>  <p><u>Continuous</u></p> 	<p>The multiple bar model is a good way to compare quantities whilst still unpicking the structure.</p> <p>Two or more bars can be drawn, with a bracket labelling the whole positioned on the right hand side of the bars. Smaller numbers can be represented with a discrete bar model whilst continuous bar models are more effective for larger numbers.</p> <p>Multiple bar models can also be used to represent the difference in subtraction. An arrow can be used to model the difference.</p> <p>When working with smaller numbers, children can use cubes and a discrete model to find the difference. This supports children to see how counting on can help when finding the difference.</p>
<p>Number Shapes</p>	<p>Early Years , 1, 2</p> 	<p>Number shapes can be useful to support children to subitise numbers as well as explore aggregation, partitioning and number bonds.</p> <p>When adding numbers, children can see how the parts come together making a whole. As children use number shapes more often, they can start to subitise the total due to their familiarity with the shape of each number.</p> <p>When subtracting numbers, children can start with the whole and then place one of the parts on top of the whole to see what part is missing. Again, children will start to be able to subitise the part that is missing due to their familiarity with the shapes.</p> <p>Children can also work systematically to find number bonds. As they increase one number by 1, they can see that the other number decreases by 1 to find all the possible number bonds for a number.</p>

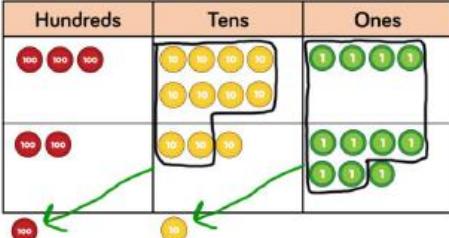
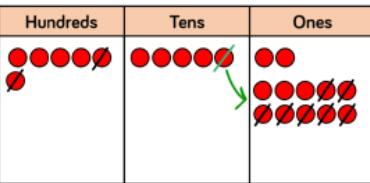
Cubes	EYFS, 1		<p>Cubes can be useful to support children with the addition and subtraction of one-digit numbers.</p> <p>When adding numbers, children can see how the parts come together to make a whole. Children could use two different colours of cubes to represent the numbers before putting them together to create the whole. When subtracting numbers, children can start with the whole and then remove the number of cubes that they are subtracting in order to find the answer. This model of subtraction is reduction, or take away.</p> <p>Cubes can also be useful to look at subtraction as difference. Here, both numbers are made and then lined up to find the difference between the numbers.</p> <p>Cubes are useful when working with smaller numbers but are less efficient with larger numbers as they are difficult to subitise and children may miscount them.</p>
Frames within 10	EYFS Y1		<p>When adding and subtracting within 10, the ten frame can support children to understand the different structures of addition and subtraction.</p> <p>Using the language of parts and wholes represented by objects on the ten frame introduces children to aggregation and partitioning.</p> <p>Aggregation is a form of addition where parts are combined together to make a whole. Partitioning is a form of subtraction where the whole is split into parts. Using these structures, the ten frame can enable children to find all the number bonds for a number.</p> <p>Children can also use ten frames to look at augmentation (increasing a number) and take-away (decreasing a number). This can be introduced through a first, then, now structure which shows the change in the number in the 'then' stage. This can be put into a story structure to help children understand the change e.g. First, there were 7 cars. Then, 3 cars left. Now, there are 4 cars.</p>

<p>Frames within 20</p> <p>Y2</p>		<p>When adding two single digits, children can make each number on separate ten frames before moving part of one number to make 10 on one of the ten frames. This supports children to see how they have partitioned one of the numbers to make 10, and makes links to effective mental methods of addition.</p> <p>When subtracting a one-digit number from a two-digit number, firstly make the larger number on 2 ten frames. Remove the smaller number, thinking carefully about how you have partitioned the number to make 10, this supports mental methods of subtraction.</p> <p>When adding three single-digit numbers, children can make each number on 3 separate 10 frames before considering which order to add the numbers in. They may be able to find a number bond to 10 which makes the calculation easier. Once again, the ten frames support the link to effective mental methods of addition as well as the importance of commutativity.</p>
<p>Bead Strings</p> <p>Year 1</p>		<p>Different sizes of bead strings can support children at different stages of addition and subtraction.</p> <p>Bead strings to 10 are very effective at helping children to investigate number bonds up to 10.</p> <p>They can help children to systematically find all the number bonds to 10 by moving one bead at a time to see the different numbers they have partitioned the 10 beads into e.g. <math>2 + 8 = 10</math>, move one bead, <math>3 + 7 = 10</math>.</p> <p>Bead strings to 20 work in a similar way but they also group the beads in fives. Children can apply their knowledge of number bonds to 10 and see the links to number bonds to 20.</p> <p>Bead strings to 100 are grouped in tens and can support children in number bonds to 100 as well as helping when adding by making ten. Bead strings can show a link to adding to the next 10 on number lines which supports a mental method of addition.</p>

Number Tracks	Year 1	<p><math>5 + 3 = 8</math></p>  <p><math>10 - 4 = 6</math></p>  <p><math>8 + 7 = 15</math></p> 	Number tracks are useful to support children in their understanding of augmentation and reduction.  When adding, children count on to find the total of the numbers. On a number track, children can place a counter on the starting number and then count on to find the total.  When subtracting, children count back to find their answer. They start at the minuend and then take away the subtrahend to find the difference between the numbers.  Number tracks can work well alongside ten frames and bead strings which can also model counting on or counting back.  Playing board games can help children to become familiar with the idea of counting on using a number track before they move on to number lines.
Labelled Number Lines	Year 2	<p><math>5 + 3 = 8</math></p>  <p><math>8 + 7 = 15</math></p>  <p><math>14 - 6 = 8</math></p> 	Labelled number lines support children in their understanding of addition and subtraction as augmentation and reduction.  Children can start by counting on or back in ones, up or down the number line. This skill links directly to the use of the number track.  Progressing further, children can add numbers by jumping to the nearest 10 and then jumping to the total. This links to the making 10 method which can also be supported by ten frames. The smaller number is partitioned to support children to make a number bond to 10 and to then add on the remaining part.  Children can subtract numbers by firstly jumping to the nearest 10. Again, this can be supported by ten frames so children can see how they partition the smaller number into the two separate jumps.

<p>Blank Number Lines</p>	<p>Year 2</p> <p><math>35 + 37 = 72</math></p>  <p><math>35 + 37 = 72</math></p>  <p><math>72 - 35 = 37</math></p> 	<p>Blank number lines provide children with a structure to add and subtract numbers in smaller parts.</p> <p>Developing from labelled number lines, children can add by jumping to the nearest 10 and then adding the rest of the number either as a whole or by adding the tens and ones separately.</p> <p>Children may also count back on a number line to subtract, again by jumping to the nearest 10 and then subtracting the rest of the number.</p> <p>Blank number lines can also be used effectively to help children subtract by finding the difference between numbers. This can be done by starting with the smaller number and then counting on to the larger number. They then add up the parts they have counted on to find the difference between the numbers.</p>
<p>Straws</p>	<p>Year 2</p> <p><math>7 + 6 = 13</math></p>  <p><math>42 - 17 = 25</math></p> 	<p>Straws are an effective way to support children in their understanding of exchange when adding and subtracting 2-digit numbers.</p> <p>Children can be introduced to the idea of bundling groups of ten when adding smaller numbers and when representing 2-digit numbers. Use elastic bands or other ties to make bundles of ten straws.</p> <p>When adding numbers, children bundle a group of 10 straws to represent the exchange from 10 ones to 1 ten. They then add the individual straws (ones) and bundles of straws (tens) to find the total.</p> <p>When subtracting numbers, children unbundle a group of 10 straws to represent the exchange from 1 ten to 10 ones.</p> <p>Straws provide a good stepping stone to adding and subtracting with Base 10/Dienes.</p>

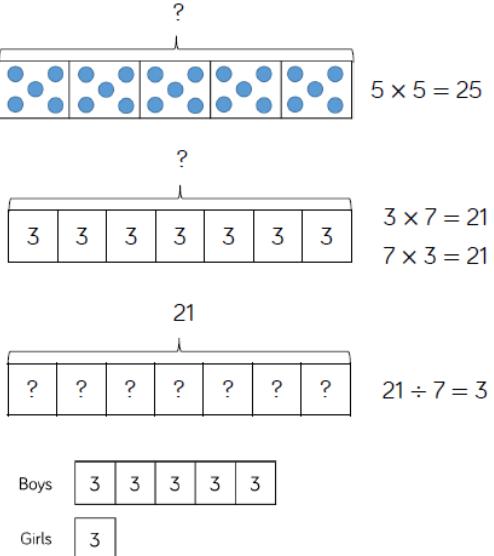
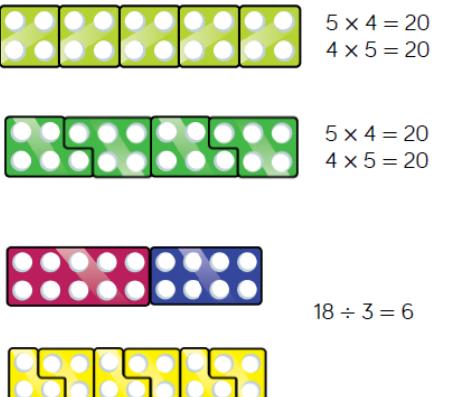
<p>Base 10 Addition</p> <p>KS2</p>	 	<p>Using Base 10 or Dienes is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.</p> <p>Children should first add without an exchange before moving on to addition with exchange.. The representation becomes less efficient with larger numbers due to the size of Base 10. In this case, place value counters may be the better model to use.</p> <p>When adding, always start with the smallest place value column. Here are some questions to support children.</p> <ul style="list-style-type: none"> <li>• How many ones are there altogether?</li> <li>• Can we make an exchange? (Yes or No)</li> <li>• How many do we exchange? (10 ones for 1 ten, show exchanged 10 in tens column by writing 1 in column)</li> <li>• How many ones do we have left? (Write in ones column)</li> <li>• Repeat for each column.</li> </ul>
<p>Base 10 Subtraction</p> <p>KS2</p>	 	<p>Using Base 10 or Dienes is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.</p> <p>Children should first subtract without an exchange before moving on to subtraction with exchange. When building the model, children should just make the minuend using Base 10, they then subtract the subtrahend. Highlight this difference to addition to avoid errors by making both numbers. Children start with the smallest place value column. When there are not enough</p> <p>ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.</p> <p>This model is efficient with up to 4-digit numbers. Place value counters are more efficient with larger numbers and decimals.</p>

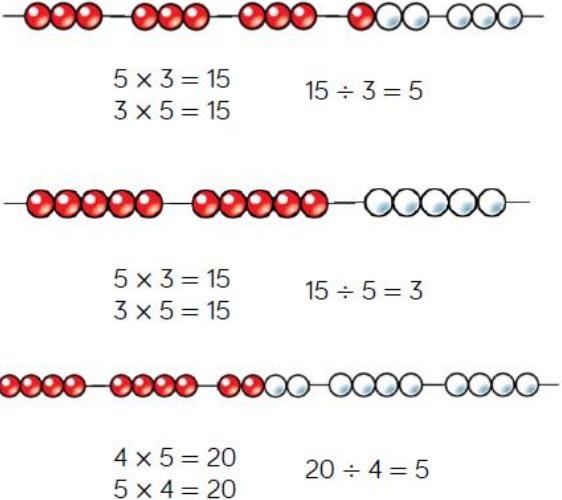
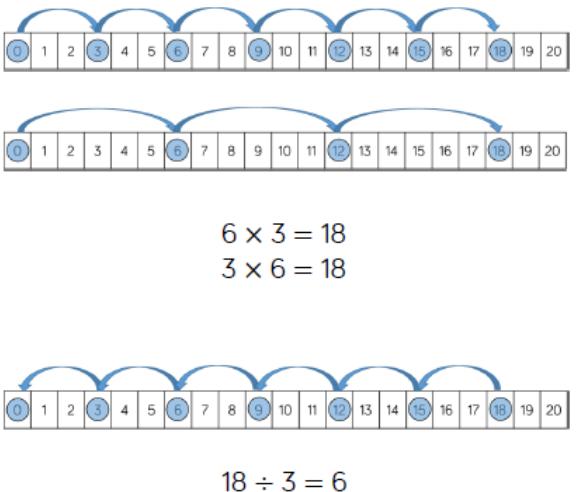
<p>Place Value Counters</p>	<p>KS2</p> 	$  \begin{array}{r}  384 \\  + 237 \\  \hline  621  \end{array}  $ <p>Using place value counters is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.</p> <p>Children should first add without an exchange before moving on to addition with exchange. Different place value counters can be used to represent larger numbers or decimals. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.</p> <p>When adding money, children can also use coins to support their understanding. It is important that children consider how the coins link to the written calculation especially when adding decimal amounts.</p>
<p>Place Value Counters Subtraction</p>	<p>KS2</p> 	$  \begin{array}{r}  652 \\  - 207 \\  \hline  445  \end{array}  $ <p>Using place value counters is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.</p> <p>Children should first subtract without an exchange before moving on to subtraction with exchange. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.</p> <p>When building the model, children should just make the minuend using counters, they then subtract the subtrahend. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.</p>

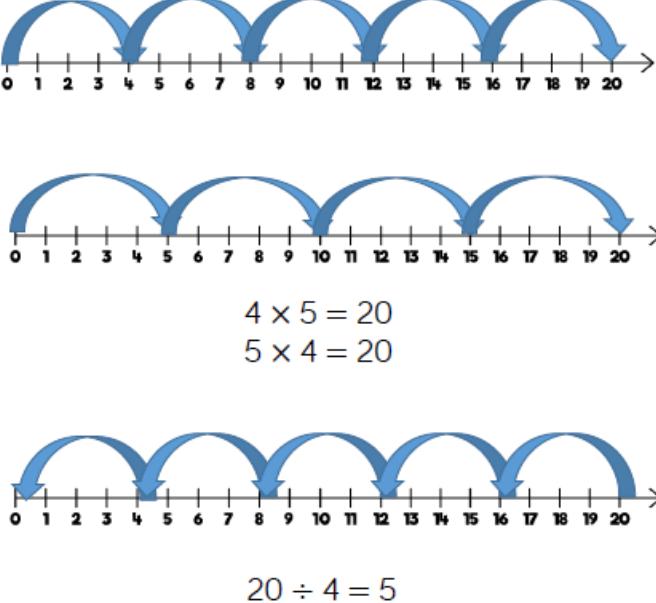
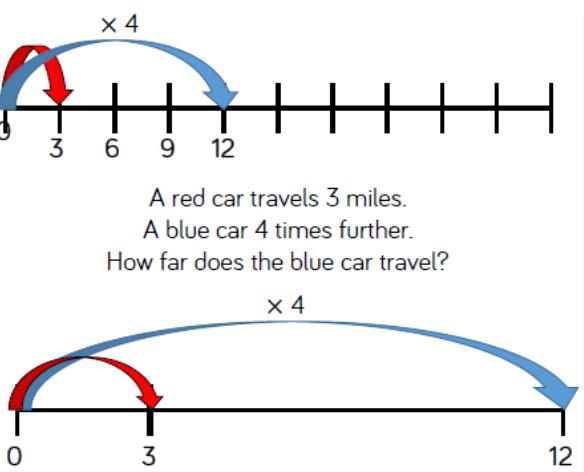
## Addition and Subtraction Glossary

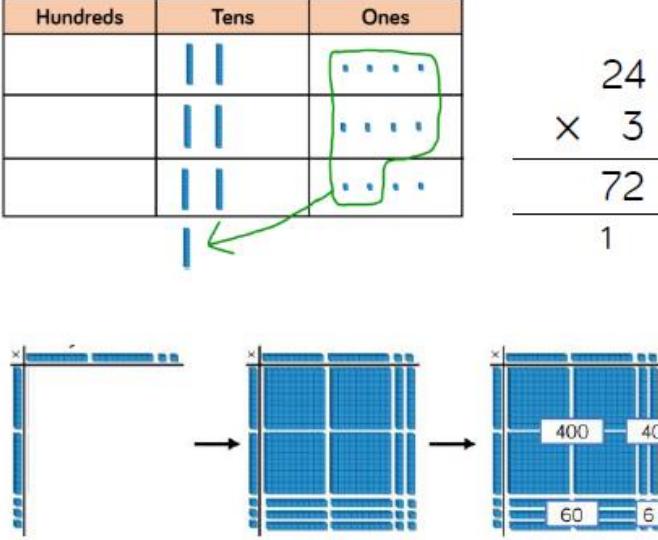
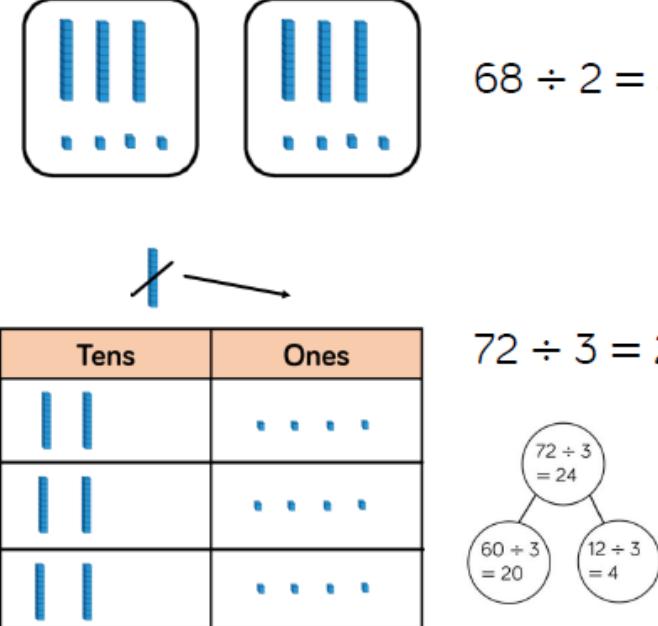
- **Addend** -A number to be added to another.
- **Aggregation** -combining two or more quantities or measures to find a total.
- **Augmentation** -increasing a quantity or measure by another quantity.
- **Commutative** –numbers can be added in any order.
- **Complement** –in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000
- **Difference** –the numerical difference between two numbers is found by comparing the quantity in each group.
- **Exchange** –Change a number or expression for another of an equal value.
- **Minuend** –A quantity or number from which another is subtracted.
- **Partitioning** –Splitting a number into its component parts.
- **Reduction** –Subtraction as take away.
- **Subitise** –Instantly recognise the number of objects in a small group without needing to count.
- **Subtrahend** -A number to be subtracted from another.
- **Sum** -The result of an addition.
- **Total** –The aggregate or the sum found by addition.

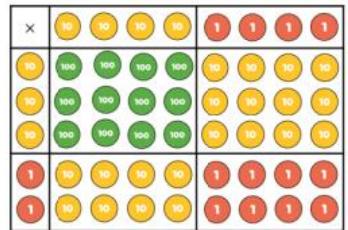
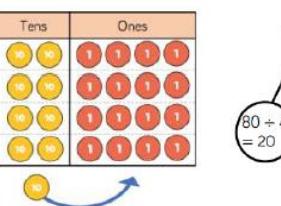
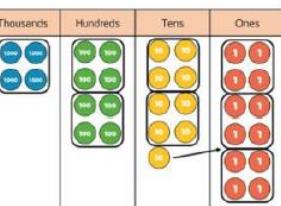
## Overview of Multiplication and Division Methods 1-6

Method	Year Group	Examples	Benefits
Bar model	All	 $5 \times 5 = 25$ $3 \times 7 = 21$ $7 \times 3 = 21$ $21 \div 7 = 3$	<p>Children can use the single bar model to represent multiplication as repeated addition. They could use counters, cubes or dots within the bar model to support calculation before moving on to placing digits into the bar model to represent the multiplication.</p> <p>Division can be represented by showing the total of the bar model and then dividing the bar model into equal groups. It is important when solving word problems that the bar model represents the problem.</p> <p>Sometimes, children may look at scaling problems. In this case, more than one bar model is useful to represent this type of problem, e.g. There are 3 girls in a group. There are 5 times more boys than girls. How many boys are there? The multiple bar model provides an opportunity to compare the groups.</p>
Number Shapes	KS1	 $5 \times 4 = 20$ $4 \times 5 = 20$ $5 \times 4 = 20$ $4 \times 5 = 20$ $18 \div 3 = 6$	<p>Number shapes support children's understanding of multiplication as repeated addition.</p> <p>Children can build multiplications in a row using the number shapes. When using odd numbers, encourage children to interlock the shapes so there are no gaps in the row. They can then use the tens number shapes along with other necessary shapes over the top of the row to check the total. Using the number shapes in multiplication can support children in discovering patterns of multiplication e.g. odd <math>\times</math> odd = even, odd <math>\times</math> even = odd, even <math>\times</math> even = even.</p> <p>When dividing, number shapes support children's understanding of division as grouping. Children make the number they are dividing and then place the number shape they are dividing by over the top of the number to find how</p>

			many groups of the number there are altogether e.g. There are 6 groups of 3 in 18.
Bead Strings	KS1		<p>Bead strings to 100 can support children in their understanding of multiplication as repeated addition. Children can build the multiplication using the beads. The colour of beads supports children in seeing how many groups of 10 they have, to calculate the total more efficiently.</p> <p>Encourage children to count in multiples as they build the number e.g. 4, 8, 12, 16, 20.</p> <p>Children can also use the bead string to count forwards and backwards in multiples, moving the beads as they count.</p> <p>When dividing, children build the number they are dividing and then group the beads into the number they are dividing by e.g. 20 divided by 4 – Make 20 and then group the beads into groups of four. Count how many groups you have made to find the answer.</p>
Number Tracks	KS1		<p>Number tracks are useful to support children to count in multiples, forwards and backwards. Moving counters or cubes along the number track can support children to keep track of their counting. Translucent counters help children to see the number they have landed on whilst counting.</p> <p>When multiplying, children place their counter on 0 to start and then count on to find the product of the numbers.</p> <p>When dividing, children place their counter on the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0.</p> <p>Children record how many jumps they have made to find the answer to the division.</p> <p>Number tracks can be useful with smaller multiples but when reaching larger numbers they can become less efficient.</p>

Number lines labelled	KS1 	<p>Labelled number lines are useful to support children to count in multiples, forwards and backwards as well as calculating single-digit multiplications.</p> <p>When multiplying, children start at 0 and then count on to find the product of the numbers.</p> <p>When dividing, start at the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0.</p> <p>Children record how many jumps they have made to find the answer to the division.</p> <p>Labelled number lines can be useful with smaller multiples, however they become inefficient as numbers become larger due to the required size of the number line.</p>
Number lines blank	KS1 	<p>Children can use blank number lines to represent scaling as multiplication or division.</p> <p>Blank number lines with intervals can support children to represent scaling accurately. Children can label intervals with multiples to calculate scaling problems.</p> <p>Blank number lines without intervals can also be used for children to represent scaling.</p>

Base 10 multiplication	KS2	 $  \begin{array}{r}  24 \\  \times 3 \\  \hline  72  \end{array}  $	<p>Using Base 10 or Dienes is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written representations match.</p> <p>As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed.</p> <p>Base 10 also supports the area model of multiplication well. Children use the equipment to build the number in a rectangular shape which they then find the area of by calculating the total value of the pieces. This area model can be linked to the grid method or the formal column method of multiplying 2-digits by 2-digits.</p>
Base 10 division	KS2	 $  68 \div 2 = 34  $ $  72 \div 3 = 24  $	<p>Using Base 10 or Dienes is an effective way to support children's understanding of division.</p> <p>When numbers become larger, it can be an effective way to move children from representing numbers as ones towards representing them as tens and ones in order to divide. Children can then share the Base 10/ Dienes between different groups e.g. by drawing circles or by rows on a place value grid.</p> <p>When they are sharing, children start with the larger place value and work from left to right. If there are any left in a column, they exchange e.g. one ten for ten ones.</p> <p>When recording, encourage children to use the part-whole model so they can consider how the number has been partitioned in order to divide. This will support them with mental methods.</p>

<p>Place Value Counters Multiplication</p>	<p>KS2</p>	 	$  \begin{array}{r}  34 \\  \times 5 \\  \hline  170 \\  12  \end{array}  $ $  \begin{array}{r}  44 \\  \times 32 \\  \hline  8 \\  80 \\  120 \\  + 1200 \\  \hline  1408  \end{array}  $	<p>Using place value counters is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written match.</p> <p>As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed. The counters should be used to support the understanding of the written method rather than support the arithmetic.</p> <p>Place value counters also support the area model of multiplication well. Children can see how to multiply 2-digit numbers by 2-digit numbers.</p>
<p>Place Value Counters Division</p>	<p>KS2</p>	 	$  \begin{array}{r}  1223 \\  4 \overline{)4892}  \end{array}  $	<p>Using place value counters is an effective way to support children's understanding of division.</p> <p>When working with smaller numbers, children can use place value counters to share between groups. They start by sharing the larger place value column and work from left to right. If there are any counters left over once they have been shared, they exchange the counter e.g. exchange one ten for ten ones. This method can be linked to the part-whole model to support children to show their thinking.</p> <p>Place value counters also support children's understanding of short division by grouping the counters rather than sharing them. Children work from left to right through the place value columns and group the counters in the number they are dividing by. If there are any counters left over after they have been grouped, they exchange the counter e.g. exchange one hundred for ten tens.</p>

# Multiplication and Division Glossary

**Array** –An ordered collection of counters, cubes or other item in rows and columns.

**Commutative** –Numbers can be multiplied in any order.

**Dividend** –In division, the number that is divided.

**Divisor** –In division, the number by which another is divided.

**Exchange** –Change a number or expression for another of an equal value.

**Factor** –A number that multiplies with another to make a product.

**Multiplicand** –In multiplication, a number to be multiplied by another.

**Partitioning** –Splitting a number into its component parts.

**Product** –The result of multiplying one number by another.

**Quotient** –The result of a division

**Remainder** –The amount left over after a division when the divisor is not a factor of the dividend.

**Scaling** –Enlarging or reducing a number by a given amount, called the scale factor

Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. They learn how to use an understanding of 10s and 1s to develop their calculation strategies, especially in addition and subtraction.

**Key language:** whole, part, ones, ten, tens, number bond, add, addition, plus, total, altogether, subtract, subtraction, find the difference, take away, minus, less, more, group, share, equal, equals, is equal to, groups, equal groups, times, multiply, multiplied by, divide, share, shared equally, times-table

**Addition and subtraction:** Children first learn to connect addition and subtraction with counting, but they soon develop two very important skills: an understanding of parts and wholes, and an understanding of unitising 10s, to develop efficient and effective calculation strategies based on known number bonds and an increasing awareness of place value. Addition and subtraction are taught in a way that is interlinked to highlight the link between the two operations.

A key idea is that children will select methods and approaches based on their number sense. For example, in Year 1, when faced with  $15 - 3$  and  $15 - 13$ , they will adapt their ways of approaching the calculation appropriately. The teaching should always emphasise the importance of mathematical thinking to ensure accuracy and flexibility of approach, and the importance of using known number facts to harness their recall of bonds within 20 to support both addition and subtraction methods.

In Year 2, they will start to see calculations presented in a column format, although this is not expected to be formalised until KS2. We show the column method in Year 2 as an option; teachers may not wish to include it until Year 3.

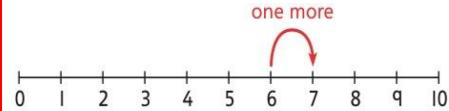
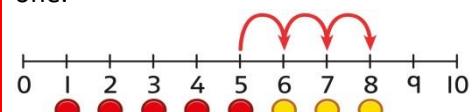
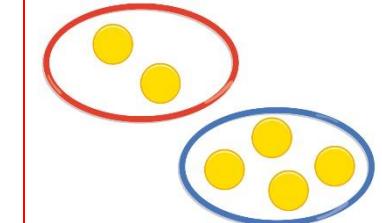
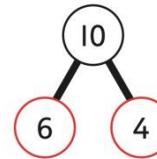
**Multiplication and division:** Children develop an awareness of equal groups and link this with counting in equal steps, starting with 2s, 5s and 10s. In Year 2, they learn to connect the language of equal groups with the mathematical symbols for multiplication and division.

They learn how multiplication and division can be related to repeated addition and repeated subtraction to find the answer to the calculation. In this key stage, it is vital that children explore and experience a variety of strong images and manipulative representations of equal groups, including concrete experiences as well as abstract calculations.

Children begin to recall some key multiplication facts, including doubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting.

**Fractions:** In Year 1, children encounter halves and quarters, and link this with their understanding of sharing. They experience key spatial representations of these fractions, and learn to recognise examples and non-examples, based on their awareness of equal parts of a whole. In Year 2, they develop an awareness of unit fractions and experience non-unit fractions, and they learn to write them and read them in the common format of numerator and denominator.

## Year 1

	Concrete	Pictorial	Abstract
Year 1 Addition	<p><b>Counting and adding more</b> Children add one more person or object to a group to find one more.</p>	<p><b>Counting and adding more</b> Children add one more cube or counter to a group to represent one more.</p>  <p><i>One more than 4 is 5.</i></p>	<p><b>Counting and adding more</b> Use a number line to understand how to link counting on with finding one more.</p>  <p><i>One more than 6 is 7. 7 is one more than 6.</i></p> <p>Learn to link counting on with adding more than one.</p>  <p><math>5 + 3 = 8</math></p>
	<p><b>Understanding part-part-whole relationship</b> Sort people and objects into parts and understand the relationship with the whole.</p>  <p><i>The parts are 2 and 4. The whole is 6.</i></p>	<p><b>Understanding part-part-whole relationship</b> Children draw to represent the parts and understand the relationship with the whole.</p>  <p><i>The parts are 1 and 5. The whole is 6.</i></p>	<p><b>Understanding part-part-whole relationship</b> Use a part-whole model to represent the numbers.</p>  $\boxed{6} + \boxed{4} = \boxed{10}$ $6 + 4 = 10$

### Knowing and finding number bonds within 10

Break apart a group and put back together to find and form number bonds.



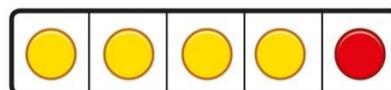
$$3 + 4 = 7$$



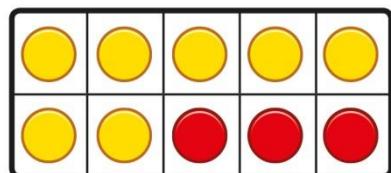
$$6 = 2 + 4$$

### Knowing and finding number bonds within 10

Use five and ten frames to represent key number bonds.



$$5 = 4 + 1$$

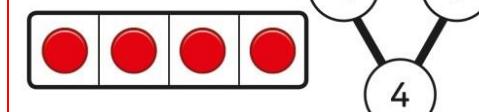


$$10 = 7 + 3$$

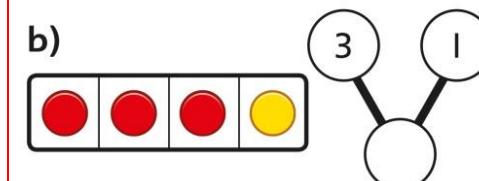
### Knowing and finding number bonds within 10

Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero.

a)



b)

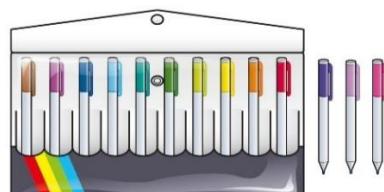


$$4 + 0 = 4$$

$$3 + 1 = 4$$

### Understanding teen numbers as a complete 10 and some more

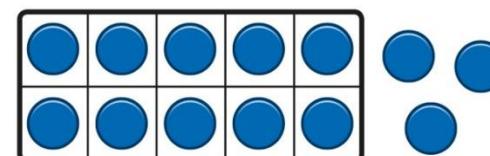
Complete a group of 10 objects and count more.



13 is 10 and 3 more.

### Understanding teen numbers as a complete 10 and some more

Use a ten frame to support understanding of a complete 10 for teen numbers.



13 is 10 and 3 more.

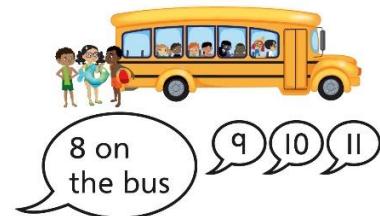
### Understanding teen numbers as a complete 10 and some more.

1 ten and 3 ones equal 13.

$$10 + 3 = 13$$

**Adding by counting on**

Children use knowledge of counting to 20 to find a total by counting on using people or objects.

**Adding the 1s**

Children use bead strings to recognise how to add the 1s to find the total efficiently.



$$2 + 3 = 5$$

$$12 + 3 = 15$$

**Bridging the 10 using number bonds**

Children use a bead string to complete a 10 and understand how this relates to the addition.

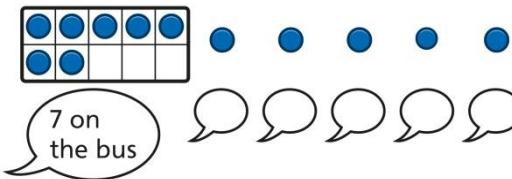


7 add 3 makes 10.

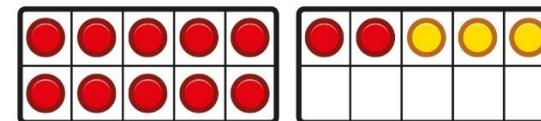
So, 7 add 5 is 10 and 2 more.

**Adding by counting on**

Children use counters to support and represent their counting on strategy.

**Adding the 1s**

Children represent calculations using ten frames to add a teen and 1s.

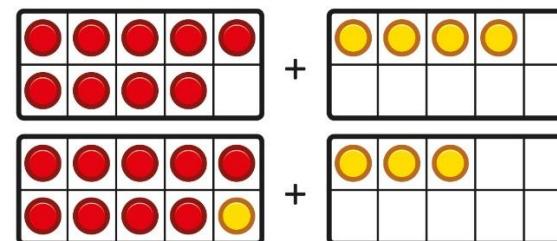


$$2 + 3 = 5$$

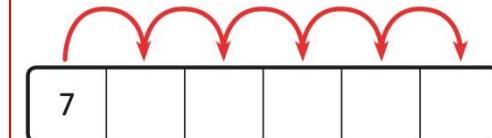
$$12 + 3 = 15$$

**Bridging the 10 using number bonds**

Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.

**Adding by counting on**

Children use number lines or number tracks to support their counting on strategy.



$$7 + 5 = \square$$

**Adding the 1s**

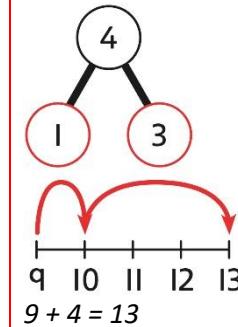
Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently.

$$3 + 5 = 8$$

$$\text{So, } 13 + 5 = 18$$

**Bridging the 10 using number bonds**

Use a part-whole model and a number line to support the calculation.



$$9 + 4 = 13$$

**Year 1  
Subtraction**

**Counting back and taking away**

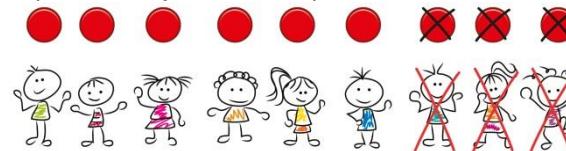
Children arrange objects and remove to find how many are left.



1 less than 6 is 5.  
6 subtract 1 is 5.

**Counting back and taking away**

Children draw and cross out or use counters to represent objects from a problem.

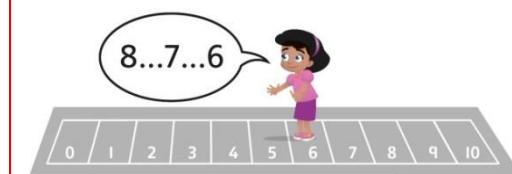


$$9 - \boxed{\quad} = \boxed{\quad}$$

There are  children left.

**Counting back and taking away**

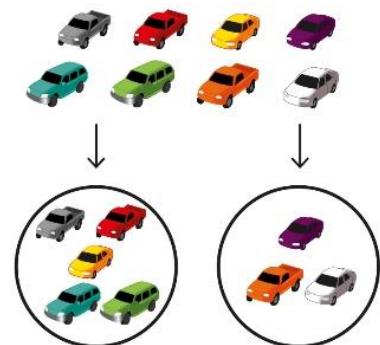
Children count back to take away and use a number line or number track to support the method.



$$9 - 3 = 6$$

**Finding a missing part, given a whole and a part**

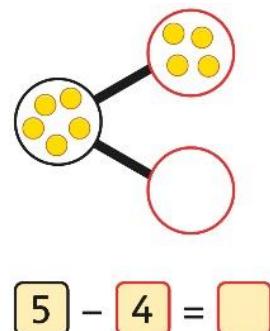
Children separate a whole into parts and understand how one part can be found by subtraction.



$$8 - 5 = ?$$

**Finding a missing part, given a whole and a part**

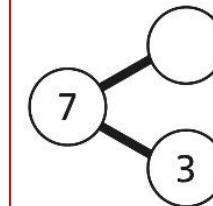
Children represent a whole and a part and understand how to find the missing part by subtraction.



$$5 - \boxed{4} = \boxed{\quad}$$

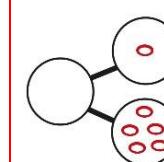
**Finding a missing part, given a whole and a part**

Children use a part-whole model to support the subtraction to find a missing part.



$$7 - 3 = ?$$

Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model.



$$\begin{array}{l} \boxed{\quad} - \boxed{\quad} = \boxed{\quad} \\ \boxed{\quad} - \boxed{\quad} = \boxed{\quad} \\ \boxed{\quad} + \boxed{\quad} = \boxed{\quad} \\ \boxed{\quad} + \boxed{\quad} = \boxed{\quad} \end{array}$$

### Finding the difference

Arrange two groups so that the difference between the groups can be worked out.



8 is 2 more than 6.

6 is 2 less than 8.

The difference between 8 and 6 is 2.

### Subtraction within 20

Understand when and how to subtract 1s efficiently.

Use a bead string to subtract 1s efficiently.

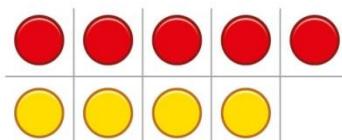


$$5 - 3 = 2$$

$$15 - 3 = 12$$

### Finding the difference

Represent objects using sketches or counters to support finding the difference.



$$5 - 4 = 1$$

The difference between 5 and 4 is 1.

### Finding the difference

Children understand 'find the difference' as subtraction.



$$10 - 6 = 4$$

The difference between 10 and 6 is 4.

### Subtracting 10s and 1s

For example:  $18 - 12$

Subtract 12 by first subtracting the 10, then the remaining 2.



First subtract the 10, then take away 2.

### Subtracting 10s and 1s

For example:  $18 - 12$

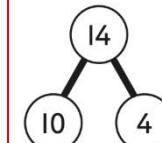
Use ten frames to represent the efficient method of subtracting 12.



First subtract the 10, then subtract 2.

### Subtracting 10s and 1s

Use a part-whole model to support the calculation.

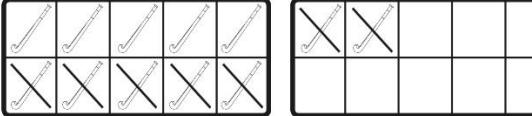
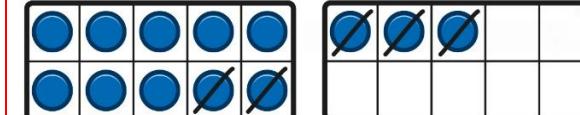
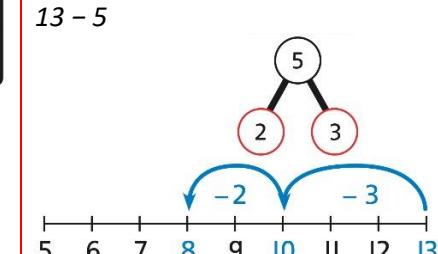
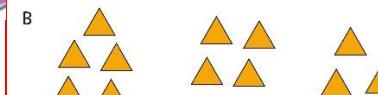
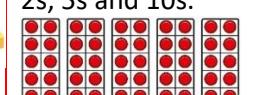


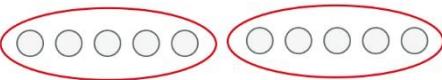
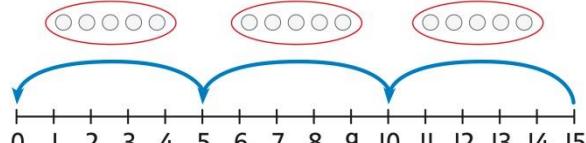
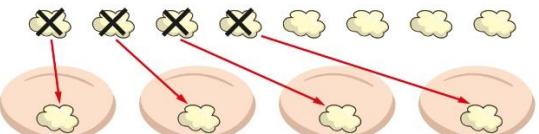
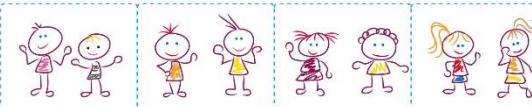
$$19 - 14$$

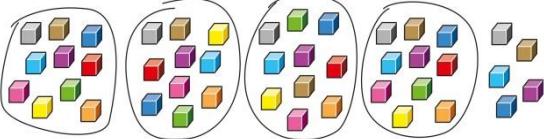
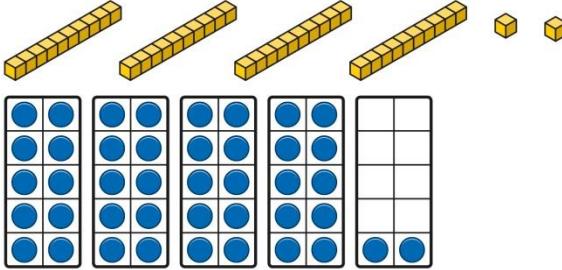
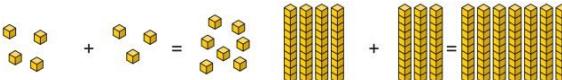
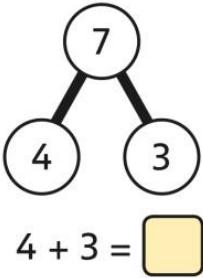
$$19 - 10 = 9$$

$$9 - 4 = 5$$

$$\text{So, } 19 - 14 = 5$$

	<p><b>Subtraction bridging 10 using number bonds</b> For example: <math>12 - 7</math></p> <p>Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.</p>  <p>7 is 2 and 5, so I take away the 2 and then the 5.</p>	<p><b>Subtraction bridging 10 using number bonds</b> Represent the use of bonds using ten frames.</p>  <p>For <math>13 - 5</math>, I take away 3 to make 10, then take away 2 to make 8.</p>	<p><b>Subtraction bridging 10 using number bonds</b> Use a number line and a part-whole model to support the method.</p> <p><math>13 - 5</math></p> 																																																						
<p><b>Year 1</b> <b>Multiplication</b></p>	<p><b>Recognising and making equal groups</b> Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal.</p> <p>A                    B                    C</p> 	<p><b>Recognising and making equal groups</b> Children draw and represent equal and unequal groups.</p> <p>A</p>  <p>B</p> 	<p><b>Describe equal groups using words</b></p> <p>Three equal groups of 4. Four equal groups of 3.</p>																																																						
	<p><b>Finding the total of equal groups by counting in 2s, 5s and 10s</b></p>  <p>There are 5 pens in each pack ... 5...10...15...20...25...30...35...40...</p>	<p><b>Finding the total of equal groups by counting in 2s, 5s and 10s</b> 100 squares and ten frames support counting in 2s, 5s and 10s.</p>  <table border="1" data-bbox="882 1200 1147 1335"> <tr><td>I</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>II</td><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>2I</td><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>3I</td><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>4I</td><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> </table>	I	1	2	3	4	5	6	7	8	9	10	II	11	12	13	14	15	16	17	18	19	20	2I	21	22	23	24	25	26	27	28	29	30	3I	31	32	33	34	35	36	37	38	39	40	4I	41	42	43	44	45	46	47	48	49	50
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3I	31	32	33	34	35	36	37	38	39	40																																															
4I	41	42	43	44	45	46	47	48	49	50																																															

<p><b>Year 1</b> <b>Division</b></p>	<p><b>Grouping</b> Learn to make equal groups from a whole and find how many equal groups of a certain size can be made.</p> <p>Sort a whole set people and objects into equal groups.</p>  <p><i>There are 10 children altogether. There are 2 in each group. There are 5 groups.</i></p>	<p><b>Grouping</b> Represent a whole and work out how many equal groups.</p>  <p><i>There are 10 in total. There are 5 in each group. There are 2 groups.</i></p>	<p><b>Grouping</b> Children may relate this to counting back in steps of 2, 5 or 10.</p> 
	<p><b>Sharing</b> Share a set of objects into equal parts and work out how many are in each part.</p> 	<p><b>Sharing</b> Sketch or draw to represent sharing into equal parts. This may be related to fractions.</p> 	<p><b>Sharing</b> <i>10 shared into 2 equal groups gives 5 in each group.</i></p>

	Concrete	Pictorial	Abstract								
Year 2 Addition											
Understanding 10s and 1s	<p>Group objects into 10s and 1s.</p>  <p>Bundle straws to understand unitising of 10s.</p> 	<p>Understand 10s and 1s equipment, and link with visual representations on ten frames.</p> 	<p>Represent numbers on a place value grid, using equipment or numerals.</p> <table border="1" data-bbox="1560 293 1852 611"> <tr> <td>Tens</td> <td>Ones</td> </tr> <tr> <td>3</td> <td>2</td> </tr> <tr> <td>Tens</td> <td>Ones</td> </tr> <tr> <td>4</td> <td>3</td> </tr> </table>	Tens	Ones	3	2	Tens	Ones	4	3
Tens	Ones										
3	2										
Tens	Ones										
4	3										
Adding 10s	<p>Use known bonds and unitising to add 10s.</p>  <p><i>I know that <math>4 + 3 = 7</math>. So, I know that 4 tens add 3 tens is 7 tens.</i></p>	<p>Use known bonds and unitising to add 10s.</p>  <p><i>I know that <math>4 + 3 = 7</math>. So, I know that 4 tens add 3 tens is 7 tens.</i></p>	<p>Use known bonds and unitising to add 10s.</p>  <p><math>4 + 3 = 7</math>  <math>4 \text{ tens} + 3 \text{ tens} = 7 \text{ tens}</math>  <math>40 + 30 = 70</math></p>								

**Adding a 1-digit number to a 2-digit number not bridging a 10**

Add the 1s to find the total. Use known bonds within 10.



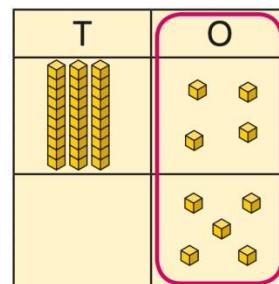
41 is 4 tens and 1 one.  
41 add 6 ones is 4 tens and 7 ones.

This can also be done in a place value grid.

Add the 1s.

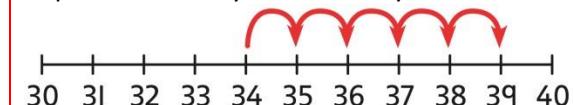


34 is 3 tens and 4 ones.  
4 ones and 5 ones are 9 ones.  
The total is 3 tens and 9 ones.



Add the 1s.

Understand the link between counting on and using known number facts. Children should be encouraged to use known number bonds to improve efficiency and accuracy.



This can be represented horizontally or vertically.

$$34 + 5 = 39$$

or

$$\begin{array}{r}
 \begin{array}{c|c}
 \text{T} & \text{O} \\
 \hline
 3 & 4 \\
 + & 5 \\
 \hline
 & 9
 \end{array}
 \end{array}$$

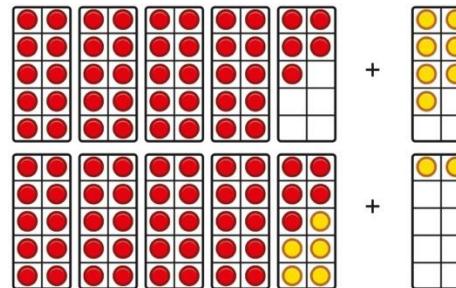
**Adding a 1-digit number to a 2-digit number bridging 10**

Complete a 10 using number bonds.

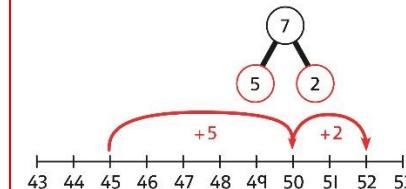


There are 4 tens and 5 ones.  
I need to add 7. I will use 5 to complete a 10, then add 2 more.

Complete a 10 using number bonds.



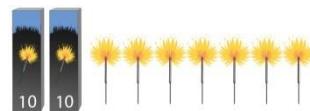
Complete a 10 using number bonds.



$$\begin{aligned}
 7 &= 5 + 2 \\
 45 + 5 + 2 &= 52
 \end{aligned}$$

### Adding a multiple of 10 to a 2-digit number

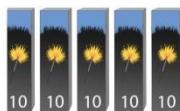
Add the 10s and then recombine.



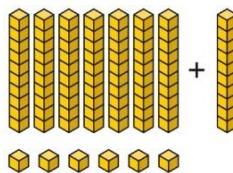
27 is 2 tens and 7 ones.

50 is 5 tens.

There are 7 tens in total and 7 ones.  
So, 27 + 50 is 7 tens and 7 ones.



Add the 10s and then recombine.



66 is 6 tens and 6 ones.

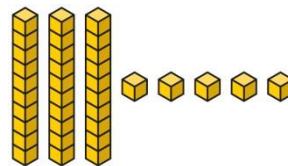
$$66 + 10 = 76$$

A 100 square can support this understanding.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

### Adding two 2-digit numbers

Add the 10s and 1s separately.



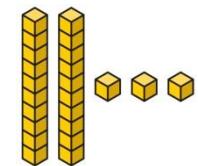
$$5 + 3 = 8$$

There are 8 ones in total.

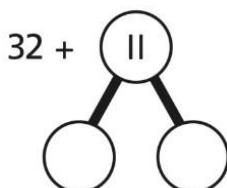
$$3 + 2 = 5$$

There are 5 tens in total.

$$35 + 23 = 58$$



Add the 10s and 1s separately. Use a part-whole model to support.



$$11 = 10 + 1$$

$$32 + 10 = 42$$

$$42 + 1 = 43$$

$$32 + 11 = 43$$

Add the 10s and then recombine.

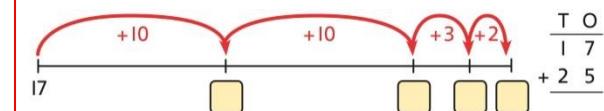
$$37 + 20 = ?$$

$$30 + 20 = 50$$

$$50 + 7 = 57$$

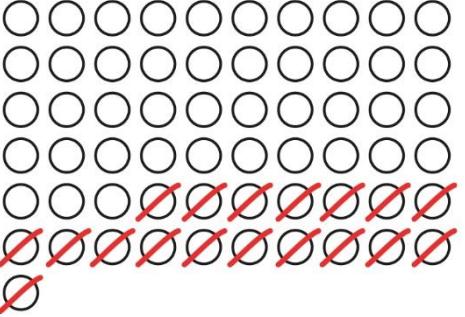
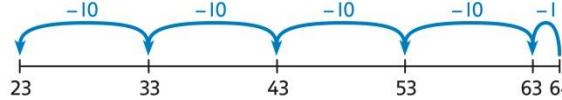
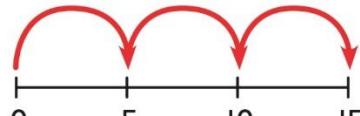
$$37 + 20 = 57$$

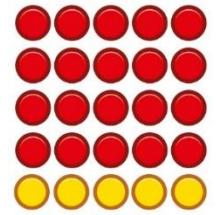
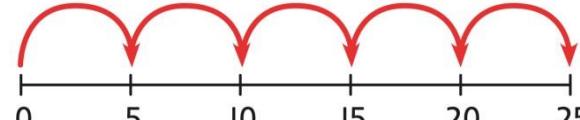
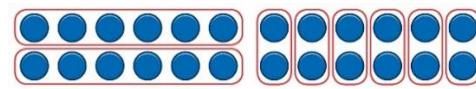
Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations.



$$17 + 25$$



<h3>Subtracting a 2-digit number</h3>	<p>Subtract by taking away.</p>  <p><math>61 - 18</math> I took away 1 ten and 8 ones.</p>	<p>Subtract the 10s and the 1s.</p> <p>This can be represented on a 100 square.</p> <table border="1" data-bbox="956 271 1327 636"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> <tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr> <tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr> <tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr> <tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr> <tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	<p>Subtract the 10s and the 1s.</p> <p>This can be represented on a number line.</p>  <p><math>64 - 41 = ?</math></p> <p><math>64 - 1 = 63</math>  <math>63 - 40 = 23</math>  <math>64 - 41 = 23</math></p>  <p><math>46 - 20 = 26</math>  <math>26 - 5 = 21</math>  <math>46 - 25 = 21</math></p>
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<h3>Year 2 Multiplication</h3>																																																																																																							
<h3>Equal groups and repeated addition</h3>	<p>Recognise equal groups and write as repeated addition and as multiplication.</p>  <p><math>3</math> groups of <math>5</math> chairs  <math>15</math> chairs altogether</p>	<p>Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication.</p>  <p><math>3</math> groups of <math>5</math>  <math>15</math> in total</p>	<p>Use a number line and write as repeated addition and as multiplication.</p>  <p><math>5 + 5 + 5 = 15</math>  <math>3 \times 5 = 15</math></p>																																																																																																				

<b>Using arrays to represent multiplication and support understanding</b>	<p>Understand the relationship between arrays, multiplication and repeated addition.</p>  <p><i>4 groups of 5</i></p>	<p>Understand the relationship between arrays, multiplication and repeated addition.</p>  <p><i>4 groups of 5 ... 5 groups of 5</i></p>	<p>Understand the relationship between arrays, multiplication and repeated addition.</p>  <p><math>5 \times 5 = 25</math></p>
<b>Understanding commutativity</b>	<p>Use arrays to visualise commutativity.</p>  <p><i>I can see 6 groups of 3. I can see 3 groups of 6.</i></p>	<p>Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.</p>  <p><i>This is 2 groups of 6 and also 6 groups of 2.</i></p>	<p>Use arrays to visualise commutativity.</p>  <p><math>4 + 4 + 4 + 4 + 4 = 20</math>  <math>5 + 5 + 5 + 5 = 20</math>  <math>4 \times 5 = 20</math> and <math>5 \times 4 = 20</math></p>

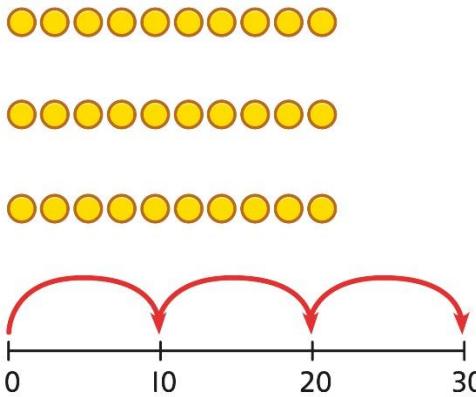
**Learning  $\times 2$ ,  $\times 5$  and  $\times 10$  table facts**

Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.



3 groups of 10 ... 10, 20, 30  
 $3 \times 10 = 30$

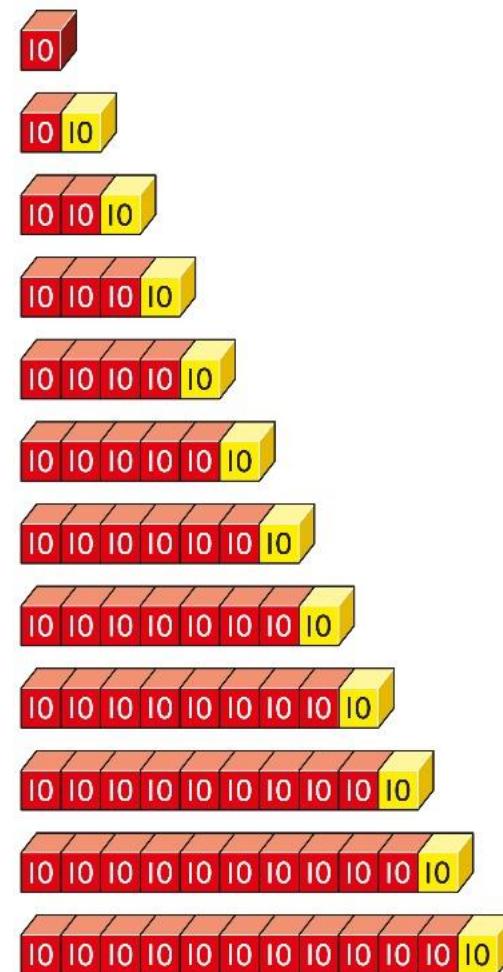
Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.



$$10 + 10 + 10 = 30$$

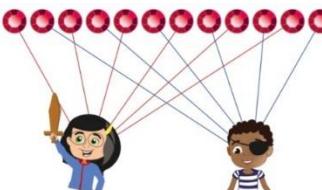
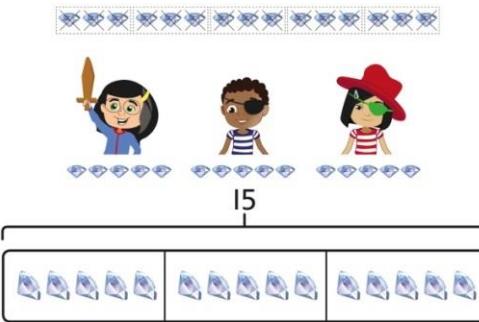
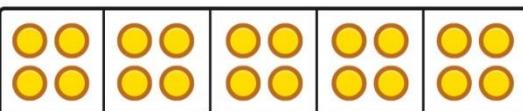
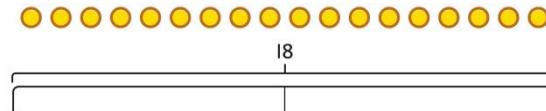
$$3 \times 10 = 30$$

Understand how the times-tables increase and contain patterns.



$$5 \times 10 = 50$$

$$6 \times 10 = 60$$

Year 2 Division			
<b>Sharing equally</b> <p>Start with a whole and share into equal parts, one at a time.</p>  <p><i>12 shared equally between 2. They get 6 each.</i></p> <p>Start to understand how this also relates to grouping. To share equally between 3 people, take a group of 3 and give 1 to each person. Keep going until all the objects have been shared</p>  <p><i>15 shared equally between 3. They get 5 each.</i></p>	<p>Represent the objects shared into equal parts using a bar model.</p>  <p><i>20 shared into 5 equal parts. There are 4 in each part.</i></p>	<p>Use a bar model to support understanding of the division.</p>  <p><math>18 \div 2 = 9</math></p>	

<b>Grouping equally</b>	<p>Understand how to make equal groups from a whole.</p> <p><i>8 divided into 4 equal groups. There are 2 in each group.</i></p>	<p>Understand the relationship between grouping and the division statements.</p> <p><math>12 \div 3 = 4</math></p> <p><math>12 \div 4 = 3</math></p> <p><math>12 \div 6 = 2</math></p> <p><math>12 \div 2 = 6</math></p>	<p>Understand how to relate division by grouping to repeated subtraction.</p> <p><i>There are 4 groups now.</i></p> <p><math>12 \div 3 = 4</math></p> <p><i>There are 4 groups.</i></p>
<b>Using known times-tables to solve divisions</b>	<p>Understand the relationship between multiplication facts and division.</p> <p><i>4 groups of 5 cars is 20 cars in total. 20 divided by 4 is 5.</i></p>	<p>Link equal grouping with repeated subtraction and known times-table facts to support division.</p> <p><i>40 divided by 4 is 10.</i></p> <p>Use a bar model to support understanding of the link between times-table knowledge and division.</p>	<p>Relate times-table knowledge directly to division.</p> <p><math>1 \times 10 = 10</math>  <math>2 \times 10 = 20</math>  <b><math>3 \times 10 = 30</math></b>  <math>4 \times 10 = 40</math>  <math>5 \times 10 = 50</math>  <math>6 \times 10 = 60</math>  <math>7 \times 10 = 70</math>  <math>8 \times 10 = 80</math></p> <p><i>I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.</i></p> <p><math>3 \times 10 = 30 \text{ so } 30 \div 10 = 3</math></p>

## KEY STAGE 2

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

**Key language:** partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

**Addition and subtraction:** In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns.

By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2.

**Multiplication and division:** Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively.

Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single digit.

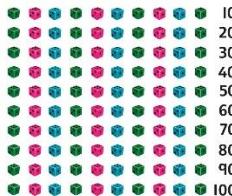
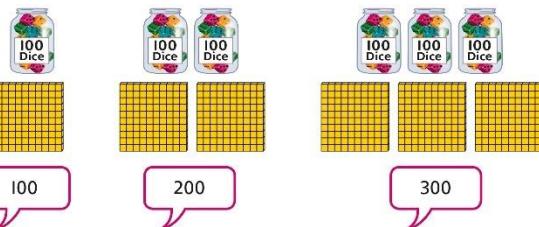
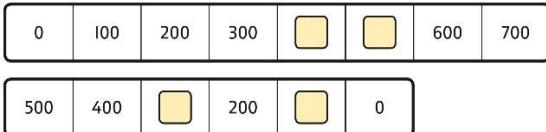
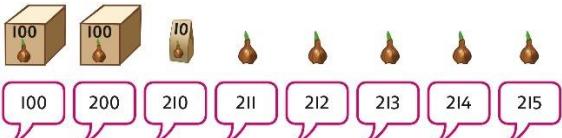
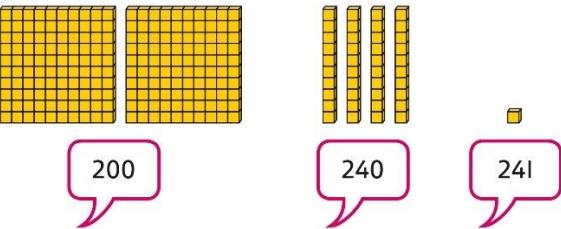
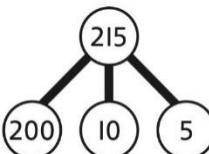
Children develop column methods to support multiplications in these cases.

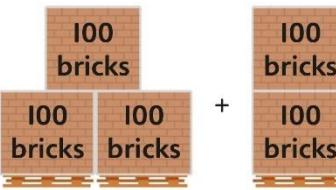
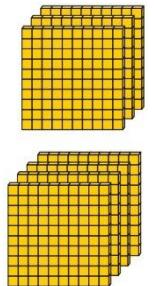
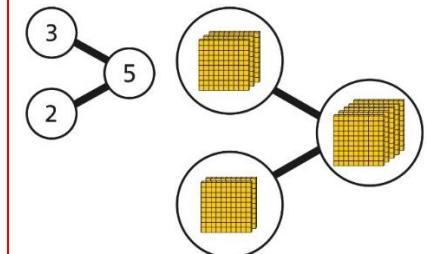
For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts. Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem.

**Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.

In Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.

	Concrete	Pictorial	Abstract
<b>Year 3 Addition</b>			
<b>Understanding 100s</b>	<p>Understand the cardinality of 100, and the link with 10 tens.</p> <p>Use cubes to place into groups of 10 tens.</p> 	<p>Unitise 100 and count in steps of 100.</p> 	<p>Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.</p> 
<b>Understanding place value to 1,000</b>	<p>Unitise 100s, 10s and 1s to build 3-digit numbers.</p> 	<p>Use equipment to represent numbers to 1,000.</p>  <p>Use a place value grid to support the structure of numbers to 1,000.</p> <p>Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount.</p>	<p>Represent the parts of numbers to 1,000 using a part-whole model.</p>  $215 = 200 + 10 + 5$ <p>Recognise numbers to 1,000 represented on a number line, including those between intervals.</p>

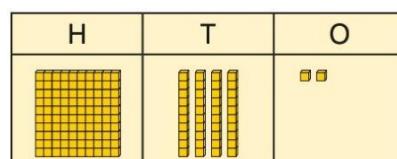
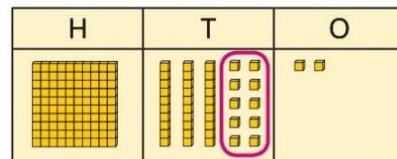
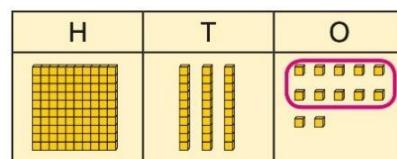
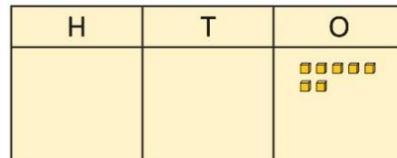
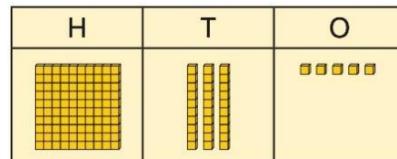
<b>Adding 100s</b>	<p>Use known facts and unitising to add multiples of 100.</p>  $3 + 2 = 5$ $3 \text{ hundreds} + 2 \text{ hundreds} = 5 \text{ hundreds}$ $300 + 200 = 500$	<p>Use known facts and unitising to add multiples of 100.</p>  $3 + 4 = 7$ $3 \text{ hundreds} + 4 \text{ hundreds} = 7 \text{ hundreds}$ $300 + 400 = 700$	<p>Use known facts and unitising to add multiples of 100.</p> <p>Represent the addition on a number line.</p> <p>Use a part-whole model to support unitising.</p>  $3 + 2 = 5$ $300 + 200 = 500$									
<b>3-digit number + 1s, no exchange or bridging</b>	<p>Use number bonds to add the 1s.</p>  $214 + 4 = ?$ <p>Now there are 4 + 4 ones in total.</p> $4 + 4 = 8$ $214 + 4 = 218$	<p>Use number bonds to add the 1s.</p> <table border="1" data-bbox="954 825 1268 1071"> <thead> <tr> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td>2</td> <td>4</td> <td>9</td> </tr> </tbody> </table> <p>Use number bonds to add the 1s.  <math>5 + 4 = 9</math></p> $245 + 4$ $5 + 4 = 9$ $245 + 4 = 249$	H	T	O				2	4	9	<p>Understand the link with counting on.</p> <p><math>245 + 4</math></p>  <p>Use number bonds to add the 1s and understand that this is more efficient and less prone to error.</p> <p><math>245 + 4 = ?</math></p> <p>I will add the 1s.  <math>5 + 4 = 9</math>  <math>So, 245 + 4 = 249</math></p>
H	T	O										
2	4	9										

**3-digit number + 1s with exchange**

Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.

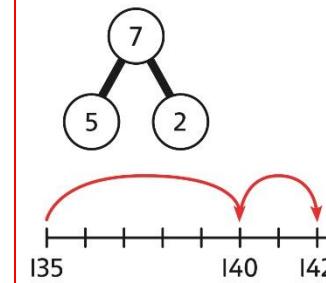
Children should explore this using unitised objects or physical apparatus.

Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.



$$135 + 7 = 142$$

Understand how to bridge by partitioning to the 1s to make the next 10.



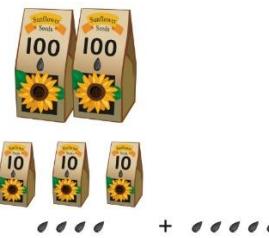
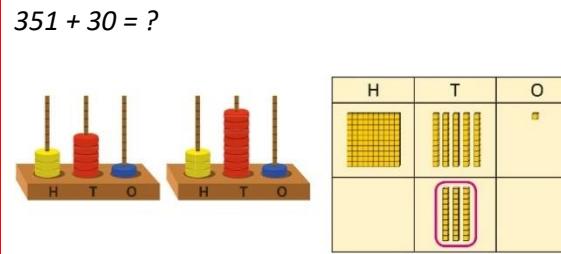
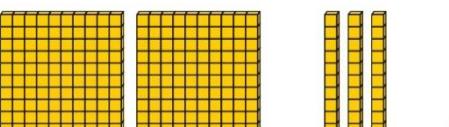
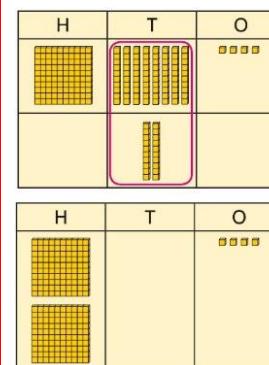
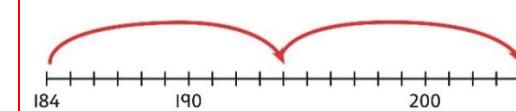
$$135 + 7 = ?$$

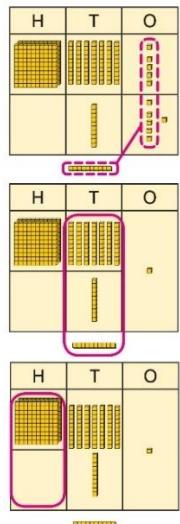
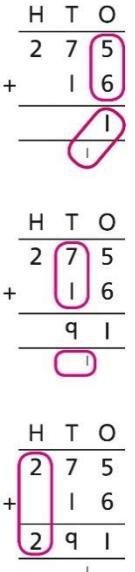
$$135 + 5 + 2 = 142$$

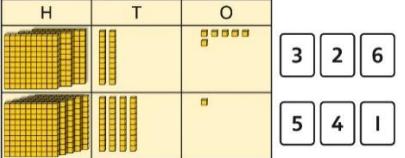
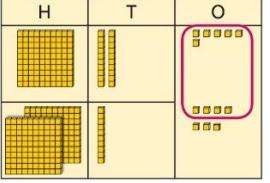
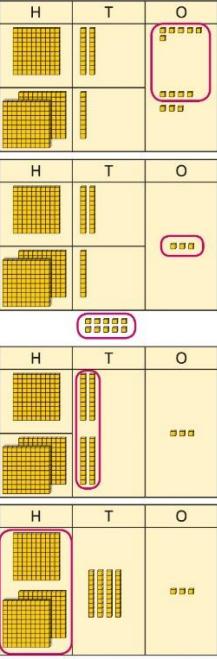
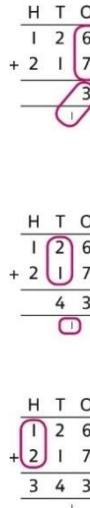
Ensure that children understand how to add 1s bridging a 100.

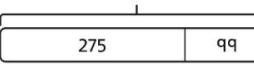
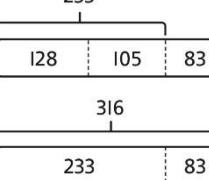
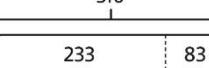
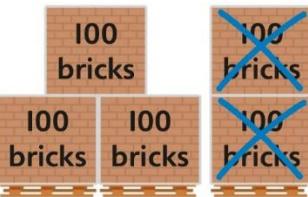
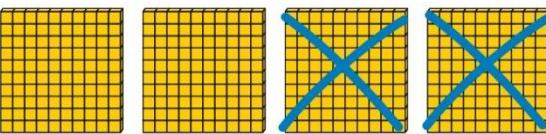
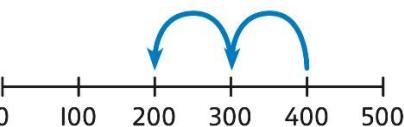
$$198 + 5 = ?$$

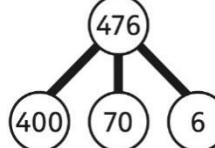
$$198 + 2 + 3 = 203$$

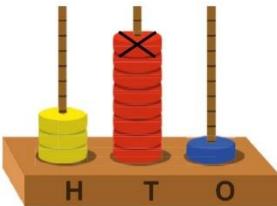
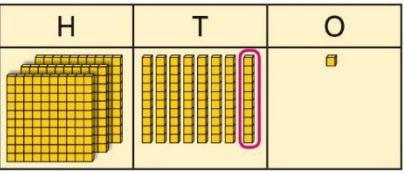
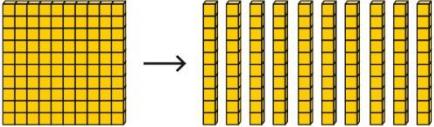
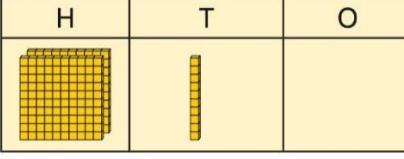
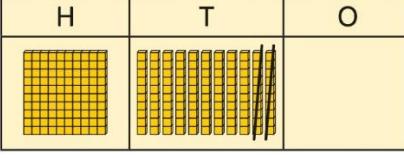
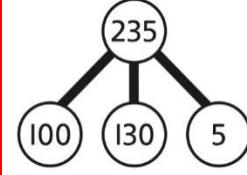
<b>3-digit number + 10s, no exchange</b>	<p>Calculate mentally by forming the number bond for the 10s.</p>  <p><math>234 + 50</math> There are 3 tens and 5 tens altogether. <math>3 + 5 = 8</math> In total there are 8 tens. <math>234 + 50 = 284</math></p>	<p>Calculate mentally by forming the number bond for the 10s.</p> <p><math>351 + 30 = ?</math></p>  <p><math>5 \text{ tens} + 3 \text{ tens} = 8 \text{ tens}</math> <math>351 + 30 = 381</math></p>	<p>Calculate mentally by forming the number bond for the 10s.</p> <p><math>753 + 40</math> <i>I know that <math>5 + 4 = 9</math></i> <i>So, <math>50 + 40 = 90</math></i> <math>753 + 40 = 793</math></p>
<b>3-digit number + 10s, with exchange</b>	<p>Understand the exchange of 10 tens for 1 hundred.</p> 	<p>Add by exchanging 10 tens for 1 hundred.</p> <p><math>184 + 20 = ?</math></p>  <p><math>184 + 20 = 204</math></p>	<p>Understand how the addition relates to counting on in 10s across 100.</p>  <p><math>184 + 20 = ?</math> <i>I can count in 10s ... 194 ... 204</i> <math>184 + 20 = 204</math></p> <p>Use number bonds within 20 to support efficient mental calculations.</p> <p><math>385 + 50</math> There are 8 tens and 5 tens. That is 13 tens. <math>385 + 50 = 300 + 130 + 5</math> <math>385 + 50 = 435</math></p>

<b>3-digit number + 2-digit number</b>	<p>Use place value equipment to make and combine groups to model addition.</p> 	<p>Use a place value grid to organise thinking and adding of 1s, then 10s.</p>	<p>Use the vertical column method to represent the addition. Children must understand how this relates to place value at each stage of the calculation.</p>
<b>3-digit number + 2-digit number, exchange required</b>	<p>Use place value equipment to model addition and understand where exchange is required.</p> <p><i>Use place value counters to represent 154 + 72.</i></p> <p><i>Use this to decide if any exchange is required.</i></p> <p><i>There are 5 tens and 7 tens. That is 12 tens so I will exchange.</i></p>	<p>Represent the required exchange on a place value grid using equipment.</p> <p><math>275 + 16 = ?</math></p>  <p><math>275 + 16 = 291</math></p> <p>Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value. Children should be encouraged at every stage to select methods that are accurate and efficient.</p>	<p>Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation.</p>  <p><math>275 + 16 = 291</math></p>

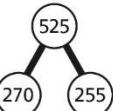
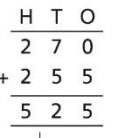
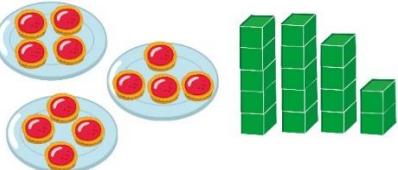
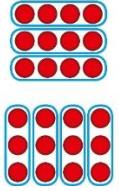
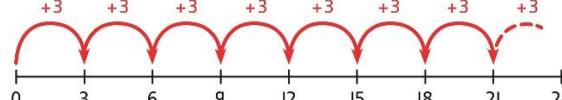
<b>3-digit number + 3-digit number, no exchange</b>	<p>Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid.</p> <p><i>326 + 541 is represented as:</i></p> 	<p>Represent the place value grid with equipment to model the stages of column addition.</p>	<p>Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.</p>
<b>3-digit number + 3-digit number, exchange required</b>	<p>Use place value equipment to enact the exchange required.</p>  <p><i>There are 13 ones. I will exchange 10 ones for 1 ten.</i></p>	<p>Model the stages of column addition using place value equipment on a place value grid.</p> 	<p>Use column addition, ensuring understanding of place value at every stage of the calculation.</p>  <p><i>126 + 217 = 343</i></p> <p>Note: Children should also study examples where exchange is required in more than one column, for example <math>185 + 318 = ?</math></p>

<b>Representing addition problems, and selecting appropriate methods</b>	<p>Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps.</p> <p>These representations will help them to select appropriate methods.</p>	<p>Children understand and create bar models to represent addition problems.</p> $275 + 99 = ?$  $275 + 99 = 374$	<p>Use representations to support choices of appropriate methods.</p>  <p><i>I will add 100, then subtract 1 to find the solution.</i></p> $128 + 105 + 83 = ?$ <p><i>I need to add three numbers.</i></p> $128 + 105 = 233$  $316$ 
<b>Year 3 Subtraction</b>			
<b>Subtracting 100s</b>	<p>Use known facts and unitising to subtract multiples of 100.</p>  $5 - 2 = 3$ $500 - 200 = 300$	<p>Use known facts and unitising to subtract multiples of 100.</p>  $4 - 2 = 2$ $400 - 200 = 200$	<p>Understand the link with counting back in 100s.</p>  $400 - 200 = 200$ <p>Use known facts and unitising as efficient and accurate methods.</p> <p><i>I know that 7 - 4 = 3. Therefore, I know that 700 - 400 = 300.</i></p>

<b>3-digit number – 1s, no exchange</b>	<p>Use number bonds to subtract the 1s.</p>  <p><math>214 - 3 = ?</math></p>  <p><math>4 - 3 = 1</math>  <math>214 - 3 = 211</math></p>	<p>Use number bonds to subtract the 1s.</p> <table border="1" data-bbox="961 203 1275 382"> <tr> <td>H</td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td>3</td> <td>1</td> <td>4</td> </tr> </table> <p><math>319 - 4 = ?</math></p> <table border="1" data-bbox="961 493 1275 673"> <tr> <td>H</td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td>3</td> <td>1</td> <td>4</td> </tr> </table> <p><math>9 - 4 = 5</math>  <math>319 - 4 = 315</math></p>	H	T	O				3	1	4	H	T	O				3	1	4	<p>Understand the link with counting back using a number line.</p> <p>Use known number bonds to calculate mentally.</p> <p><math>476 - 4 = ?</math></p>  <p><math>6 - 4 = 2</math>  <math>476 - 4 = 472</math></p>
H	T	O																			
3	1	4																			
H	T	O																			
3	1	4																			
<b>3-digit number – 1s, exchange or bridging required</b>	<p>Understand why an exchange is necessary by exploring why 1 ten must be exchanged.</p> <p>Use place value equipment.</p>	<p>Represent the required exchange on a place value grid.</p> <p><math>151 - 6 = ?</math></p> <table border="1" data-bbox="961 1017 1343 1160"> <tr> <td>H</td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </table> <table border="1" data-bbox="961 1176 1343 1319"> <tr> <td>H</td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </table>	H	T	O				H	T	O				<p>Calculate mentally by using known bonds.</p> <p><math>151 - 6 = ?</math></p> <p><math>151 - 1 - 5 = 145</math></p>						
H	T	O																			
H	T	O																			

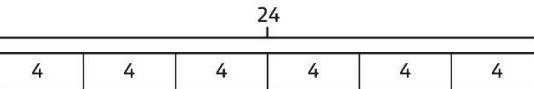
<p><b>3-digit number – 10s, no exchange</b></p>	<p>Subtract the 10s using known bonds.</p>  <p><math>381 - 10 = ?</math></p> <p>8 tens with 1 removed is 7 tens.</p> <p><math>381 - 10 = 371</math></p>	<p>Subtract the 10s using known bonds.</p>  <p><math>8 \text{ tens} - 1 \text{ ten} = 7 \text{ tens}</math></p> <p><math>381 - 10 = 371</math></p>	<p>Use known bonds to subtract the 10s mentally.</p> <p><math>372 - 50 = ?</math></p> <p><math>70 - 50 = 20</math></p> <p>So, <math>372 - 50 = 322</math></p>
<p><b>3-digit number – 10s, exchange or bridging required</b></p>	<p>Use equipment to understand the exchange of 1 hundred for 10 tens.</p> 	<p>Represent the exchange on a place value grid using equipment.</p> <p><math>210 - 20 = ?</math></p>  <p><i>I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.</i></p>  <p><math>210 - 20 = 190</math></p>	<p>Understand the link with counting back on a number line.</p> <p>Use flexible partitioning to support the calculation.</p> <p><math>235 - 60 = ?</math></p>  <p><math>235 = 100 + 130 + 5</math></p> <p><math>235 - 60 = 100 + 70 + 5 = 175</math></p>



<b>Representing subtraction problems</b>		<p>Use bar models to represent subtractions.</p> <p>'Find the difference' is represented as two bars for comparison.</p> <p>Team A </p> <p>Team B </p> <p>Bar models can also be used to show that a part must be taken away from the whole.</p>	<p>Children use alternative representations to check calculations and choose efficient methods.</p> <p>Children use inverse operations to check additions and subtractions.</p> <p>The part-whole model supports understanding.</p> <p><i>I have completed this subtraction.</i>  <math>525 - 270 = 255</math>  <i>I will check using addition.</i></p> <p></p> <p></p>
<b>Year 3 Multiplication</b>			
<b>Understanding equal grouping and repeated addition</b>	<p>Children continue to build understanding of equal groups and the relationship with repeated addition.</p> <p>They recognise both examples and non-examples using objects.</p> <p></p> <p>Children recognise that arrays can be used to model commutative multiplications.</p>	<p>Children recognise that arrays demonstrate commutativity.</p> <p></p> <p><i>This is 3 groups of 4.</i>  <i>This is 4 groups of 3.</i></p>	<p>Children understand the link between repeated addition and multiplication.</p> <p></p> <p><i>8 groups of 3 is 24.</i></p> <p><math>3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 24</math></p> <p><math>8 \times 3 = 24</math></p> <p>A bar model may represent multiplications as equal groups.</p>



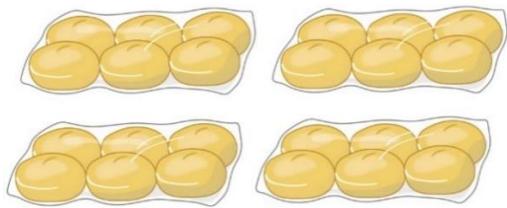
*I can see 3 groups of 8.  
I can see 8 groups of 3.*



$$6 \times 4 = 24$$

### Using commutativity to support understanding of the times-tables

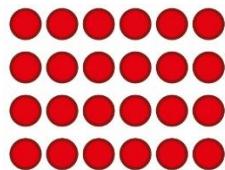
Understand how to use times-tables facts flexibly.



*There are 6 groups of 4 pens.  
There are 4 groups of 6 bread rolls.*

*I can use  $6 \times 4 = 24$  to work out both totals.*

Understand how times-table facts relate to commutativity.



$$6 \times 4 = 24$$
$$4 \times 6 = 24$$

Understand how times-table facts relate to commutativity.

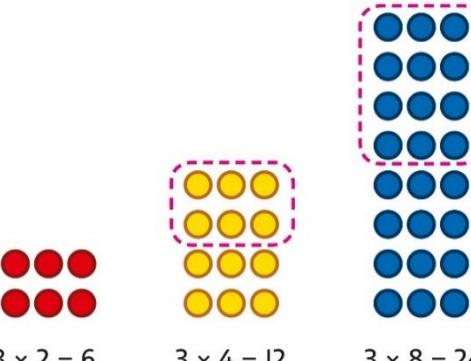
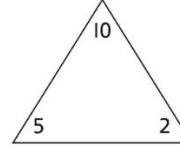
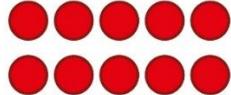
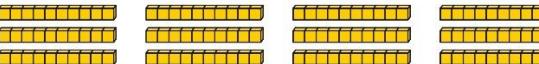
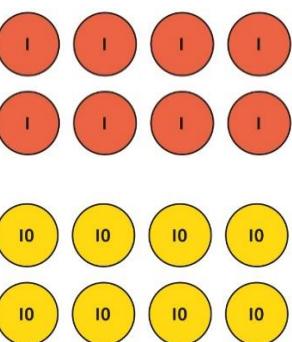
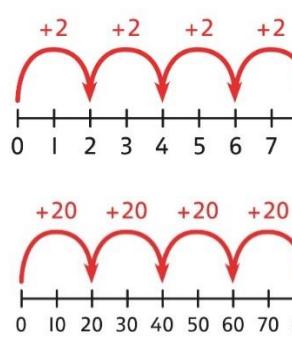
*I need to work out 4 groups of 7.*

*I know that  $7 \times 4 = 28$*

*so, I know that*

*4 groups of 7 = 28  
and*

*7 groups of 4 = 28.*

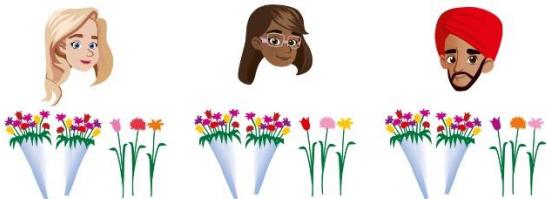
<p><b>Understanding and using <math>\times 3</math>, <math>\times 2</math>, <math>\times 4</math> and <math>\times 8</math> tables.</b></p>	<p>Children learn the times-tables as 'groups of', but apply their knowledge of commutativity.</p>  <p><i>I can use the <math>\times 3</math> table to work out how many keys. I can also use the <math>\times 3</math> table to work out how many batteries.</i></p>	<p>Children understand how the <math>\times 2</math>, <math>\times 4</math> and <math>\times 8</math> tables are related through repeated doubling.</p>  <p><math>3 \times 2 = 6</math>      <math>3 \times 4 = 12</math>      <math>3 \times 8 = 24</math></p>	<p>Children understand the relationship between related multiplication and division facts in known times-tables.</p>   <p><math>2 \times 5 = 10</math> <math>5 \times 2 = 10</math> <math>10 \div 5 = 2</math> <math>10 \div 2 = 5</math></p>
<p><b>Using known facts to multiply 10s, for example <math>3 \times 40</math></b></p>	<p>Explore the relationship between known times-tables and multiples of 10 using place value equipment.</p> <p><i>Make 4 groups of 3 ones.</i></p>  <p><i>Make 4 groups of 3 tens.</i></p>  <p><i>What is the same? What is different?</i></p>	<p>Understand how unitising 10s supports multiplying by multiples of 10.</p>  <p><i>4 groups of 2 ones is 8 ones. 4 groups of 2 tens is 8 tens.</i></p> <p><math>4 \times 2 = 8</math> <math>4 \times 20 = 80</math></p>	<p>Understand how to use known times-tables to multiply multiples of 10.</p>  <p><math>4 \times 2 = 8</math> <math>4 \times 20 = 80</math></p>

## Multiplying a 2-digit number by a 1-digit number

Understand how to link partitioning a 2-digit number with multiplying.

*Each person has 23 flowers.*

*Each person has 2 tens and 3 ones.*



*There are 3 groups of 2 tens.*

*There are 3 groups of 3 ones.*

Use place value equipment to model the multiplication context.

T	O
2	3
2	3
2	3
2	3

*There are 3 groups of 3 ones.*

*There are 3 groups of 2 tens.*

Use place value to support how partitioning is linked with multiplying by a 2-digit number.

$$3 \times 24 = ?$$

T	O
2	4
2	4
2	4
2	4

$$3 \times 4 = 12$$

T	O
2	4
2	4
2	4

$$3 \times 20 = 60$$

$$60 + 12 = 72$$

$$3 \times 24 = 72$$

Use addition to complete multiplications of 2-digit numbers by a 1-digit number.

$$4 \times 13 = ?$$

$$4 \times 3 = 12$$

$$4 \times 10 = 40$$

$$12 + 40 = 52$$

$$4 \times 13 = 52$$

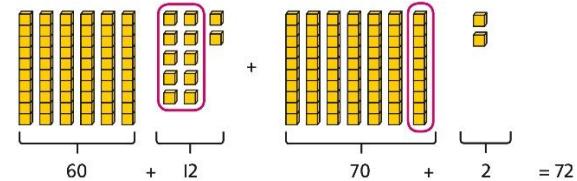
**Multiplying a 2-digit number by a 1-digit number, expanded column method**

Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications.

$$3 \times 24 = ?$$

$$3 \times 20 = 60$$

$$3 \times 4 = 12$$



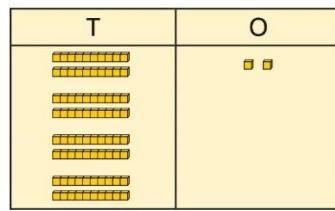
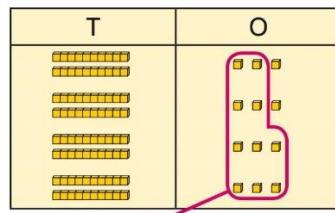
$$3 \times 24 = 60 + 12$$

$$3 \times 24 = 70 + 2$$

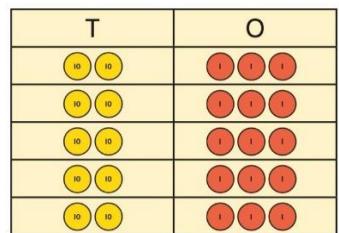
$$3 \times 24 = 72$$

Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s.

$$4 \times 23 = ?$$



$$4 \times 23 = 92$$



$$5 \times 23 = ?$$

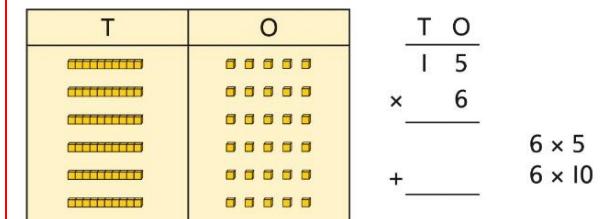
$$5 \times 3 = 15$$

$$5 \times 20 = 100$$

$$5 \times 23 = 115$$

Children may write calculations in expanded column form, but must understand the link with place value and exchange.

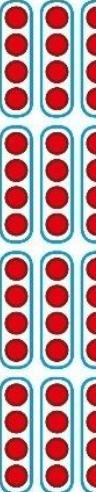
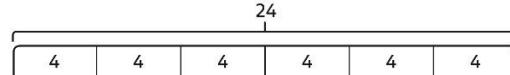
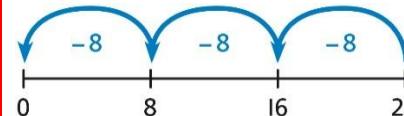
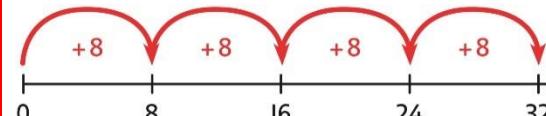
Children are encouraged to write the expanded parts of the calculation separately.

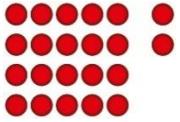
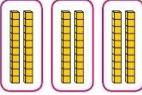
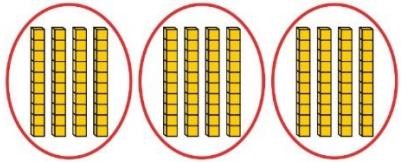


$$\begin{array}{r}
 \text{T} \text{ } \text{O} \\
 1 \text{ } 5 \\
 \times \text{ } 6 \\
 \hline
 6 \times 5 \\
 6 \times 10 \\
 \hline
 \end{array}$$

$$5 \times 28 = ?$$

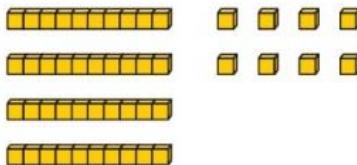
$$\begin{array}{r}
 \text{T} \text{ } \text{O} \\
 2 \text{ } 8 \\
 \times \text{ } 5 \\
 \hline
 40 \\
 100 \\
 \hline
 140
 \end{array}
 \quad
 \begin{array}{l}
 5 \times 8 \\
 5 \times 20 \\
 \hline
 140
 \end{array}$$

Year 3 Division			
<b>Using times-tables knowledge to divide</b> <p>Use knowledge of known times-tables to calculate divisions.</p>  <p><i>24 divided into groups of 8. There are 3 groups of 8.</i></p>	<p>Use knowledge of known times-tables to calculate divisions.</p>  <p><math>48 \div 4 = 12</math></p> <p><i>48 divided into groups of 4. There are 12 groups.</i></p> <p><math>4 \times 12 = 48</math> <math>48 \div 4 = 12</math></p>	<p>Use knowledge of known times-tables to calculate divisions.</p> <p><i>I need to work out 30 shared between 5.</i></p> <p><i>I know that <math>6 \times 5 = 30</math> so I know that <math>30 \div 5 = 6</math>.</i></p> <p>A bar model may represent the relationship between sharing and grouping.</p>  <p><math>24 \div 4 = 6</math> <math>24 \div 6 = 4</math></p> <p>Children understand how division is related to both repeated subtraction and repeated addition.</p>  <p><math>24 \div 8 = 3</math></p>  <p><math>32 \div 8 = 4</math></p>	

<p><b>Understanding remainders</b></p>	<p>Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.</p>  <p><i>There are 13 sticks in total. There are 3 groups of 4, with 1 remainder.</i></p>	<p>Use images to explain remainders.</p>  <p><math>22 \div 5 = 4 \text{ remainder } 2</math></p>	<p>Understand that the remainder is what cannot be shared equally from a set.</p> <p><math>22 \div 5 = ?</math></p> <p><math>3 \times 5 = 15</math>  <math>4 \times 5 = 20</math>  <math>5 \times 5 = 25 \dots \text{this is larger than } 22</math>  <math>\text{So, } 22 \div 5 = 4 \text{ remainder } 2</math></p>
<p><b>Using known facts to divide multiples of 10</b></p>	<p>Use place value equipment to understand how to divide by unitising.</p> <p><i>Make 6 ones divided by 3.</i></p>  <p><i>Now make 6 tens divided by 3.</i></p>  <p><i>What is the same? What is different?</i></p>	<p>Divide multiples of 10 by unitising.</p>  <p><i>12 tens shared into 3 equal groups. 4 tens in each group.</i></p>	<p>Divide multiples of 10 by a single digit using known times-tables.</p> <p><math>180 \div 3 = ?</math></p> <p><i>180 is 18 tens.</i></p> <p><i>18 divided by 3 is 6. 18 tens divided by 3 is 6 tens.</i></p> <p><math>18 \div 3 = 6</math>  <math>180 \div 3 = 60</math></p>

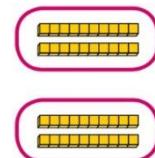
**2-digit number divided by 1-digit number, no remainders**

Children explore dividing 2-digit numbers by using place value equipment.



$$48 \div 2 = ?$$

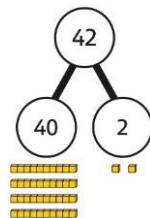
*First divide the 10s.*



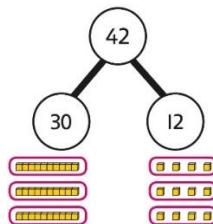
*Then divide the 1s.*



Children explore which partitions support particular divisions.



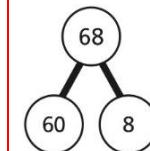
*I need to partition 42 differently to divide by 3.*



$$42 = 30 + 12$$

$$42 \div 3 = 14$$

Children partition a number into 10s and 1s to divide where appropriate.



$$60 \div 2 = 30$$

$$8 \div 2 = 4$$

$$30 + 4 = 34$$

$$68 \div 2 = 34$$

Children partition flexibly to divide where appropriate.

$$42 \div 3 = ?$$

$$42 = 40 + 2$$

*I need to partition 42 differently to divide by 3.*

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

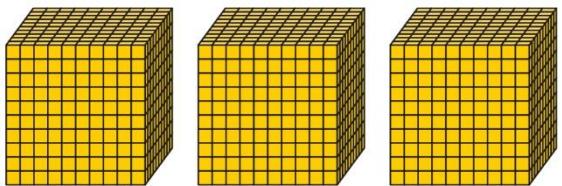
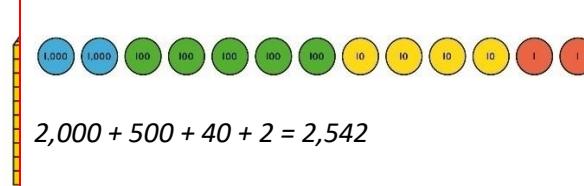
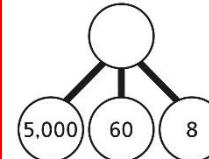
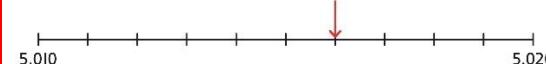
$$12 \div 3 = 4$$

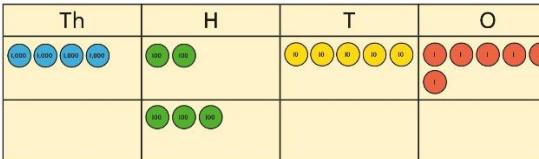
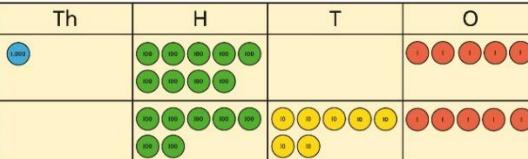
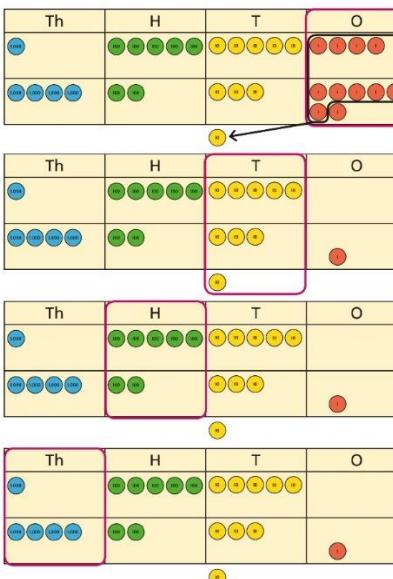
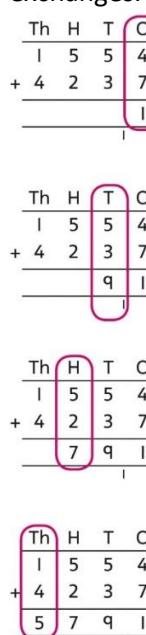
$$10 + 4 = 14$$

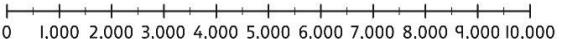
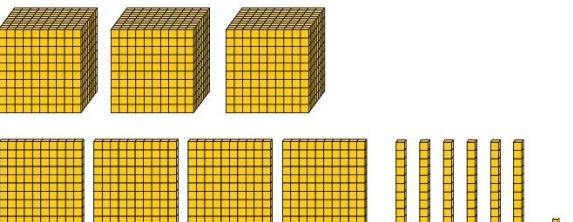
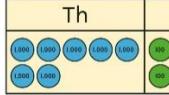
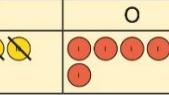
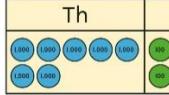
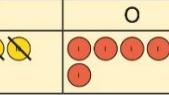
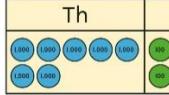
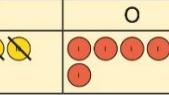
$$42 \div 3 = 14$$

<b>2-digit number divided by 1-digit number, with remainders</b>	<p>Use place value equipment to understand the concept of remainder.</p> <p><i>Make 29 from place value equipment. Share it into 2 equal groups.</i></p>  <p><i>There are two groups of 14 and 1 remainder.</i></p>	<p>Use place value equipment to understand the concept of remainder in division.</p> <p><math>29 \div 2 = ?</math></p>  <p><math>29 \div 2 = 14 \text{ remainder } 1</math></p>	<p>Partition to divide, understanding the remainder in context.</p> <p><i>67 children try to make 5 equal lines.</i></p> <p><math>67 = 50 + 17</math>  <math>50 \div 5 = 10</math></p> <p><math>17 \div 5 = 3 \text{ remainder } 2</math>  <math>67 \div 5 = 13 \text{ remainder } 2</math></p> <p><i>There are 13 children in each line and 2 children left out.</i></p>
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#### Year 4

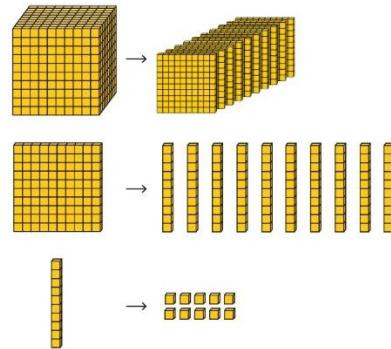
	Concrete	Pictorial	Abstract
Year 4 Addition			
Understanding numbers to 10,000	<p>Use place value equipment to understand the place value of 4-digit numbers.</p>  <p><i>4 thousands equal 4,000.</i></p> <p><i>1 thousand is 10 hundreds.</i></p>	<p>Represent numbers using place value counters once children understand the relationship between 1,000s and 100s.</p>  <p><math>2,000 + 500 + 40 + 2 = 2,542</math></p>	<p>Understand partitioning of 4-digit numbers, including numbers with digits of 0.</p>  <p><math>5,000 + 60 + 8 = 5,068</math></p> <p>Understand and read 4-digit numbers on a number line.</p> 

<p><b>Choosing mental methods where appropriate</b></p>	<p>Use unitising and known facts to support mental calculations.</p> <p><i>Make 1,405 from place value equipment.</i></p> <p>Add 2,000.</p> <p>Now add the 1,000s. 1 thousand + 2 thousands = 3 thousands</p> <p><math>1,405 + 2,000 = 3,405</math></p>	<p>Use unitising and known facts to support mental calculations.</p> <p></p> <p><i>I can add the 100s mentally.</i></p> <p><math>200 + 300 = 500</math></p> <p><i>So, <math>4,256 + 300 = 4,556</math></i></p>	<p>Use unitising and known facts to support mental calculations.</p> <p><math>4,256 + 300 = ?</math></p> <p><math>2 + 3 = 5 \quad 200 + 300 = 500</math></p> <p><math>4,256 + 300 = 4,556</math></p>
<p><b>Column addition with exchange</b></p>	<p>Use place value equipment on a place value grid to organise thinking.</p> <p>Ensure that children understand how the columns relate to place value and what to do if the numbers are not all 4-digit numbers.</p> <p><i>Use equipment to show <math>1,905 + 775</math>.</i></p> <p></p> <p><i>Why have only three columns been used for the second row? Why is the Thousands box empty?</i></p> <p><i>Which columns will total 10 or more?</i></p>	<p>Use place value equipment to model required exchanges.</p> <p></p> <p><i>Include examples that exchange in more than one column.</i></p>	<p>Use a column method to add, including exchanges.</p> <p></p> <p><i>Include examples that exchange in more than one column.</i></p>

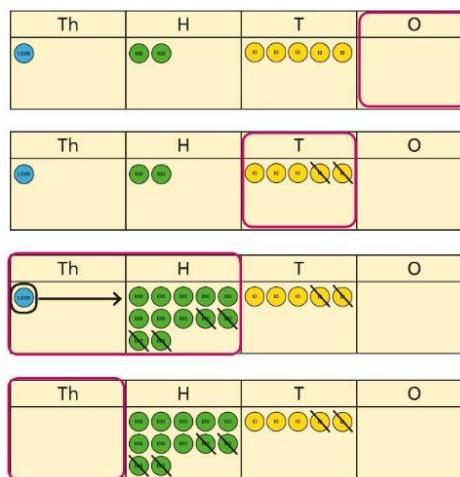
<b>Representing additions and checking strategies</b>		<p>Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate.</p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td colspan="2" style="text-align: center;">1,373</td></tr> <tr><td style="text-align: center;">799</td><td style="text-align: center;">574</td></tr> </table> <table style="display: inline-table; vertical-align: middle;"> <tr><td style="text-align: right;">Th</td><td style="text-align: right;">H</td><td style="text-align: right;">T</td><td style="text-align: right;">O</td></tr> <tr><td style="text-align: right;">7</td><td style="text-align: right;">9</td><td style="text-align: right;">9</td><td></td></tr> <tr><td style="text-align: right;">+</td><td style="text-align: right;">5</td><td style="text-align: right;">7</td><td style="text-align: right;">4</td></tr> <tr><td style="text-align: right;">1</td><td style="text-align: right;">3</td><td style="text-align: right;">7</td><td style="text-align: right;">3</td></tr> <tr><td style="text-align: right;">1</td><td style="text-align: right;">1</td><td style="text-align: right;">1</td><td></td></tr> </table> <p><i>I chose to work out 574 + 800, then subtract 1.</i></p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td colspan="2" style="text-align: center;">6,000</td></tr> <tr><td style="text-align: center;">2,999</td><td style="text-align: center;">3,001</td></tr> </table> <p><i>This is equivalent to 3,000 + 3,000.</i></p>	1,373		799	574	Th	H	T	O	7	9	9		+	5	7	4	1	3	7	3	1	1	1		6,000		2,999	3,001	<p>Use rounding and estimating on a number line to check the reasonableness of an addition.</p>  <p><math>912 + 6,149 = ?</math></p> <p><i>I used rounding to work out that the answer should be approximately <math>1,000 + 6,000 = 7,000</math>.</i></p>
1,373																															
799	574																														
Th	H	T	O																												
7	9	9																													
+	5	7	4																												
1	3	7	3																												
1	1	1																													
6,000																															
2,999	3,001																														
<b>Year 4 Subtraction</b>	<b>Choosing mental methods where appropriate</b> <p>Use place value equipment to justify mental methods.</p>  <p><i>What number will be left if we take away 300?</i></p>	<p>Use place value grids to support mental methods where appropriate.</p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td style="text-align: center;">Th</td><td style="text-align: center;">H</td><td style="text-align: center;">T</td><td style="text-align: center;">O</td></tr> <tr><td>  </td><td>  </td><td>  </td><td>  </td></tr> </table> <p><math>7,646 - 40 = 7,606</math></p>	Th	H	T	O					<p>Use knowledge of place value and unitising to subtract mentally where appropriate.</p> <p><math>3,501 - 2,000</math></p> <p><math>3 \text{ thousands} - 2 \text{ thousands} = 1 \text{ thousand}</math></p> <p><math>3,501 - 2,000 = 1,501</math></p>																				
Th	H	T	O																												
																															

### Column subtraction with exchange

Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.

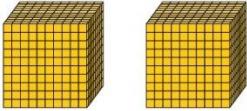
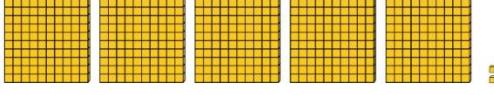
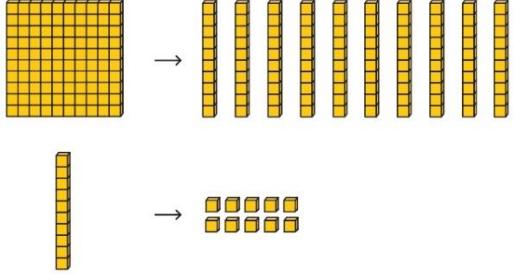
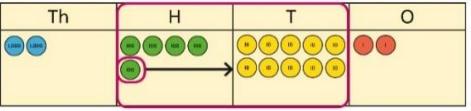
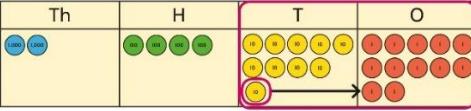
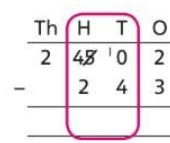
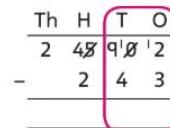
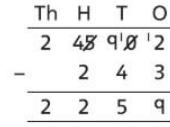
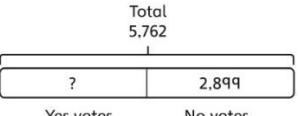
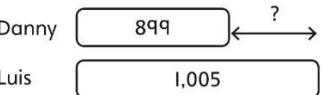
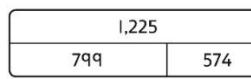
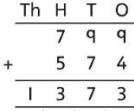


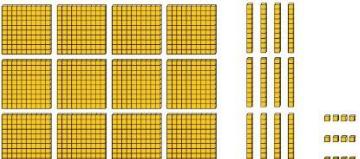
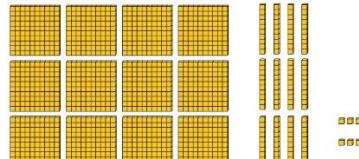
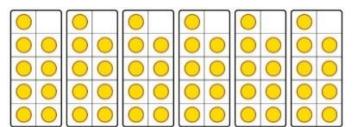
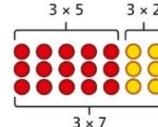
Represent place value equipment on a place value grid to subtract, including exchanges where needed.

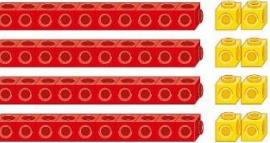
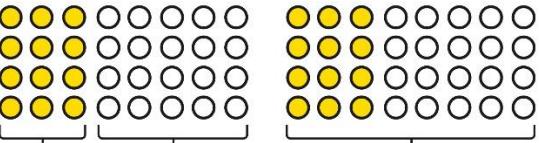
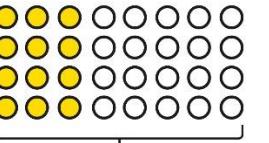
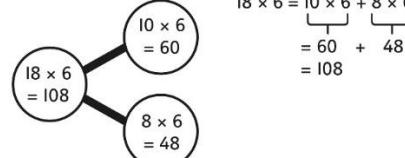
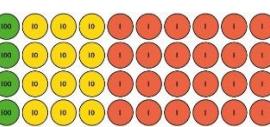
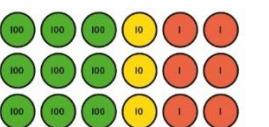


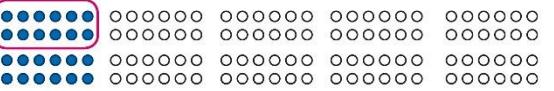
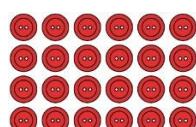
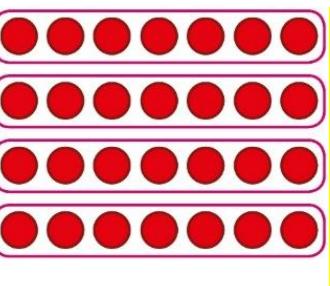
Use column subtraction, with understanding of the place value of any exchange required.

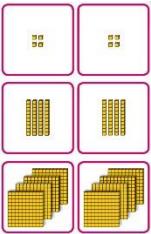
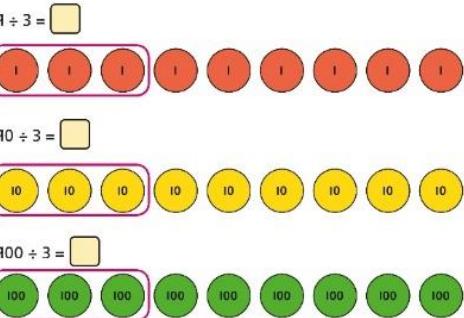
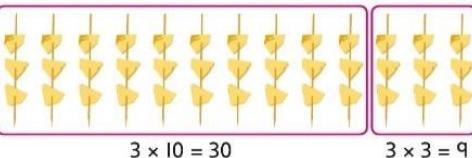
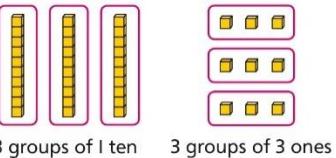
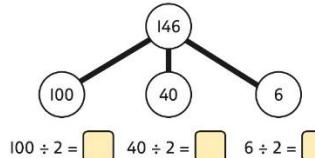
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 \begin{array}{r}
 \text{Th} & \text{H} & \text{T} & \text{O} \\
 \boxed{1} & 2 & 5 & 0 \\
 - & 4 & 2 & 0 \\
 \hline
 & & & \boxed{0}
 \end{array} \\
 \begin{array}{r}
 \text{Th} & \text{H} & \text{T} & \text{O} \\
 \boxed{1} & 2 & 5 & 0 \\
 - & 4 & 2 & 0 \\
 \hline
 & & \boxed{3} & 0
 \end{array} \\
 \begin{array}{r}
 \text{Th} & \text{H} & \text{T} & \text{O} \\
 \cancel{1} & 2 & 5 & 0 \\
 - & 4 & 2 & 0 \\
 \hline
 & \boxed{8} & 3 & 0
 \end{array} \\
 \begin{array}{r}
 \text{Th} & \text{H} & \text{T} & \text{O} \\
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 & \boxed{8} & 3 & 0
 \end{array}
 \end{array}$$

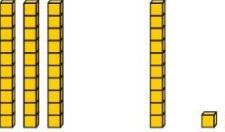
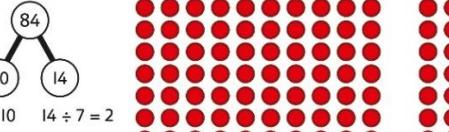
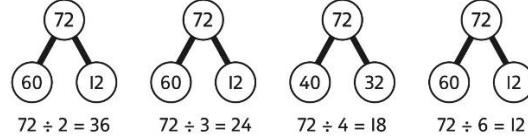
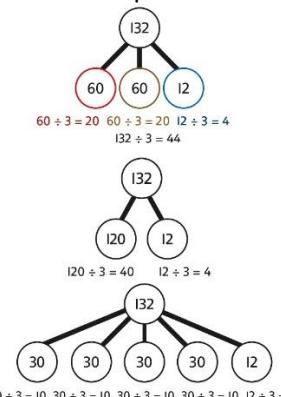
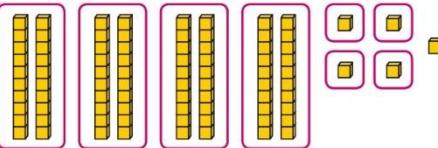
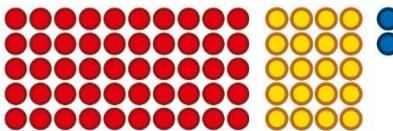
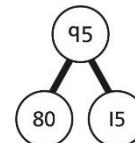
<p><b>Column subtraction with exchange across more than one column</b></p>	<p>Understand why two exchanges may be necessary.  <math>2,502 - 243 = ?</math></p>  <p></p> <p><i>I need to exchange a 10 for some 1s, but there are not any 10s here.</i></p> 	<p>Make exchanges across more than one column where there is a zero as a place holder.  <math>2,502 - 243 = ?</math></p>  	<p>Make exchanges across more than one column where there is a zero as a place holder.  <math>2,502 - 243 = ?</math></p>   
<p><b>Representing subtractions and checking strategies</b></p>		<p>Use bar models to represent subtractions where a part needs to be calculated.</p>  <p><i>I can work out the total number of Yes votes using <math>5,762 - 2,899</math>.</i></p> <p>Bar models can also represent 'find the difference' as a subtraction problem.</p> 	<p>Use inverse operations to check subtractions.</p> <p><i>I calculated <math>1,225 - 799 = 574</math>. I will check by adding the parts.</i></p>   <p><i>The parts do not add to make 1,225. I must have made a mistake.</i></p>

<b>Year 4</b> <b>Multiplication</b>			
<b>Multiplying by multiples of 10 and 100</b>	<p>Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.</p>  <p>3 groups of 4 ones is 12 ones. 3 groups of 4 tens is 12 tens. 3 groups of 4 hundreds is 12 hundreds.</p>	<p>Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.</p>  <p><math>3 \times 4 = 12</math> <math>3 \times 40 = 120</math> <math>3 \times 400 = 1,200</math></p>	<p>Use known facts and understanding of place value and commutativity to multiply mentally.</p> <p><math>4 \times 7 = 28</math> <math>4 \times 70 = 280</math> <math>40 \times 7 = 280</math> <math>4 \times 700 = 2,800</math> <math>400 \times 7 = 2,800</math></p>
<b>Understanding times-tables up to <math>12 \times 12</math></b>	<p>Understand the special cases of multiplying by 1 and 0.</p>  <p><math>5 \times 1 = 5</math>      <math>5 \times 0 = 0</math></p>	<p>Represent the relationship between the <math>\times 9</math> table and the <math>\times 10</math> table.</p>  <p>Represent the <math>\times 11</math> table and <math>\times 12</math> tables in relation to the <math>\times 10</math> table.</p>  <p><math>2 \times 11 = 20 + 2</math> <math>3 \times 11 = 30 + 3</math> <math>4 \times 11 = 40 + 4</math>  <math>4 \times 12 = 40 + 8</math></p>	<p>Understand how times-tables relate to counting patterns.</p> <p>Understand links between the <math>\times 3</math> table, <math>\times 6</math> table and <math>\times 9</math> table <math>5 \times 6</math> is double <math>5 \times 3</math></p> <p><math>\times 5</math> table and <math>\times 6</math> table <i>I know that <math>7 \times 5 = 35</math> so I know that <math>7 \times 6 = 35 + 7</math>.</i></p> <p><math>\times 5</math> table and <math>\times 7</math> table <math>3 \times 7 = 3 \times 5 + 3 \times 2</math></p>  <p><math>\times 9</math> table and <math>\times 10</math> table <math>6 \times 10 = 60</math> <math>6 \times 9 = 60 - 6</math></p>

<h3>Understanding and using partitioning in multiplication</h3>	<p>Make multiplications by partitioning.</p> <p><math>4 \times 12</math> is 4 groups of 10 and 4 groups of 2.</p>  <p><math>4 \times 12 = 40 + 8</math></p>	<p>Understand how multiplication and partitioning are related through addition.</p>  <p><math>4 \times 3 = 12</math>  <math>4 \times 5 = 20</math>  <math>12 + 20 = 32</math></p>  <p><math>4 \times 8 = 32</math></p>	<p>Use partitioning to multiply 2-digit numbers by a single digit.</p> <p><math>18 \times 6 = ?</math></p>  <p><math>18 \times 6 = 10 \times 6 + 8 \times 6</math>  <math>= 60 + 48</math>  <math>= 108</math></p>
<h3>Column multiplication for 2- and 3-digit numbers multiplied by a single digit</h3>	<p>Use place value equipment to make multiplications.</p> <p>Make <math>4 \times 136</math> using equipment.</p>  <p><i>I can work out how many 1s, 10s and 100s.</i></p> <p><i>There are <math>4 \times 6</math> ones... 24 ones</i>  <i>There are <math>4 \times 3</math> tens ... 12 tens</i>  <i>There are <math>4 \times 1</math> hundreds ... 4 hundreds</i></p> <p><math>24 + 120 + 400 = 544</math></p>	<p>Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit.</p>  <p><math display="block">  \begin{array}{r}  3 \ 1 \ 2 \\  \times \ 3 \\  \hline  9 \ 3 \ 6  \end{array}  </math></p>	<p>Use the formal column method for up to 3-digit numbers multiplied by a single digit.</p> <p><math display="block">  \begin{array}{r}  3 \ 1 \ 2 \\  \times \ 3 \\  \hline  9 \ 3 \ 6  \end{array}  </math></p> <p>Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation.</p> <p><math display="block">  \begin{array}{r}  2 \ 3 \\  \times \ 5 \\  \hline  1 \ 5 \\  1 \ 0 \ 0 \\  \hline  1 \ 1 \ 5  \end{array}  \qquad  \begin{array}{r}  2 \ 3 \\  \times \ 5 \\  \hline  1 \ 1 \ 5  \end{array}  </math></p>

<b>Multiplying more than two numbers</b>	<p>Represent situations by multiplying three numbers together.</p>  <p>Each sheet has <math>2 \times 5</math> stickers. There are 3 sheets.</p> <p>There are <math>5 \times 2 \times 3</math> stickers in total.</p> $5 \times 2 \times 3 = 30$ $\begin{array}{c} 10 \times 3 = 30 \\ \hline \end{array}$	<p>Understand that commutativity can be used to multiply in different orders.</p>  $2 \times 6 \times 10 = 120$ $12 \times 10 = 120$ $10 \times 6 \times 2 = 120$ $60 \times 2 = 120$	<p>Use knowledge of factors to simplify some multiplications.</p> $24 \times 5 = 12 \times 2 \times 5$ $\begin{array}{c} 12 \times 2 \times 5 = \\ \hline 12 \times 10 = 120 \\ \hline \end{array}$ <p>So, <math>24 \times 5 = 120</math></p>
<b>Year 4 Division</b>	<p><b>Understanding the relationship between multiplication and division, including times-tables</b></p> <p>Use objects to explore families of multiplication and division facts.</p>  $4 \times 6 = 24$ <p>24 is 6 groups of 4. 24 is 4 groups of 6.</p> <p>24 divided by 6 is 4. 24 divided by 4 is 6.</p>	<p>Represent divisions using an array.</p>  $28 \div 7 = 4$	<p>Understand families of related multiplication and division facts.</p> <p>I know that <math>5 \times 7 = 35</math> so I know all these facts:</p> $\begin{array}{l} 5 \times 7 = 35 \\ 7 \times 5 = 35 \\ 35 = 5 \times 7 \\ 35 = 7 \times 5 \\ 35 \div 5 = 7 \\ 35 \div 7 = 5 \\ 7 = 35 \div 5 \\ 5 = 35 \div 7 \end{array}$

<b>Dividing multiples of 10 and 100 by a single digit</b>	<p>Use place value equipment to understand how to use unitising to divide.</p>  <p>8 ones divided into 2 equal groups 4 ones in each group</p> <p>8 tens divided into 2 equal groups 4 tens in each group</p> <p>8 hundreds divided into 2 equal groups 4 hundreds in each group</p>	<p>Represent divisions using place value equipment.</p>  <p><math>9 \div 3 =</math> <input type="text"/></p> <p><math>90 \div 3 =</math> <input type="text"/></p> <p><math>900 \div 3 =</math> <input type="text"/></p> <p><math>9 \div 3 = 3</math></p> <p>9 tens divided by 3 is 3 tens. 9 hundreds divided by 3 is 3 hundreds.</p>	<p>Use known facts to divide 10s and 100s by a single digit.</p> <p><math>15 \div 3 = 5</math></p> <p><math>150 \div 3 = 50</math></p> <p><math>1500 \div 3 = 500</math></p>
<b>Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s</b>	<p>Partition into 10s and 1s to divide where appropriate.</p> <p><math>39 \div 3 = ?</math></p>  <p><math>3 \times 10 = 30</math></p> <p><math>3 \times 3 = 9</math></p> <p><math>39 = 30 + 9</math></p> <p><math>30 \div 3 = 10</math></p> <p><math>9 \div 3 = 3</math></p> <p><math>39 \div 3 = 13</math></p>	<p>Partition into 100s, 10s and 1s using Base 10 equipment to divide where appropriate.</p> <p><math>39 \div 3 = ?</math></p>  <p>3 groups of 1 ten</p> <p>3 groups of 3 ones</p> <p><math>39 = 30 + 9</math></p> <p><math>30 \div 3 = 10</math></p> <p><math>9 \div 3 = 3</math></p> <p><math>39 \div 3 = 13</math></p>	<p>Partition into 100s, 10s and 1s using a part-whole model to divide where appropriate.</p> <p><math>142 \div 2 = ?</math></p>  <p><math>100 \div 2 =</math> <input type="text"/></p> <p><math>40 \div 2 =</math> <input type="text"/></p> <p><math>6 \div 2 =</math> <input type="text"/></p> <p><math>100 \div 2 = 50</math></p> <p><math>40 \div 2 = 20</math></p> <p><math>6 \div 2 = 3</math></p> <p><math>50 + 20 + 3 = 73</math></p> <p><math>142 \div 2 = 73</math></p>

<p><b>Dividing 2-digit and 3-digit numbers by a single digit, using flexible partitioning</b></p>	<p>Use place value equipment to explore why different partitions are needed.</p> <p><math>42 \div 3 = ?</math></p> <p><i>I will split it into 30 and 12, so that I can divide by 3 more easily.</i></p> 	<p>Represent how to partition flexibly where needed.</p> <p><math>84 \div 7 = ?</math></p> <p><i>I will partition into 70 and 14 because I am dividing by 7.</i></p>  <p>84 <math>\div</math> 7 = 12</p> <p>70 <math>\div</math> 7 = 10   14 <math>\div</math> 7 = 2</p>	<p>Make decisions about appropriate partitioning based on the division required.</p>  <p><math>72 \div 2 = 36</math>   <math>72 \div 3 = 24</math>   <math>72 \div 4 = 18</math>   <math>72 \div 6 = 12</math></p> <p>Understand that different partitions can be used to complete the same division.</p>  <p><math>60 \div 3 = 20</math>   <math>60 \div 3 = 20</math>   <math>12 \div 3 = 4</math>  <math>132 \div 3 = 44</math></p> <p><math>120 \div 3 = 40</math>   <math>12 \div 3 = 4</math></p> <p><math>30 \div 3 = 10</math>   <math>30 \div 3 = 10</math>   <math>30 \div 3 = 10</math>   <math>30 \div 3 = 10</math>   <math>12 \div 3 = 4</math></p>
<p><b>Understanding remainders</b></p>	<p>Use place value equipment to find remainders.</p> <p><i>85 shared into 4 equal groups</i></p> <p><i>There are 24, and 1 that cannot be shared.</i></p> 	<p>Represent the remainder as the part that cannot be shared equally.</p>  <p><math>72 \div 5 = 14</math> remainder 2</p>	<p>Understand how partitioning can reveal remainders of divisions.</p>  <p><math>80 \div 4 = 20</math>  <math>12 \div 4 = 3</math></p> <p><math>95 \div 4 = 23</math> remainder 3</p>

## KEY STAGE 2

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

**Key language:** decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

**Addition and subtraction:** Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.

Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.

Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.

**Multiplication and division:** Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.

Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.

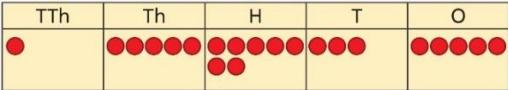
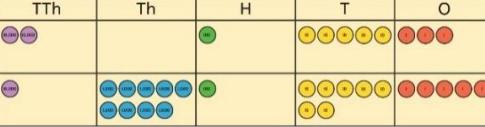
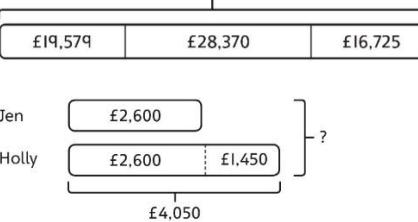
Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.

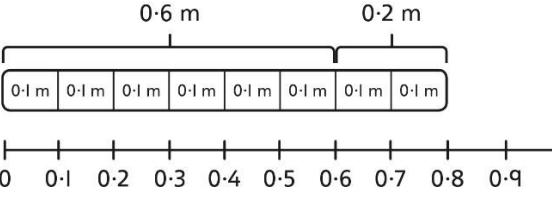
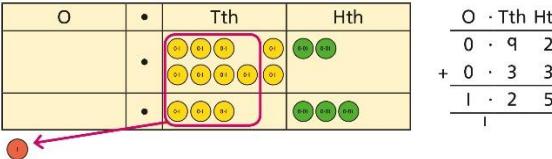
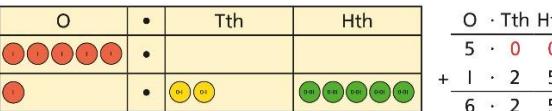
Multiplication and division of decimals are also introduced and refined in Year 6.

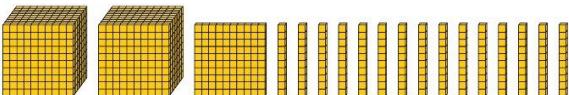
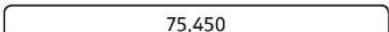
**Fractions:** Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them.

Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.

Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

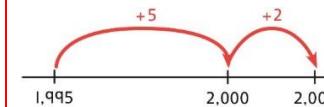
	Concrete	Pictorial	Abstract
Year 5 Addition			
Column addition with whole numbers	<p>Use place value equipment to represent additions.</p> <p><i>Add a row of counters onto the place value grid to show <math>15,735 + 4,012</math>.</i></p> 	<p>Represent additions, using place value equipment on a place value grid alongside written methods.</p>  <p><i>I need to exchange 10 tens for a 100.</i></p> $  \begin{array}{r}  \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\  \hline  2 & 0 & 1 & 5 & 3 \\  + & 1 & 9 & 1 & 7 & 5 \\  \hline  3 & 9 & 3 & 2 & 8 \\  \hline  \end{array}  $	<p>Use column addition, including exchanges.</p> $  \begin{array}{r}  \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\  \hline  1 & 9 & 1 & 7 & 5 \\  + & 1 & 8 & 4 & 1 & 7 \\  \hline  3 & 7 & 5 & 9 & 2 \\  \hline  \end{array}  $
Representing additions		<p>Bar models represent addition of two or more numbers in the context of problem solving.</p>  $  \begin{array}{r}  \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\  \hline  2 & 3 & 4 & 0 & 5 \\  + & 7 & 8 & 9 & 2 \\  \hline  2 & 0 & 2 & 9 & 7 \\  \hline  \end{array}  $ $  \begin{array}{r}  \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\  \hline  2 & 3 & 4 & 0 & 5 \\  + & 7 & 8 & 9 & 2 \\  \hline  3 & 1 & 2 & 9 & 7 \\  \hline  \end{array}  $	<p>Use approximation to check whether answers are reasonable.</p> <p><i>I will use <math>23,000 + 8,000</math> to check.</i></p>

<b>Adding tenths</b>	<p>Link measure with addition of decimals.</p> <p><i>Two lengths of fencing are 0.6 m and 0.2 m. How long are they when added together?</i></p> <p>0.6 m                    0.2 m</p> 	<p>Use a bar model with a number line to add tenths.</p>  <p><math>0.6 + 0.2 = 0.8</math> <math>6 \text{ tenths} + 2 \text{ tenths} = 8 \text{ tenths}</math></p>	<p>Understand the link with adding fractions.</p> $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$ <p><math>6 \text{ tenths} + 2 \text{ tenths} = 8 \text{ tenths}</math> <math>0.6 + 0.2 = 0.8</math></p>
<b>Adding decimals using column addition</b>	<p>Use place value equipment to represent additions.</p> <p><i>Show 0.23 + 0.45 using place value counters.</i></p>	<p>Use place value equipment on a place value grid to represent additions.</p> <p>Represent exchange where necessary.</p>  <p>Include examples where the numbers of decimal places are different.</p> 	<p>Add using a column method, ensuring that children understand the link with place value.</p> $  \begin{array}{r}  \text{O} \cdot \text{Tth} \text{ Hth} \\  0 \cdot 2 \quad 3 \\  + 0 \cdot 4 \quad 5 \\  \hline  0 \cdot 6 \quad 8  \end{array}  $ <p>Include exchange where required, alongside an understanding of place value.</p> $  \begin{array}{r}  \text{O} \cdot \text{Tth} \text{ Hth} \\  0 \cdot 9 \quad 2 \\  + 0 \cdot 3 \quad 3 \\  \hline  1 \cdot 2 \quad 5  \end{array}  $ <p>Include additions where the numbers of decimal places are different.</p> <p><math>3.4 + 0.65 = ?</math></p> $  \begin{array}{r}  \text{O} \cdot \text{Tth} \text{ Hth} \\  3 \cdot 4 \quad 0 \\  + 0 \cdot 6 \quad 5 \\  \hline  \end{array}  $

<b>Year 5</b> <b>Subtraction</b>																																																																																																							
<b>Column subtraction with whole numbers</b>	<p>Use place value equipment to understand where exchanges are required.</p> <p><math>2,250 - 1,070</math></p> 	<p>Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.</p> <p><math>15,735 - 2,582 = 13,153</math></p> <table border="1" data-bbox="961 473 1529 568"> <thead> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>5</td> <td>7</td> <td>3</td> <td>5</td> </tr> <tr> <td>-</td> <td>2</td> <td>5</td> <td>8</td> <td>2</td> </tr> <tr> <td colspan="5" style="text-align: right;"><hr/></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>3</td> </tr> </tbody> </table> <p>Now subtract the 10s. Exchange 1 hundred for 10 tens.</p> <table border="1" data-bbox="961 616 1529 711"> <thead> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>5</td> <td>7</td> <td>3</td> <td>5</td> </tr> <tr> <td>-</td> <td>2</td> <td>5</td> <td>8</td> <td>2</td> </tr> <tr> <td colspan="5" style="text-align: right;"><hr/></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>5</td> </tr> </tbody> </table> <p>Subtract the 100s, 1,000s and 10,000s.</p> <table border="1" data-bbox="961 751 1529 846"> <thead> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>5</td> <td>7</td> <td>3</td> <td>5</td> </tr> <tr> <td>-</td> <td>2</td> <td>5</td> <td>8</td> <td>2</td> </tr> <tr> <td colspan="5" style="text-align: right;"><hr/></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>1</td> </tr> </tbody> </table>	TTh	Th	H	T	O	1	5	7	3	5	-	2	5	8	2	<hr/>									3	TTh	Th	H	T	O	1	5	7	3	5	-	2	5	8	2	<hr/>									5	TTh	Th	H	T	O	1	5	7	3	5	-	2	5	8	2	<hr/>									1	<p>Use column subtraction methods with exchange where required.</p> <table border="1" data-bbox="1551 330 1769 462"> <thead> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>6</td> <td>1</td> <td>0</td> <td>9</td> </tr> <tr> <td>-</td> <td>1</td> <td>8</td> <td>5</td> <td>3</td> </tr> <tr> <td colspan="5" style="text-align: right;"><hr/></td> </tr> <tr> <td>4</td> <td>3</td> <td>5</td> <td>6</td> <td>3</td> </tr> </tbody> </table> <p><math>62,097 - 18,534 = 43,563</math></p>	TTh	Th	H	T	O	5	6	1	0	9	-	1	8	5	3	<hr/>					4	3	5	6	3
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<b>Checking strategies and representing subtractions</b>	<p>Bar models represent subtractions in problem contexts, including 'find the difference'.</p> <p>Athletics Stadium </p> <p>Hockey Centre </p> <p>Velodrome </p>	<p>Children can explain the mistake made when the columns have not been ordered correctly.</p> <table border="1" data-bbox="1551 965 1702 1097"> <thead> <tr> <th colspan="5">Bella's working</th> </tr> <tr> <th>T</th> <th>T</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>7</td> <td>8</td> <td>7</td> <td>7</td> </tr> <tr> <td>+ 4</td> <td>0</td> <td>1</td> <td>2</td> <td></td> </tr> <tr> <td colspan="5" style="text-align: right;"><hr/></td> </tr> <tr> <td>5</td> <td>7</td> <td>9</td> <td>9</td> <td>7</td> </tr> </tbody> </table> <table border="1" data-bbox="1731 965 1882 1097"> <thead> <tr> <th colspan="5">Correct method</th> </tr> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>7</td> <td>8</td> <td>7</td> <td>7</td> </tr> <tr> <td>+ 4</td> <td>0</td> <td>1</td> <td>2</td> <td></td> </tr> <tr> <td colspan="5" style="text-align: right;"><hr/></td> </tr> <tr> <td>2</td> <td>1</td> <td>8</td> <td>8</td> <td>9</td> </tr> </tbody> </table>	Bella's working					T	T	H	T	O	1	7	8	7	7	+ 4	0	1	2		<hr/>					5	7	9	9	7	Correct method					TTh	Th	H	T	O	1	7	8	7	7	+ 4	0	1	2		<hr/>					2	1	8	8	9	<p>Use approximation to check calculations.</p> <p><i>I calculated 18,000 + 4,000 mentally to check my subtraction.</i></p>																																								
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**Choosing efficient methods**

To subtract two large numbers that are close, children find the difference by counting on.  
 $2,002 - 1,995 = ?$



Use addition to check subtractions.  
*I calculated  $7,546 - 2,355 = 5,191$ .  
 I will check using the inverse.*

**Subtracting decimals**

Explore complements to a whole number by working in the context of length.



$$1 \text{ m} - \boxed{\phantom{0}} \text{ m} = \boxed{\phantom{0}} \text{ m}$$

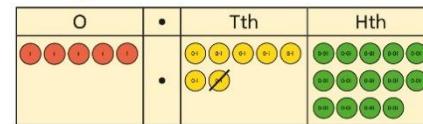
$$1 - 0.49 = ?$$

Use a place value grid to represent the stages of column subtraction, including exchanges where required.

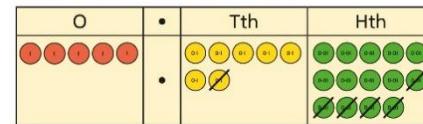
$$5.74 - 2.25 = ?$$



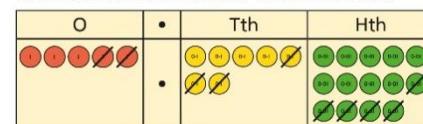
Exchange 1 tenth for 10 hundredths.



Now subtract the 5 hundredths.

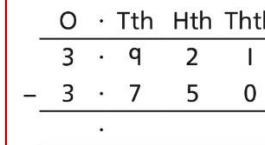


Now subtract the 2 tenths, then the 2 ones.

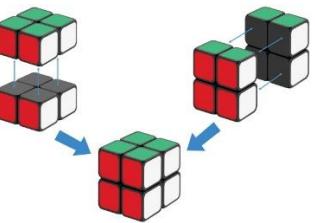
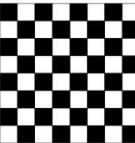
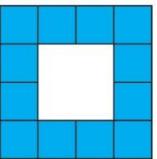
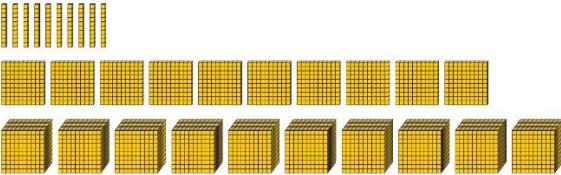


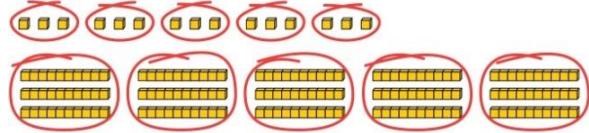
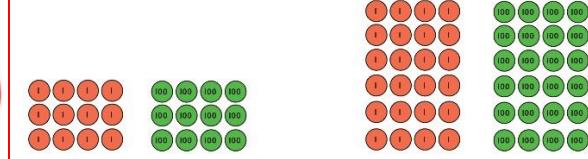
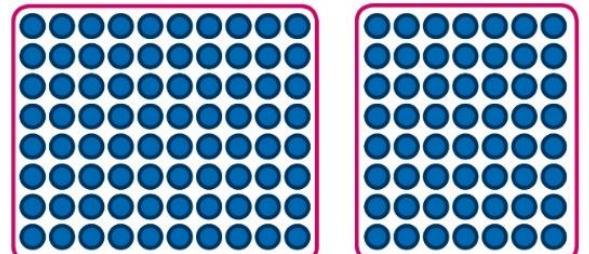
Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places.

$$3.921 - 3.75 = ?$$



q

<b>Year 5</b> <b>Multiplication</b>															
<b>Understanding factors</b>	<p>Use cubes or counters to explore the meaning of 'square numbers'.</p> <p><i>25 is a square number because it is made from 5 rows of 5.</i></p> <p>Use cubes to explore cube numbers.</p>  <p><i>8 is a cube number.</i></p>	<p>Use images to explore examples and non-examples of square numbers.</p>  <p><math>8 \times 8 = 64</math>  <math>8^2 = 64</math></p>  <p><i>12 is not a square number, because you cannot multiply a whole number by itself to make 12.</i></p>	<p>Understand the pattern of square numbers in the multiplication tables.</p> <p>Use a multiplication grid to circle each square number. Can children spot a pattern?</p>												
<b>Multiplying by 10, 100 and 1,000</b>	<p>Use place value equipment to multiply by 10, 100 and 1,000 by unitising.</p> <table border="1" data-bbox="361 981 923 1140"> <tbody> <tr> <td><math>4 \times 1 = 4 \text{ ones} = 4</math></td> <td></td> </tr> <tr> <td><math>4 \times 10 = 4 \text{ tens} = 40</math></td> <td></td> </tr> <tr> <td><math>4 \times 100 = 4 \text{ hundreds} = 400</math></td> <td></td> </tr> </tbody> </table>	$4 \times 1 = 4 \text{ ones} = 4$		$4 \times 10 = 4 \text{ tens} = 40$		$4 \times 100 = 4 \text{ hundreds} = 400$		<p>Understand the effect of repeated multiplication by 10.</p> 	<p>Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.</p> <table border="1" data-bbox="1567 981 1927 1108"> <thead> <tr> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td>I</td> <td>7</td> </tr> </tbody> </table> <p><math>17 \times 10 = 170</math>  <math>17 \times 100 = 17 \times 10 \times 10 = 1,700</math>  <math>17 \times 1,000 = 17 \times 10 \times 10 \times 10 = 17,000</math></p>	H	T	O		I	7
$4 \times 1 = 4 \text{ ones} = 4$															
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<p><b>Multiplying by multiples of 10, 100 and 1,000</b></p>	<p>Use place value equipment to explore multiplying by unitising.</p>  <p>5 groups of 3 ones is 15 ones. 5 groups of 3 tens is 15 tens.  So, I know that 5 groups of 3 thousands would be 15 thousands.</p>	<p>Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.</p>  <p><math>4 \times 3 = 12</math>      <math>6 \times 4 = 24</math>  <math>4 \times 300 = 1,200</math>      <math>6 \times 400 = 2,400</math></p>	<p>Use known facts and unitising to multiply.</p> <p><math>5 \times 4 = 20</math>  <math>5 \times 40 = 200</math>  <math>5 \times 400 = 2,000</math>  <math>5 \times 4,000 = 20,000</math>  <math>5,000 \times 4 = 20,000</math></p>																									
<p><b>Multiplying up to 4-digit numbers by a single digit</b></p>	<p>Explore how to use partitioning to multiply efficiently.</p> <p><math>8 \times 17 = ?</math></p>  <p><math>8 \times 10 = 80</math>  <math>8 \times 7 = 56</math>  <math>80 + 56 = 136</math>    <math>So, 8 \times 17 = 136</math></p>	<p>Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.</p> <table border="1" data-bbox="956 794 1401 1203"> <thead> <tr> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>(100)</td> <td>(10) (10) (10) (10) (10) (10)</td> <td>(1) (1) (1)</td> </tr> <tr> <td>(100)</td> <td>(10) (10) (10) (10) (10) (10)</td> <td>(1) (1) (1)</td> </tr> <tr> <td>(100)</td> <td>(10) (10) (10) (10) (10) (10)</td> <td>(1) (1) (1)</td> </tr> <tr> <td>(100)</td> <td>(10) (10) (10) (10) (10) (10)</td> <td>(1) (1) (1)</td> </tr> <tr> <td>(100)</td> <td>(10) (10) (10) (10) (10) (10)</td> <td>(1) (1) (1)</td> </tr> </tbody> </table>	H	T	O	(100)	(10) (10) (10) (10) (10) (10)	(1) (1) (1)	(100)	(10) (10) (10) (10) (10) (10)	(1) (1) (1)	(100)	(10) (10) (10) (10) (10) (10)	(1) (1) (1)	(100)	(10) (10) (10) (10) (10) (10)	(1) (1) (1)	(100)	(10) (10) (10) (10) (10) (10)	(1) (1) (1)	<p>Use an area model and then add the parts.</p> <table border="1" data-bbox="1545 746 2120 825"> <tr> <td>100</td> <td>60</td> <td>3</td> </tr> <tr> <td>5</td> <td><math>100 \times 5 = 500</math></td> <td><math>60 \times 5 = 300</math></td> <td><math>3 \times 5 = 15</math></td> </tr> </table> <p>Use a column multiplication, including any required exchanges.</p> $  \begin{array}{r}  & 1 & 3 & 6 \\  \times & & & 6 \\  \hline  & 8 & 1 & 6 \\  & 2 & 3  \end{array}  $	100	60	3	5	$100 \times 5 = 500$	$60 \times 5 = 300$	$3 \times 5 = 15$
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100	60	3																										
5	$100 \times 5 = 500$	$60 \times 5 = 300$	$3 \times 5 = 15$																									

## Multiplying 2-digit numbers by 2-digit numbers

Partition one number into 10s and 1s, then add the parts.

$$23 \times 15 = ?$$



$$10 \times 15 = 150$$



$$10 \times 15 = 150$$



$$3 \times 15 = 45$$

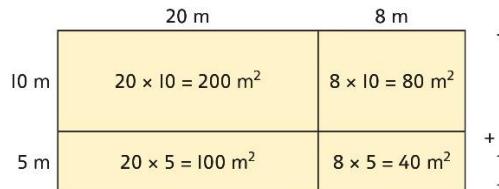
There are 345 bottles of milk in total.

$$\begin{array}{r}
 \text{H} \quad \text{T} \quad \text{O} \\
 1 \quad 5 \quad 0 \\
 1 \quad 5 \quad 0 \\
 + \quad \quad 4 \quad 5 \\
 \hline
 3 \quad 4 \quad 5
 \end{array}$$

$$23 \times 15 = 345$$

Use an area model and add the parts.

$$28 \times 15 = ?$$



$$\begin{array}{r}
 \text{H} \quad \text{T} \quad \text{O} \\
 2 \quad 0 \quad 0 \\
 1 \quad 0 \quad 0 \\
 8 \quad 0 \\
 + \quad 4 \quad 0 \\
 \hline
 4 \quad 2 \quad 0
 \end{array}$$

$$\begin{array}{r}
 3 \quad 4 \\
 \times \quad 2 \quad 7 \\
 \hline
 2 \quad 3 \quad 8
 \end{array}$$

$$34 \times 7$$

$$\begin{array}{r}
 3 \quad 4 \\
 \times \quad 2 \quad 7 \\
 \hline
 2 \quad 3 \quad 8
 \end{array}$$

$$34 \times 7$$

$$\begin{array}{r}
 6 \quad 8 \quad 0
 \end{array}$$

$$34 \times 20$$

$$\begin{array}{r}
 3 \quad 4 \\
 \times \quad 2 \quad 7 \\
 \hline
 2 \quad 3 \quad 8
 \end{array}$$

$$34 \times 7$$

$$\begin{array}{r}
 6 \quad 8 \quad 0
 \end{array}$$

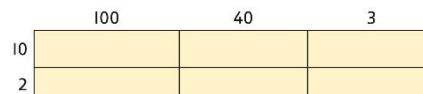
$$34 \times 20$$

$$\begin{array}{r}
 9 \quad 1 \quad 8
 \end{array}$$

$$34 \times 27$$

## Multiplying up to 4-digits by 2-digits

Use the area model then add the parts.



$$143 \times 12 = 1,716$$

There are 1,716 boxes of cereal in total.

$$143 \times 12 = 1,716$$

Use column multiplication, ensuring understanding of place value at each stage.

$$\begin{array}{r}
 \text{Th} \quad \text{H} \quad \text{T} \quad \text{O} \\
 1 \quad 0 \quad 0 \quad 0 \\
 4 \quad 0 \quad 0 \quad 0 \\
 2 \quad 0 \quad 0 \quad 0 \\
 8 \quad 0 \quad 0 \quad 0 \\
 3 \quad 0 \quad 0 \quad 0 \\
 + \quad \quad \quad \quad 6 \\
 \hline
 1 \quad 7 \quad 1 \quad 6
 \end{array}$$

$$\begin{array}{r}
 1 \quad 4 \quad 3 \\
 \times \quad 1 \quad 2 \\
 \hline
 2 \quad 8 \quad 6
 \end{array}$$

$$143 \times 2$$

$$\begin{array}{r}
 1 \quad 4 \quad 3 \quad 0 \\
 \times \quad \quad \quad \quad 1 \\
 \hline
 1 \quad 4 \quad 3 \quad 0
 \end{array}$$

$$143 \times 10$$

$$\begin{array}{r}
 1 \quad 7 \quad 1 \quad 6 \\
 \hline
 1 \quad 7 \quad 1 \quad 6
 \end{array}$$

$$143 \times 12$$

Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.

$$1,274 \times 32 = ?$$

First multiply 1,274 by 2.

$$\begin{array}{r}
 1 & 2 & 7 & 4 \\
 \times & 3 & 2 \\
 \hline
 2 & 5 & 4 & 8
 \end{array} \quad 1,274 \times 2$$

Then multiply 1,274 by 30.

$$\begin{array}{r}
 1 & 2 & 7 & 4 \\
 \times & 3 & 2 \\
 \hline
 2 & 5 & 4 & 8 \\
 3 & 8 & 2 & 2 & 0
 \end{array} \quad 1,274 \times 2 \quad 1,274 \times 30$$

Finally, find the total.

$$\begin{array}{r}
 1 & 2 & 7 & 4 \\
 \times & 3 & 2 \\
 \hline
 2 & 5 & 4 & 8 \\
 3 & 8 & 2 & 2 & 0 \\
 \hline
 4 & 0 & 7 & 6 & 8
 \end{array} \quad 1,274 \times 2 \quad 1,274 \times 30 \quad 1,274 \times 32$$

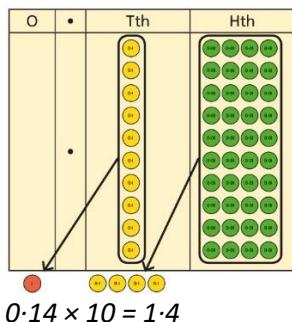
↓

$$1,274 \times 32 = 40,768$$

### Multiplying decimals by 10, 100 and 1,000

Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.

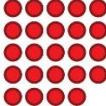
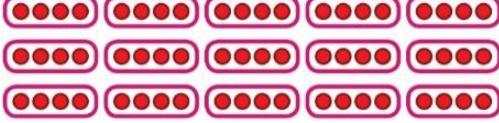
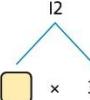
Represent multiplication by 10 as exchange on a place value grid.

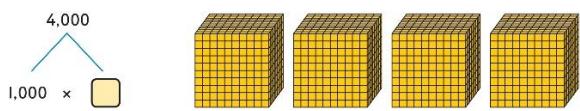
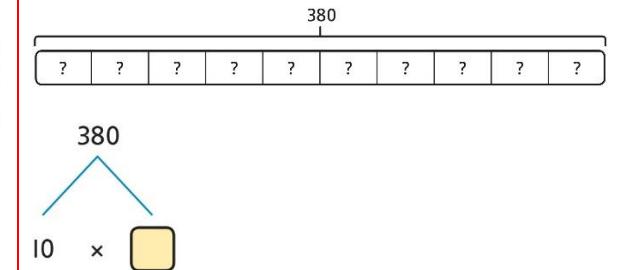
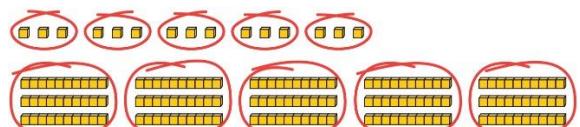
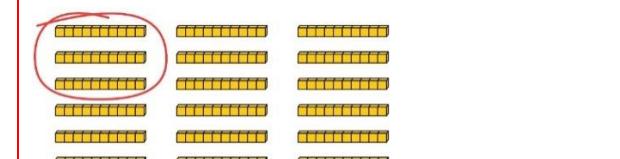


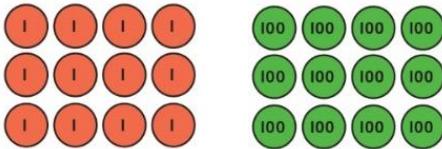
Understand how this exchange is represented on a place value chart.

Th	H	T	O	.	Tth
		2	5		5
	2	5	0		0
2	5	0	0		0

$2 \cdot 5 \times 10 = 25$   
 $2 \cdot 5 \times 100 = 250$   
 $2 \cdot 5 \times 1,000 = 2,500$

<b>Year 5</b> <b>Division</b>			
<b>Understanding factors and prime numbers</b>	<p>Use equipment to explore the factors of a given number.</p>  $24 \div 3 = 8$ $24 \div 8 = 3$ <p><i>8 and 3 are factors of 24 because they divide 24 exactly.</i></p> $24 \div 5 = 4 \text{ remainder } 4.$  <p><i>5 is not a factor of 24 because there is a remainder.</i></p>	<p>Understand that prime numbers are numbers with exactly two factors.</p> $13 \div 1 = 13$ $13 \div 2 = 6 \text{ r } 1$ $13 \div 4 = 4 \text{ r } 1$ <p><i>1 and 13 are the only factors of 13. 13 is a prime number.</i></p>	<p>Understand how to recognise prime and composite numbers.</p> <p><i>I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.</i></p> <p><i>I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.</i></p> <p><i>I know that 1 is not a prime number, as it has only 1 factor.</i></p>
<b>Understanding inverse operations and the link with multiplication, grouping and sharing</b>	<p>Use equipment to group and share and to explore the calculations that are present.</p> <p><i>I have 28 counters.</i></p> <p><i>I made 7 groups of 4. There are 28 in total.</i></p> <p><i>I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.</i></p> <p><i>I have 28 in total. I made groups of 4. There are 7 equal groups.</i></p>	<p>Represent multiplicative relationships and explore the families of division facts.</p>  $60 \div 4 = 15$ $60 \div 15 = 4$	<p>Represent the different multiplicative relationships to solve problems requiring inverse operations.</p> <p><math>12 \div 3 = \square</math></p> <p><math>12 \div \square = 3</math></p> <p><math>\square \times 3 = 12</math></p> <p><math>\square \div 3 = 12</math></p>  <p>Understand missing number problems for division calculations and know how to solve them using inverse operations.</p> $22 \div ? = 2$ $22 \div 2 = ?$ $? \div 2 = 22$ $? \div 22 = 2$

<p><b>Dividing whole numbers by 10, 100 and 1,000</b></p>	<p>Use place value equipment to support unitising for division.</p> <p><math>4,000 \div 1,000</math></p> <p></p> <p>4,000 is 4 thousands.</p> <p><math>4 \times 1,000 = 4,000</math></p> <p>So, <math>4,000 \div 1,000 = 4</math></p>	<p>Use a bar model to support dividing by unitising.</p> <p><math>380 \div 10 = 38</math></p> <p></p> <p>380 is 38 tens.</p> <p><math>38 \times 10 = 380</math></p> <p><math>10 \times 38 = 380</math></p> <p>So, <math>380 \div 10 = 38</math></p>	<p>Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.</p> <p></p> <p><math>3,200 \div 100 = ?</math></p> <p>3,200 is 3 thousands and 2 hundreds.</p> <p><math>200 \div 100 = 2</math></p> <p><math>3,000 \div 100 = 30</math></p> <p><math>3,200 \div 100 = 32</math></p> <p>So, the digits will move two places to the right.</p>
<p><b>Dividing by multiples of 10, 100 and 1,000</b></p>	<p>Use place value equipment to represent known facts and unitising.</p> <p></p> <p>15 ones put into groups of 3 ones. There are 5 groups.</p> <p><math>15 \div 3 = 5</math></p> <p>15 tens put into groups of 3 tens. There are 5 groups.</p> <p><math>150 \div 30 = 5</math></p>	<p>Represent related facts with place value equipment when dividing by unitising.</p> <p></p> <p>180 is 18 tens.</p> <p>18 tens divided into groups of 3 tens. There are 6 groups.</p> <p><math>180 \div 30 = 6</math></p>	<p>Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.</p> <p><math>3,000 \div 5 = 600</math></p> <p><math>3,000 \div 50 = 60</math></p> <p><math>3,000 \div 500 = 6</math></p> <p><math>5 \times 600 = 3,000</math></p> <p><math>50 \times 60 = 3,000</math></p> <p><math>500 \times 6 = 3,000</math></p>



12 ones divided into groups of 4. There are 3 groups.

12 hundreds divided into groups of 4 hundreds.  
There are 3 groups.

$$1200 \div 400 = 3$$

### Dividing up to four digits by a single digit using short division

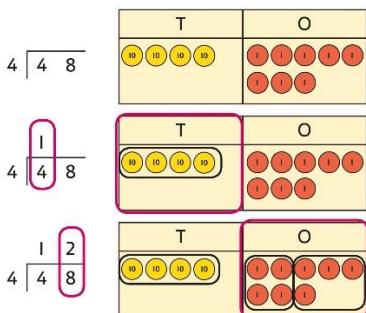
Explore grouping using place value equipment.

$$268 \div 2 = ?$$

There is 1 group of 2 hundreds.  
There are 3 groups of 2 tens.  
There are 4 groups of 2 ones.

$$264 \div 2 = 134$$

Use place value equipment on a place value grid alongside short division.  
The model uses grouping.  
A sharing model can also be used, although the model would need adapting.



Lay out the problem as a short division.

There is 1 group of 4 in 4 tens.  
There are 2 groups of 4 in 8 ones.

Work with divisions that require exchange.

Use short division for up to 4-digit numbers divided by a single digit.

$$\begin{array}{r} 0 \ 5 \ 5 \ 6 \\ 7 \overline{)3 \ 3 \ 8 \ 3 \ 9 \ 4 \ 2} \\ \end{array}$$

$$3,892 \div 7 = 556$$

Use multiplication to check.

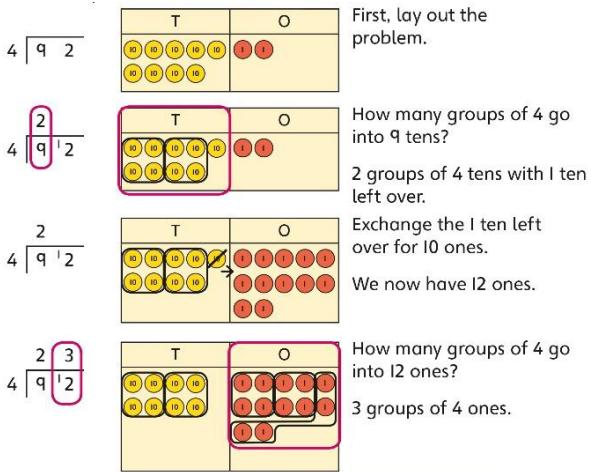
$$556 \times 7 = ?$$

$$6 \times 7 = 42$$

$$50 \times 7 = 350$$

$$500 \times 7 = 3500$$

$$3,500 + 350 + 42 = 3,892$$



### Understanding remainders

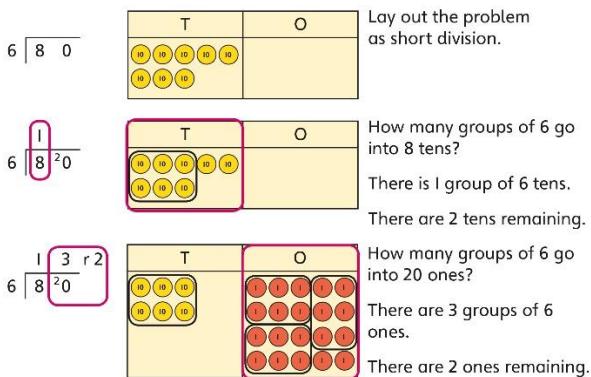
Understand remainders using concrete versions of a problem.

*80 cakes divided into trays of 6.*



*80 cakes in total. They make 13 groups of 6, with 2 remaining.*

Use short division and understand remainders as the last remaining 1s.

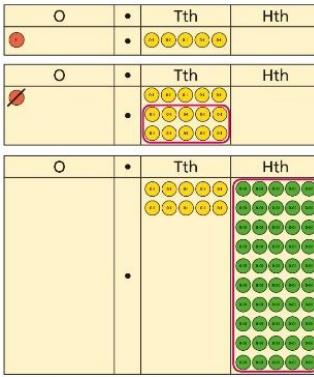
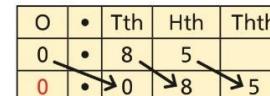
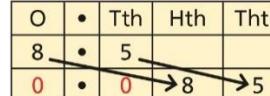
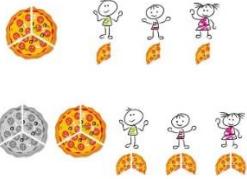


In problem solving contexts, represent divisions including remainders with a bar model.

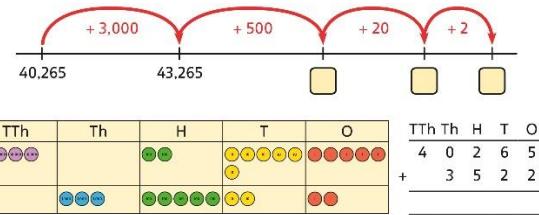
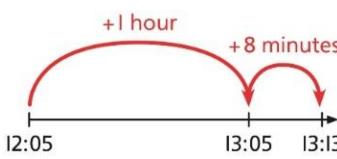
$$\begin{array}{r} 683 \\ \hline 136 \quad 136 \quad 136 \quad 136 \quad 136 \quad 3 \end{array}$$

$$683 = 136 \times 5 + 3$$

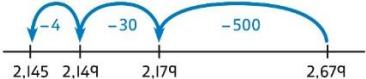
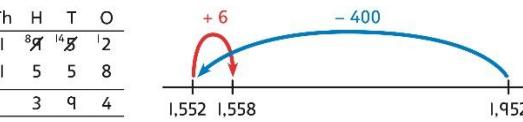
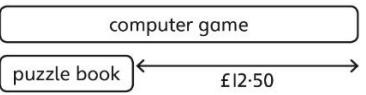
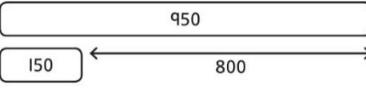
$$683 \div 5 = 136 \text{ r } 3$$

<b>Dividing decimals by 10, 100 and 1,000</b>	<p>Understand division by 10 using exchange.</p> <p><i>2 ones are 20 tenths.</i></p> <p><i>20 tenths divided by 10 is 2 tenths.</i></p>	<p>Represent division using exchange on a place value grid.</p>  <p><i>1·5 is 1 one and 5 tenths.</i>  <i>This is equivalent to 10 tenths and 50 hundredths.</i>  <i>10 tenths divided by 10 is 1 tenth.</i>  <i>50 hundredths divided by 10 is 5 hundredths.</i>  <i>1·5 divided by 10 is 1 tenth and 5 hundredths.</i>  <math>1·5 \div 10 = 0·15</math></p>	<p>Understand the movement of digits on a place value grid.</p>  <p><math>0·85 \div 10 = 0·085</math></p>  <p><math>8·5 \div 100 = 0·085</math></p>
<b>Understanding the relationship between fractions and division</b>	<p>Use sharing to explore the link between fractions and division.</p> <p><i>1 whole shared between 3 people. Each person receives one-third.</i></p> 	<p>Use a bar model and other fraction representations to show the link between fractions and division.</p>  $1 \div 3 = \frac{1}{3}$	<p>Use the link between division and fractions to calculate divisions.</p> $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$ $11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$

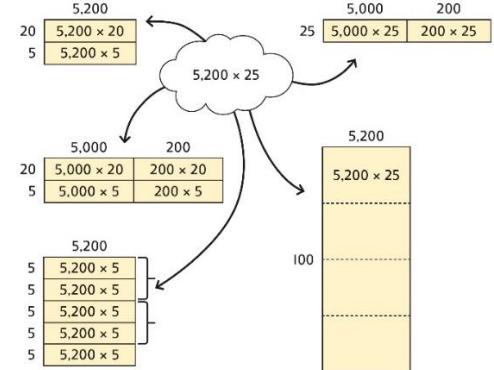
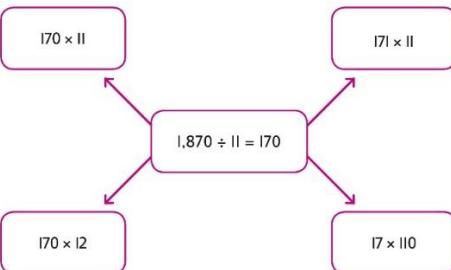
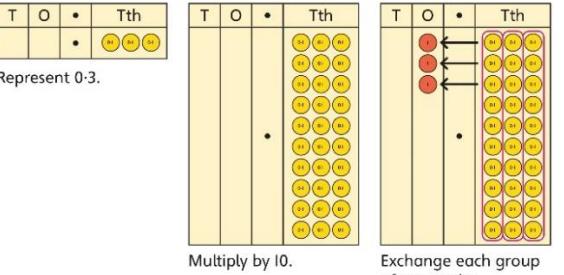
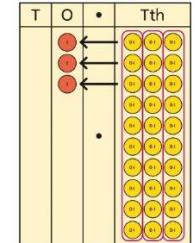
Year 6

	Concrete	Pictorial	Abstract		
<b>Year 6 Addition</b>					
<b>Comparing and selecting efficient methods</b>	<p>Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.</p> 	<p>Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation.</p> <p>Compare written and mental methods alongside place value representations.</p> 	<p>Use column addition where mental methods are not efficient. Recognise common errors with column addition.</p> <p><math>32,145 + 4,302 = ?</math></p> <table style="display: flex; justify-content: space-around; margin-top: 10px;"> <tr> <td style="text-align: center;"> <math display="block">\begin{array}{r} \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\ 3 \text{ } 2 \text{ } 1 \text{ } 4 \text{ } 5 \\ + \text{ } 4 \text{ } 3 \text{ } 0 \text{ } 2 \\ \hline 3 \text{ } 6 \text{ } 4 \text{ } 4 \text{ } 7 \end{array}</math> </td> <td style="text-align: center;"> <math display="block">\begin{array}{r} \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\ 3 \text{ } 2 \text{ } 1 \text{ } 4 \text{ } 5 \\ + \text{ } 4 \text{ } 3 \text{ } 0 \text{ } 2 \\ \hline 7 \text{ } 5 \text{ } 1 \text{ } 6 \text{ } 5 \end{array}</math> </td> </tr> </table> <p>Which method has been completed accurately?</p> <p>What mistake has been made?</p> <p>Column methods are also used for decimal additions where mental methods are not efficient.</p>  <p><math display="block">\begin{array}{r} \text{H} \text{ T} \text{ O} \cdot \text{Tth} \text{ Hth} \\ 1 \text{ } 4 \text{ } 0 \cdot 0 \text{ } 9 \\ + \text{ } 4 \text{ } 9 \cdot 8 \text{ } 9 \\ \hline 1 \text{ } 8 \text{ } 9 \cdot 9 \text{ } 8 \end{array}</math></p>	$\begin{array}{r} \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\ 3 \text{ } 2 \text{ } 1 \text{ } 4 \text{ } 5 \\ + \text{ } 4 \text{ } 3 \text{ } 0 \text{ } 2 \\ \hline 3 \text{ } 6 \text{ } 4 \text{ } 4 \text{ } 7 \end{array}$	$\begin{array}{r} \text{TTh} \text{ Th} \text{ H} \text{ T} \text{ O} \\ 3 \text{ } 2 \text{ } 1 \text{ } 4 \text{ } 5 \\ + \text{ } 4 \text{ } 3 \text{ } 0 \text{ } 2 \\ \hline 7 \text{ } 5 \text{ } 1 \text{ } 6 \text{ } 5 \end{array}$
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<p><b>Selecting mental methods for larger numbers where appropriate</b></p> <p>Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.</p> <p></p> <p><math>2,411,301 + 500,000 = ?</math></p> <p><i>This would be 5 more counters in the HTh place.</i></p> <p><i>So, the total is 2,911,301.</i></p> <p><math>2,411,301 + 500,000 = 2,911,301</math></p>	<p>Use a bar model to support thinking in addition problems.</p> <p><math>257,000 + 99,000 = ?</math></p> <p></p> <p><i>I added 100 thousands then subtracted 1 thousand.</i></p> <p><math>257 \text{ thousands} + 100 \text{ thousands} = 357 \text{ thousands}</math></p> <p><math>257,000 + 100,000 = 357,000</math></p> <p><math>357,000 - 1,000 = 356,000</math></p> <p><i>So, <math>257,000 + 99,000 = 356,000</math></i></p>	<p>Use place value and unitising to support mental calculations with larger numbers.</p> <p><math>195,000 + 6,000 = ?</math></p> <p><math>195 + 5 + 1 = 201</math></p> <p><i>195 thousands + 6 thousands = 201 thousands</i></p> <p><i>So, <math>195,000 + 6,000 = 201,000</math></i></p>
<p><b>Understanding order of operations in calculations</b></p> <p><math>3 \times 5 - 2 = ?</math></p> <p></p> <p></p> <p><math>3 \times (5 - 2)</math></p> <p></p> <p><math>(3 \times 5) - 2</math></p> <p></p>	<p>Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations.</p> <p></p> <p><math>16 \times 4</math></p> <p><math>\text{cab } [4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4 \ 4]</math></p> <p><math>\text{trailer } [6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6 \ 6]</math></p> <p><math>16 \times 6</math></p> <p>This can be written as: <math>16 \times 4 + 16 \times 6</math></p> <p><math>(16 \times 4) + (16 \times 6)</math></p> <p><math>64 + 96 = 160</math></p>	<p>Understand the correct order of operations in calculations without brackets.</p> <p>Understand how brackets affect the order of operations in a calculation.</p> <p><math>4 + 6 \times 16</math></p> <p><math>4 + 96 = 100</math></p> <p><math>(4 + 6) \times 16</math></p> <p><math>10 \times 16 = 160</math></p>

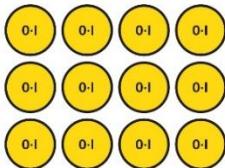
<b>Year 6</b> <b>Subtraction</b>			
<b>Comparing and selecting efficient methods</b>	<p>Use counters on a place value grid to represent subtractions of larger numbers.</p> 	<p>Compare subtraction methods alongside place value representations.</p>  <p>Th H T O 2 6 7 9 - 5 3 4 ————— 2 1 4 5</p>	<p>Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy.</p>  <p>Use column subtraction for decimal problems, including in the context of measure.</p> 
<b>Subtracting mentally with larger numbers</b>		<p>Use a bar model to show how unitising can support mental calculations.</p> <p><math>950,000 - 150,000</math> That is 950 thousands - 150 thousands</p>  <p>So, the difference is 800 thousands. <math>950,000 - 150,000 = 800,000</math></p>	<p>Subtract efficiently from powers of 10.</p> <p><math>10,000 - 500 = ?</math></p>

<b>Year 6</b> <b>Multiplication</b>																																							
<b>Multiplying up to a 4-digit number by a single digit number</b>	<p>Use equipment to explore multiplications.</p> <p>4 groups of 2,345</p> <p>This is a multiplication:</p> $4 \times 2,345$ $2,345 \times 4$	<p>Use place value equipment to compare methods.</p> <p><b>Method 1</b></p> <p><b>Method 2</b></p> <p> <math>4 \times 3,000</math>   <math>4 \times 200</math>   <math>4 \times 20</math>   <math>4 \times 5</math>  <math>12,000 + 800 + 80 + 20 = 12,900</math> </p>	<p>Understand area model and short multiplication.</p> <p>Compare and select appropriate methods for specific multiplications.</p> <p><b>Method 3</b></p> <table border="1"> <tr> <td>3,000</td> <td>200</td> <td>20</td> <td>5</td> </tr> <tr> <td>4</td> <td>12,000</td> <td>800</td> <td>80</td> <td>20</td> </tr> </table> <p><math>12,000 + 800 + 80 + 20 = 12,900</math></p> <p><b>Method 4</b></p> <table border="1"> <tr> <td>3</td> <td>2</td> <td>2</td> <td>5</td> </tr> <tr> <td></td> <td></td> <td>4</td> <td></td> </tr> <tr> <td>1</td> <td>2</td> <td>9</td> <td>0</td> </tr> <tr> <td></td> <td></td> <td>1</td> <td>2</td> </tr> </table>	3,000	200	20	5	4	12,000	800	80	20	3	2	2	5			4		1	2	9	0			1	2											
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1	2	9	0																																				
		1	2																																				
<b>Multiplying up to a 4-digit number by a 2-digit number</b>	<p>Use an area model alongside written multiplication.</p> <p><b>Method 1</b></p> <table border="1"> <tr> <td>1,000</td> <td>200</td> <td>30</td> <td>5</td> </tr> <tr> <td>20</td> <td>20,000</td> <td>4,000</td> <td>600</td> <td>100</td> </tr> <tr> <td>1</td> <td>1,000</td> <td>200</td> <td>30</td> <td>5</td> </tr> </table> <p> <math>\begin{array}{r} 1 &amp; 2 &amp; 3 &amp; 5 \\ \times &amp; 2 &amp; 1 \\ \hline &amp; 5 &amp; &amp; 1 \times 5 \\ &amp; 3 &amp; 0 &amp; 1 \times 30 \\ &amp; 2 &amp; 0 &amp; 0 1 \times 200 \\ &amp; 1 &amp; 0 &amp; 0 &amp; 1 \times 1,000 \\ &amp; 1 &amp; 0 &amp; 0 &amp; 20 \times 5 \\ &amp; 6 &amp; 0 &amp; 0 &amp; 20 \times 30 \\ &amp; 4 &amp; 0 &amp; 0 &amp; 20 \times 200 \\ \hline 2 &amp; 0 &amp; 0 &amp; 0 &amp; 20 \times 1,000 \\ \hline 2 &amp; 5 &amp; 9 &amp; 3 &amp; 5 \\ \hline \end{array}</math> <math>21 \times 1,235</math> </p>	1,000	200	30	5	20	20,000	4,000	600	100	1	1,000	200	30	5	<p>Use compact column multiplication with understanding of place value at all stages.</p> <table border="1"> <tr> <td>1</td> <td>2</td> <td>3</td> <td>5</td> </tr> <tr> <td></td> <td></td> <td>2</td> <td>1</td> </tr> <tr> <td>1</td> <td>2</td> <td>3</td> <td>5</td> <td><math>1 \times 1,235</math></td> </tr> <tr> <td>2</td> <td>4</td> <td>7</td> <td>0</td> <td><math>20 \times 1,235</math></td> </tr> <tr> <td>2</td> <td>5</td> <td>9</td> <td>3</td> <td><math>21 \times 1,235</math></td> </tr> </table>	1	2	3	5			2	1	1	2	3	5	$1 \times 1,235$	2	4	7	0	$20 \times 1,235$	2	5	9	3	$21 \times 1,235$
1,000	200	30	5																																				
20	20,000	4,000	600	100																																			
1	1,000	200	30	5																																			
1	2	3	5																																				
		2	1																																				
1	2	3	5	$1 \times 1,235$																																			
2	4	7	0	$20 \times 1,235$																																			
2	5	9	3	$21 \times 1,235$																																			

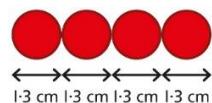
<p><b>Using knowledge of factors and partitions to compare methods for multiplications</b></p>	<p>Use equipment to understand square numbers and cube numbers.</p>  $5 \times 5 = 5^2 = 25$ $5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	<p>Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.</p>  <p>Represent and compare methods using a bar model.</p>	<p>Use a known fact to generate families of related facts.</p>  <p>Use factors to calculate efficiently.</p> $  \begin{aligned}  15 \times 16 &= 3 \times 5 \times 2 \times 8 \\  &= 3 \times 8 \times 2 \times 5 \\  &= 24 \times 10 \\  &= 240  \end{aligned}  $
<p><b>Multiplying by 10, 100 and 1,000</b></p>	<p>Use place value equipment to explore exchange in decimal multiplication.</p>  <p>Represent 0-3.</p> <p>Multiply by 10.</p> <p>Exchange each group of ten tenths.</p> <p><math>0.3 \times 10 = ?</math></p> <p>0.3 is 3 tenths.</p> <p>10 × 3 tenths are 30 tenths.</p> <p>30 tenths are equivalent to 3 ones.</p>	<p>Understand how the exchange affects decimal numbers on a place value grid.</p>  <p><math>0.3 \times 10 = 3</math></p>	<p>Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000.</p> $  \begin{aligned}  8 \times 100 &= 800 \\  8 \times 300 &= 800 \times 3 \\  &= 2,400  \end{aligned}  $ $  \begin{aligned}  2.5 \times 10 &= 25 \\  2.5 \times 20 &= 2.5 \times 10 \times 2 \\  &= 50  \end{aligned}  $

## Multiplying decimals

Explore decimal multiplications using place value equipment and in the context of measures.



3 groups of 4 tenths is 12 tenths.  
4 groups of 3 tenths is 12 tenths.



$$\begin{aligned}4 \times 1 \text{ cm} &= 4 \text{ cm} \\4 \times 0.3 \text{ cm} &= 1.2 \text{ cm} \\4 \times 1.3 &= 4 + 1.2 = 5.2 \text{ cm}\end{aligned}$$

Represent calculations on a place value grid.

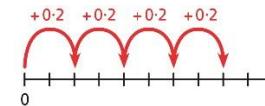
$$3 \times 3 = 9$$

$$3 \times 0.3 = 0.9$$

T	O	•	Tth
		•	

Understand the link between multiplying decimals and repeated addition.

T	O	•	Tth
		•	



Use known facts to multiply decimals.

$$4 \times 3 = 12$$

$$4 \times 0.3 = 1.2$$

$$4 \times 0.03 = 0.12$$

$$20 \times 5 = 100$$

$$20 \times 0.5 = 10$$

$$20 \times 0.05 = 1$$

Find families of facts from a known multiplication.

*I know that  $18 \times 4 = 72$ .*

*This can help me work out:*

$$1.8 \times 4 = ?$$

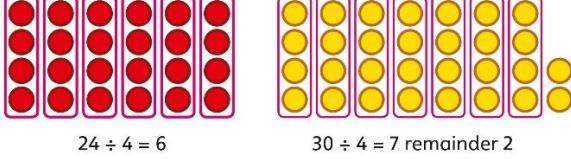
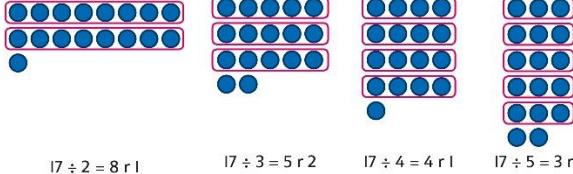
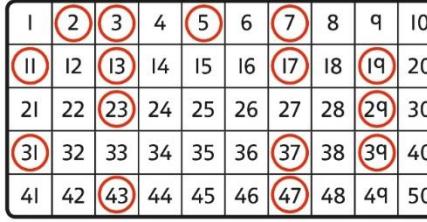
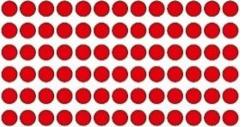
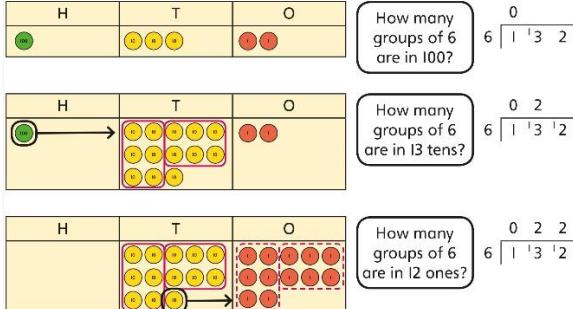
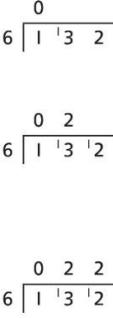
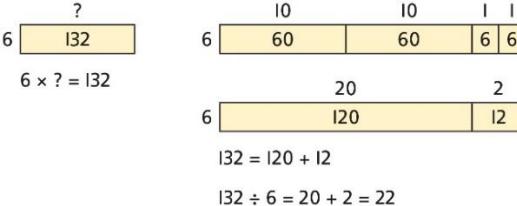
$$18 \times 0.4 = ?$$

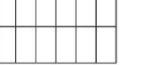
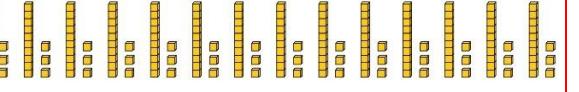
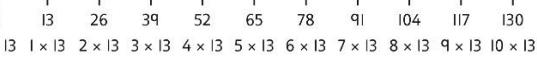
$$180 \times 0.4 = ?$$

$$18 \times 0.04 = ?$$

Use a place value grid to understand the effects of multiplying decimals.

	H	T	O	•	Tth	Hth
$2 \times 3$			6	•		
$0.2 \times 3$			0	•	6	
$0.02 \times 3$				•		

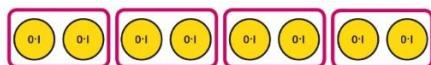
Year 6 Division			
Understanding factors	<p>Use equipment to explore different factors of a number.</p>  <p><i>4 is a factor of 24 but is not a factor of 30.</i></p>	<p>Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.</p> 	<p>Recognise and know primes up to 100. Understand that 2 is the only even prime, and that 1 is not a prime number.</p> 
Dividing by a single digit	<p>Use equipment to make groups from a total.</p>  <p><i>There are 78 in total. There are 6 groups of 13. There are 13 groups of 6.</i></p>		<p>Use short division to divide by a single digit.</p>  <p><i>Use an area model to link multiplication and division.</i></p> 

<b>Dividing by a 2-digit number using factors</b>	<p>Understand that division by factors can be used when dividing by a number that is not prime.</p>	<p>Use factors and repeated division.</p> $1,260 \div 14 = ?$ <p>1,260  </p> $1,260 \div 2 = 630$ $630 \div 7 = 90$ $1,260 \div 14 = 90$	<p>Use factors and repeated division where appropriate.</p> $2,100 \div 12 = ?$ <p><math>2,100 \rightarrow \boxed{\div 2} \rightarrow \boxed{\div 6} \rightarrow</math>  <math>2,100 \rightarrow \boxed{\div 6} \rightarrow \boxed{\div 2} \rightarrow</math>  <math>2,100 \rightarrow \boxed{\div 3} \rightarrow \boxed{\div 4} \rightarrow</math>  <math>2,100 \rightarrow \boxed{\div 4} \rightarrow \boxed{\div 3} \rightarrow</math>  <math>2,100 \rightarrow \boxed{\div 3} \rightarrow \boxed{\div 2} \rightarrow \boxed{\div 2} \rightarrow</math></p>
<b>Dividing by a 2-digit number using long division</b>	<p>Use equipment to build numbers from groups.</p>  <p><i>182 divided into groups of 13. There are 14 groups.</i></p>	<p>Use an area model alongside written division to model the process.</p> $377 \div 13 = ?$ <p><math>\begin{array}{r} 377 \\ \hline 13 \end{array}</math></p> <p><math>\begin{array}{r} 10 \quad ? \\ \hline 13 \end{array}</math></p> <p><math>\begin{array}{r} 10 \quad 10 \quad ? \\ \hline 13 \end{array}</math></p> <p><math>\begin{array}{r} 29 \\ \hline 10 \quad 10 \quad q \\ \hline 13 \end{array}</math></p> $377 \div 13 = 29$	<p>Use long division where factors are not useful (for example, when dividing by a 2-digit prime number). Write the required multiples to support the division process.</p> $377 \div 13 = ?$ <p></p> <p><math>\begin{array}{r} 3 \ 7 \ 7 \\ - \ 1 \ 3 \ 0 \quad 10 \\ \hline 2 \ 4 \ 7 \\ - \ 1 \ 3 \ 0 \quad 10 \\ \hline 1 \ 1 \ 7 \\ - \ 1 \ 1 \ 7 \quad q \\ \hline 0 \quad 29 \end{array}</math></p> $377 \div 13 = 29$ <p>A slightly different layout may be used, with the division completed above rather than at the side.</p>

			$  \begin{array}{r}  3 \\  21 \overline{)7 \ 9 \ 8} \\  - 6 \ 3 \ 0 \\  \hline 1 \ 6 \ 8  \end{array}  $ $  \begin{array}{r}  3 \ 8 \\  21 \overline{)7 \ 9 \ 8} \\  - 6 \ 3 \ 0 \\  \hline 1 \ 6 \ 8 \\  - 1 \ 6 \ 8 \\  \hline 0  \end{array}  $
<b>Dividing by 10, 100 and 1,000</b>	<p>Use place value equipment to explore division as exchange.</p> <p>0 • Tth Hth Thth</p> <p>0 • Tth Hth Thth</p> <p>Exchange each 0-1 for ten 0-01s.</p> <p>Divide 20 counters by 10.</p> <p>0.2 is 2 tenths. 2 tenths is equivalent to 20 hundredths. 20 hundredths divided by 10 is 2 hundredths.</p>	<p>Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.</p> <p>12</p> <p>1-2</p> <p>1-2 x 10 = 12</p> <p>H T O • Tth Hth</p> <p>1-2</p> <p>1-2 ÷ 10 = 1-2</p> <p>Understand how to divide using division by 10, 100 and 1,000.</p> <p>12 ÷ 20 = ?</p> <p>12</p> <p>1-2</p> <p>12 ÷ 10 = 1-2</p> <p>1.2</p> <p>1-2</p> <p>1-2 ÷ 2 = 0.6</p>	<p>Use knowledge of factors to divide by multiples of 10, 100 and 1,000.</p> <p>40 ÷ 50 = <input type="text"/></p> <p>40 → <input type="text"/> ÷ 10 → <input type="text"/> ÷ 5 → ?</p> <p>40 → <input type="text"/> ÷ 5 → <input type="text"/> ÷ 10 → ?</p> <p>40 ÷ 5 = 8</p> <p>8 ÷ 10 = 0.8</p> <p>So, 40 ÷ 50 = 0.8</p>

**Dividing decimals**

Use place value equipment to explore division of decimals.



*8 tenths divided into 4 groups. 2 tenths in each group.*

Use a bar model to represent divisions.

0.8			
?	?	?	?

$$4 \times 2 = 8$$

$$8 \div 4 = 2$$

$$\text{So, } 4 \times 0.2 = 0.8 \quad 0.8 \div 4 = 0.2$$

Use short division to divide decimals with up to 2 decimal places.

$$8 \overline{)4 \cdot 2 \ 4}$$

0 .

$$8 \overline{)4 \cdot 4 \ 2 \ 4}$$

0 .

$$8 \overline{)4 \cdot 4 \ 2 \ 2 \ 4}$$

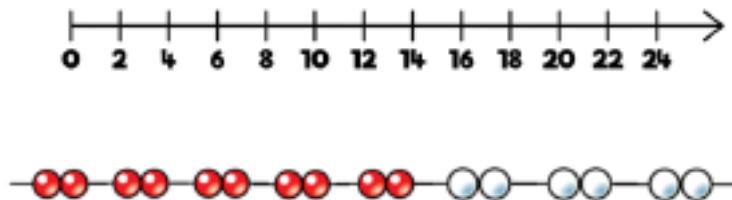
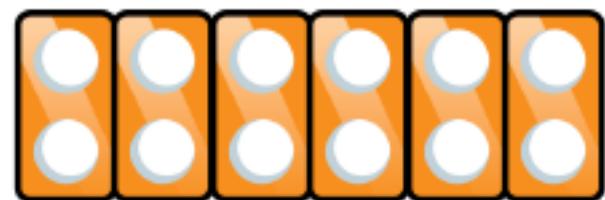
0 .

$$8 \overline{)4 \cdot 4 \ 2 \ 2 \ 4}$$

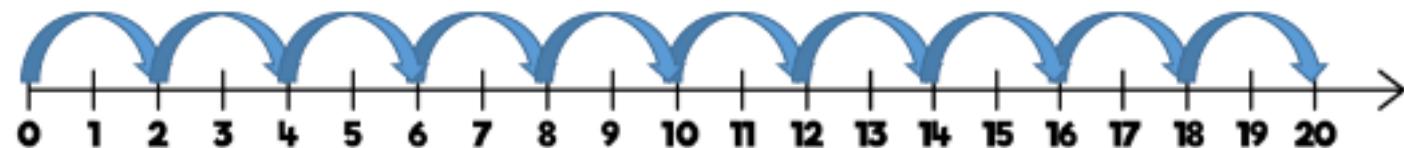
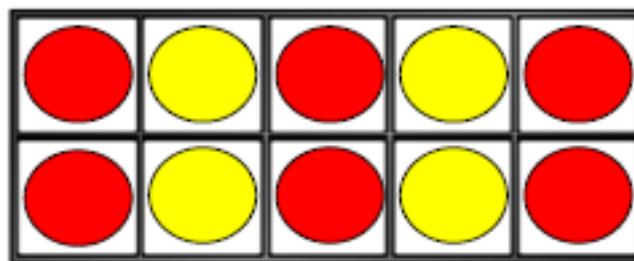
3

## Times Tables

### Skill: 2 times table



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50



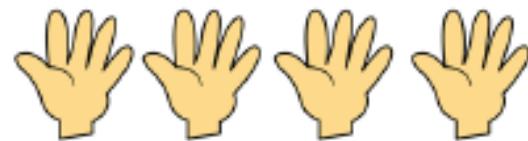
### Year: 2

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

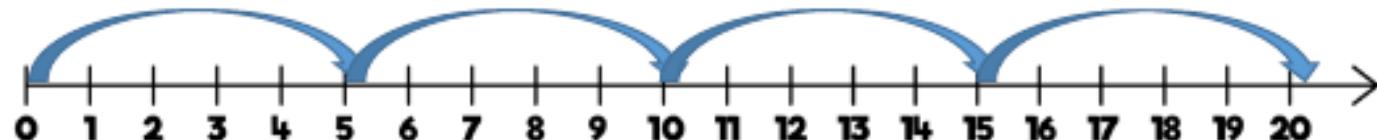
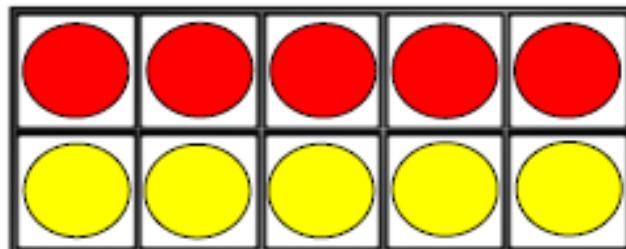
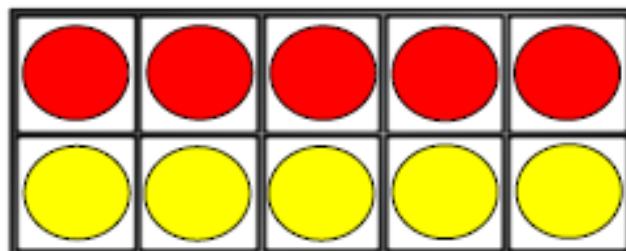
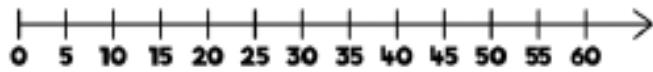
Look for patterns in the two times table, using concrete manipulatives to support. Notice how all the numbers are even and there is a pattern in the ones.

Use different models to develop fluency.

## Skill: 5 times table



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

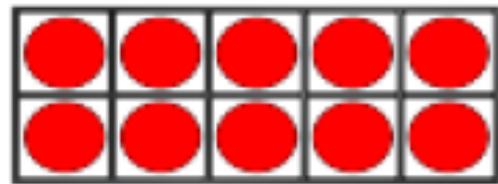
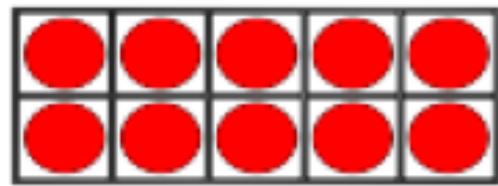
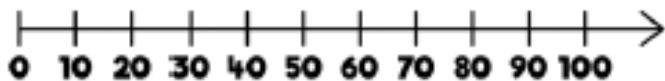


Year: 2

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the five times table, using concrete manipulatives to support. Notice the pattern in the ones as well as highlighting the odd, even, odd, even pattern.

## Skill: 10 times table



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



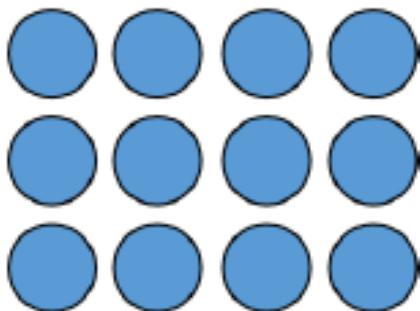
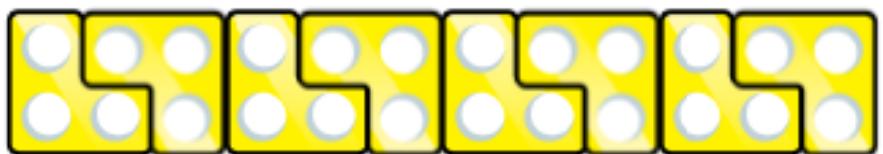
## Year: 2

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

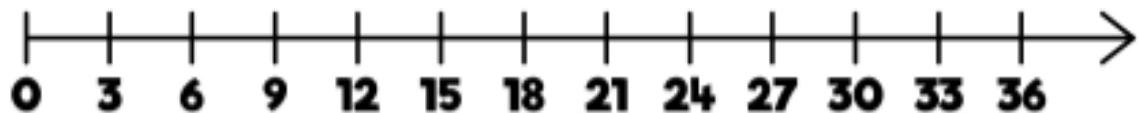
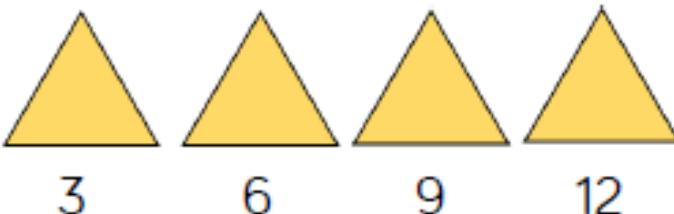
Look for patterns in the ten times table, using concrete manipulatives to support. Notice the pattern in the digits—the ones are always 0, and the tens increase by 1 ten each time.

## Skill: 3 times table

Year: 3



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

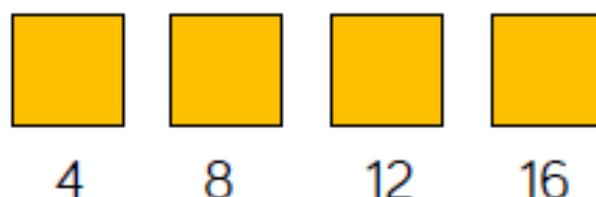
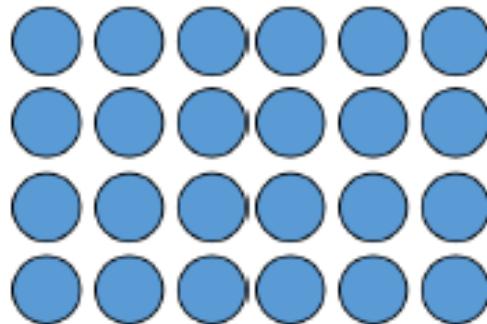
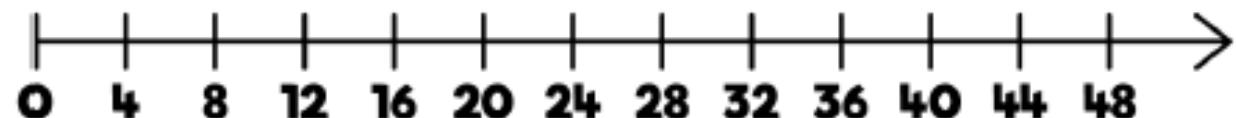
Look for patterns in the three times table, using concrete manipulatives to support. Notice the odd, even, odd, even pattern using number shapes to support. Highlight the pattern in the ones using a hundred square.

## Skill: 4 times table



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

4	8	12	16	20
24	28	32	36	40
44	48	52	56	60



**Year: 3**

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the four times table, using manipulatives to support. Make links to the 2 times table, seeing how each multiple is double the twos. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

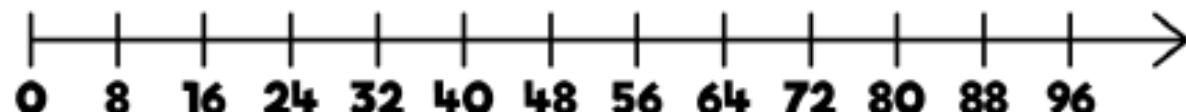
## Skill: 8 times table



8      16      24      32

8	16	24	32	40
48	56	64	72	80

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Year: 3

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the eight times table, using manipulatives to support. Make links to the 4 times table, seeing how each multiple is double the fours. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

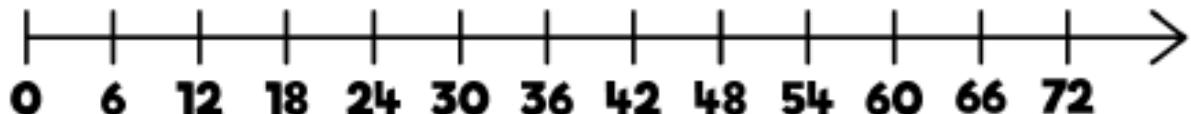
## Skill: 6 times table

Year: 4



6	12	18	24	30
36	42	48	54	60
66	72	78	84	90

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the six times table, using manipulatives to support. Make links to the 3 times table, seeing how each multiple is double the threes. Notice the pattern in the ones within each group of five multiples.

Highlight that all the multiples are even using number shapes to support.

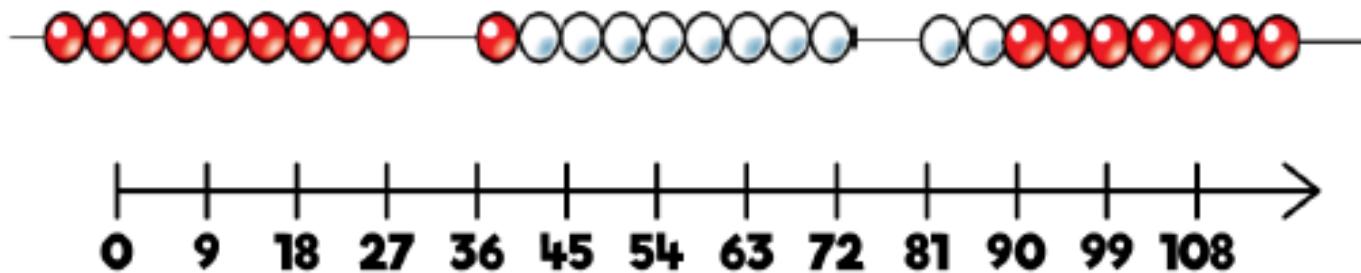
## Skill: 9 times table

Year: 4



9	18	27	36	45
54	63	72	81	90

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd, even pattern within the multiples.

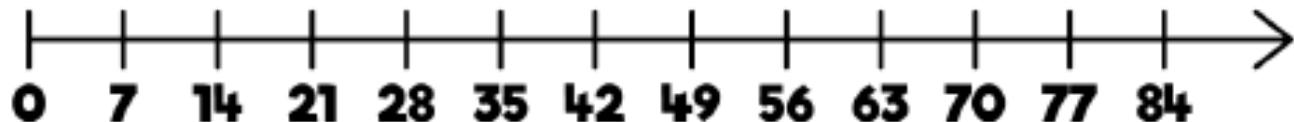
## Skill: 7 times table

Year: 4



7	14	21	28	35
42	49	56	63	70

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Encourage daily counting in multiples both forwards and backwards, supported by a number line or a hundred square. The seven times table can be trickier to learn due to the lack of obvious pattern in the numbers, however they already know several facts due to commutativity. Children can still see the odd, even pattern in the multiples using number shapes to support.

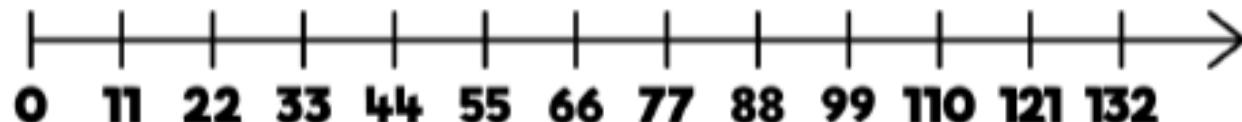
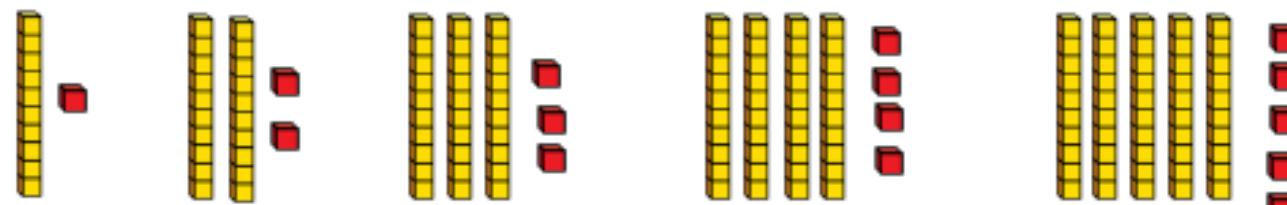
## Skill: 11 times table

Year: 4

11	22	33	44	55	66
77	88	99	110	121	132



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

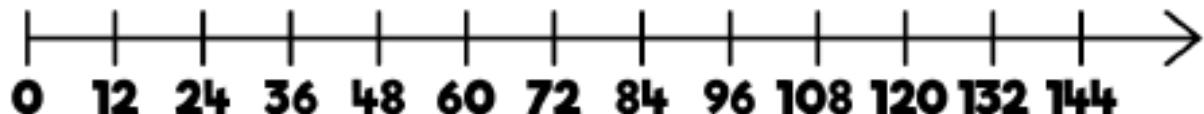
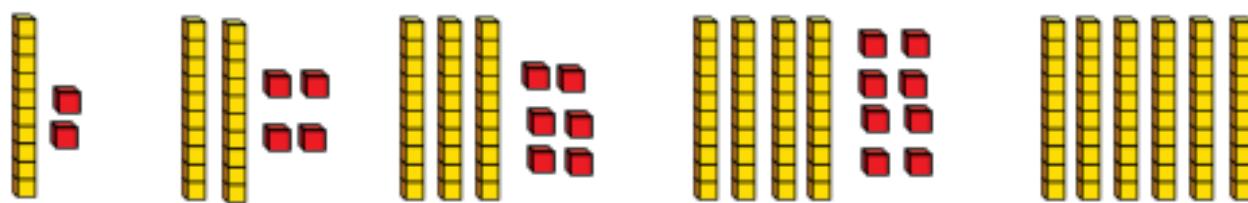
Look for patterns in the eleven times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support. Also consider the pattern after crossing 100

## Skill: 12 times table

12	24	36	48	60
72	84	96	108	120
132	144			



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Year: 4

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the 12 times table, using manipulatives to support. Make links to the 6 times table, seeing how each multiple is double the sixes. Notice the pattern in the ones within each group of five multiples. The hundred square can support in highlighting this pattern.